

19.5 For aluminum, we want to compute the Debye temperature, θ_D , given the expression for A in Equation 19.2 and the heat capacity at 15 K. First of all, let us determine the magnitude of A , as

$$\begin{aligned} A &= \frac{C_v}{T^3} \\ &= \frac{(4.60 \text{ J/mol} \cdot \text{K})(1 \text{ kg}/1000 \text{ g})(26.98 \text{ g/mol})}{(15 \text{ K})^3} \\ &= 3.68 \times 10^{-5} \text{ J/mol} \cdot \text{K}^4 \end{aligned}$$

As stipulated in the problem statement

$$A = \frac{12\pi^4 R}{5\theta_D^3}$$

Or, solving for θ_D

$$\begin{aligned} \theta_D &= \left(\frac{12\pi^4 R}{5A} \right)^{1/3} \\ &= \left[\frac{(12)(\pi)^4 (8.31 \text{ J/mol} \cdot \text{K})}{(5)(3.68 \times 10^{-5} \text{ J/mol} \cdot \text{K}^4)} \right]^{1/3} = 375 \text{ K} \end{aligned}$$