

18.48 For this problem, we are given, for NaCl, the activation energy (173,000 J/mol) and preexponential ( $4.0 \times 10^{-4} \text{ m}^2/\text{s}$ ) for the diffusion coefficient of  $\text{Na}^+$  and are asked to compute the mobility for a  $\text{Na}^+$  ion at 873 K. The mobility,  $\mu_{\text{Na}^+}$ , may be computed using Equation 18.23; however, this expression also includes the diffusion coefficient  $D_{\text{Na}^+}$ , which is determined using Equation 5.8 as

$$\begin{aligned} D_{\text{Na}^+} &= D_0 \exp\left(-\frac{Q_d}{RT}\right) \\ &= (4.0 \times 10^{-4} \text{ m}^2/\text{s}) \exp\left[-\frac{173,000 \text{ J/mol}}{(8.31 \text{ J/mol-K})(873 \text{ K})}\right] \\ &= 1.76 \times 10^{-14} \text{ m}^2/\text{s} \end{aligned}$$

Now solving for  $\mu_{\text{Na}^+}$  yields

$$\begin{aligned} \mu_{\text{Na}^+} &= \frac{n_{\text{Na}^+} e D_{\text{Na}^+}}{kT} \\ &= \frac{(1)(1.602 \times 10^{-19} \text{ C/atom})(1.76 \times 10^{-14} \text{ m}^2/\text{s})}{(1.38 \times 10^{-23} \text{ J/atom-K})(873 \text{ K})} \\ &= 2.34 \times 10^{-13} \text{ m}^2/\text{V-s} \end{aligned}$$

(Note: the value of  $n_{\text{Na}^+}$  is unity, since the valence for sodium is one.)