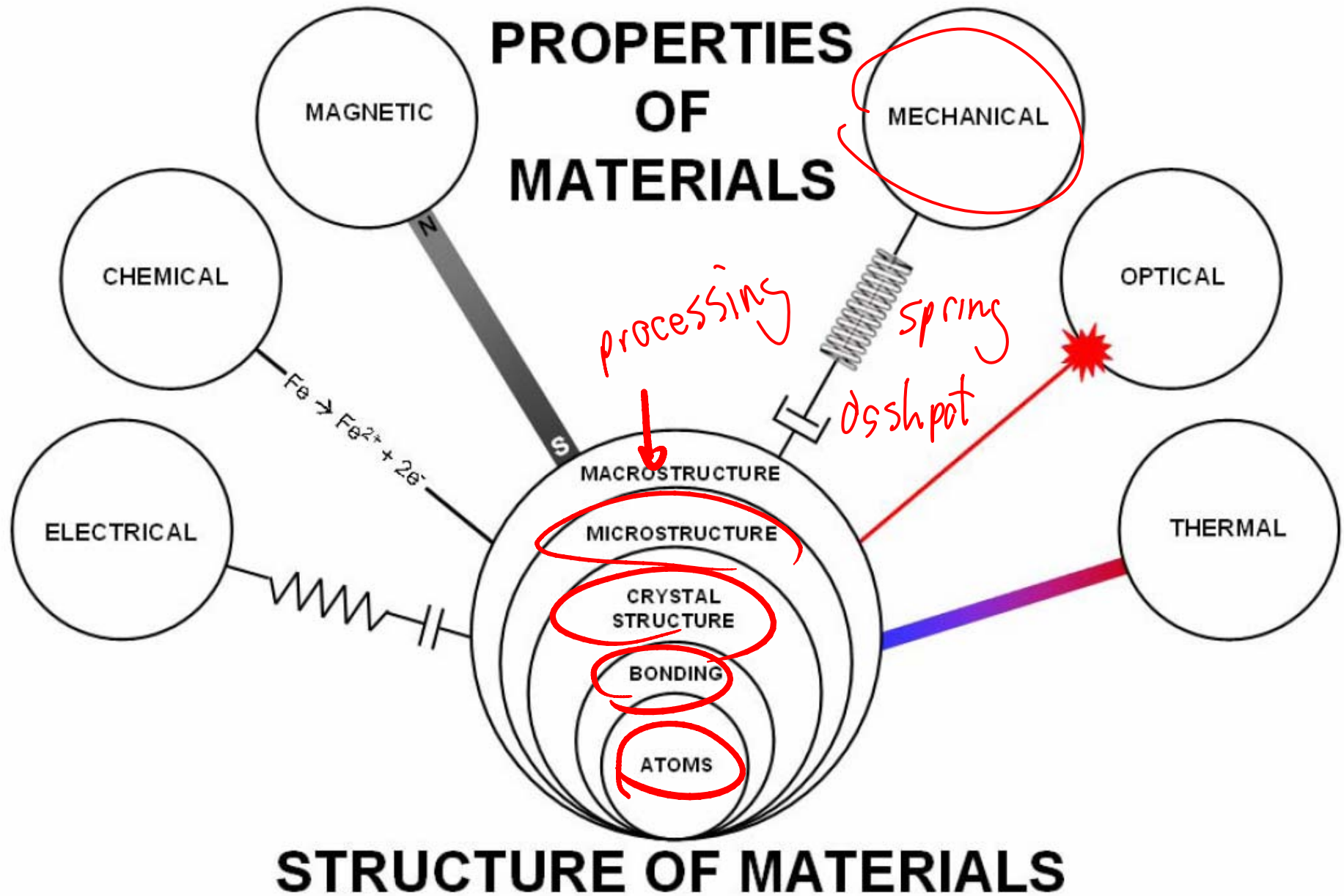


# Announcements

- **Mid-term grades should be up on WebCT tomorrow.**
  - **THANK YOU** for your work in taking the exam.
  - **PLEASE** be patient!
  - The actual content of the exam will be reviewed in the tutorials this week.
- **WE WILL DO A NEEDS ASSESSMENT (survey) once the grades are out.**
- **Welcome to the second half of the course.**
  - **Moving along to PROPERTIES**
  - **What was the first half?**



## Materials

*→ "non destructively" test them*

- **Handle these materials**
- **Find adjectives to describe how the respond mechanically**

TOUGH

## Adjectives

ELASTIC

HARD / SOFT

BRITTLE

STIFF

RIGID

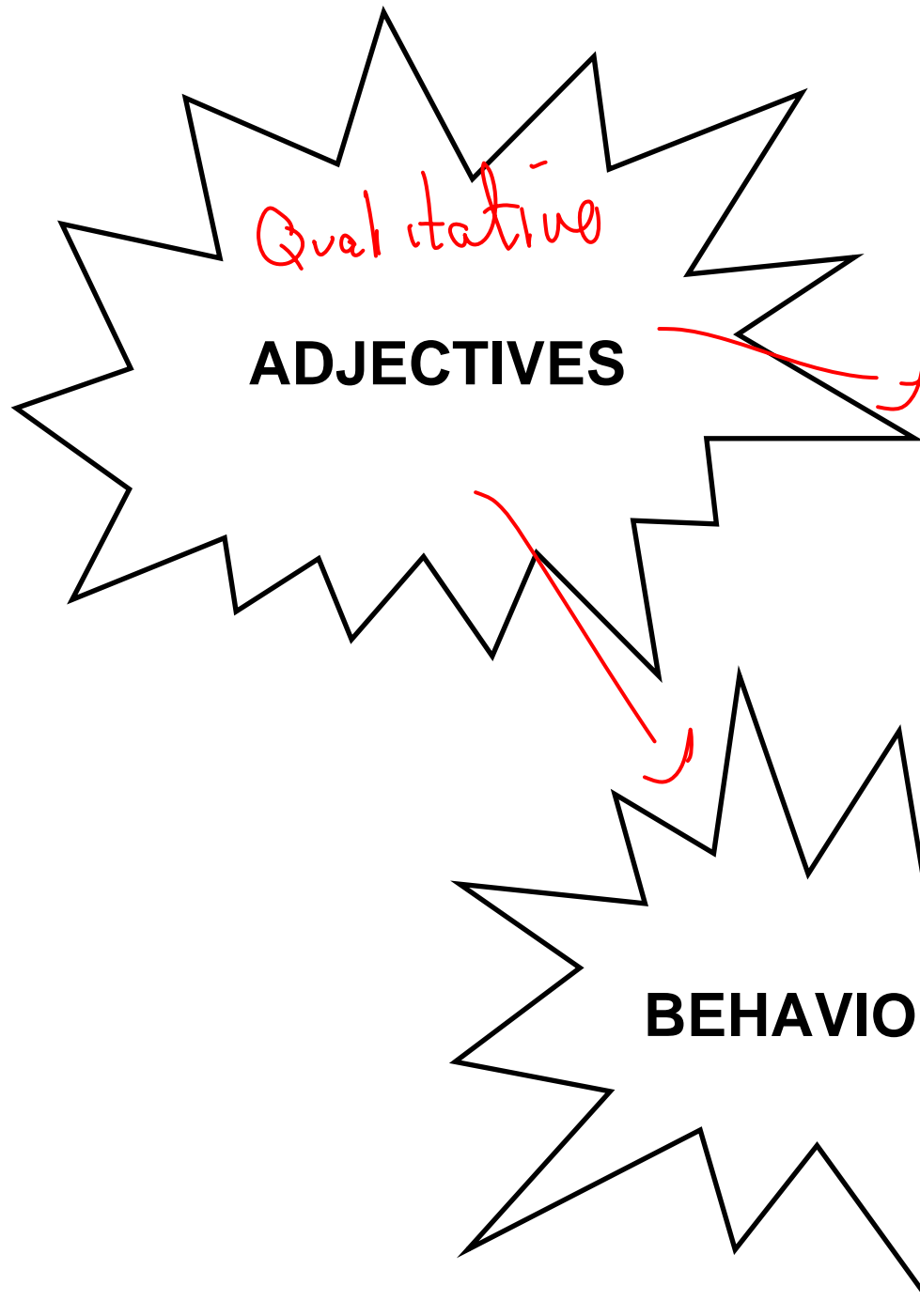
STRONG

DEFORMABLE

BOUNCY

SHINY

LIGHT



# Chapter 6:

## Mechanical Properties

### ISSUES TO ADDRESS...

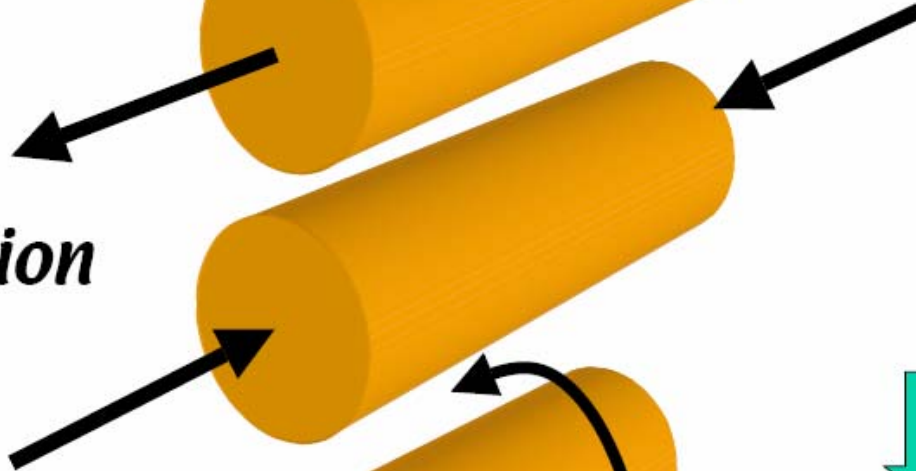
- **Stress** and **strain**: What are they and why are they used instead of load and deformation?
- **Elastic** behavior: When loads are small, how much deformation occurs? What materials deform least?
- **Plastic** behavior: At what point does permanent deformation occur? What materials are most resistant to permanent deformation?
- **Toughness** and **ductility**: What are they and how do we measure them?

## *Types of loads and deformations*

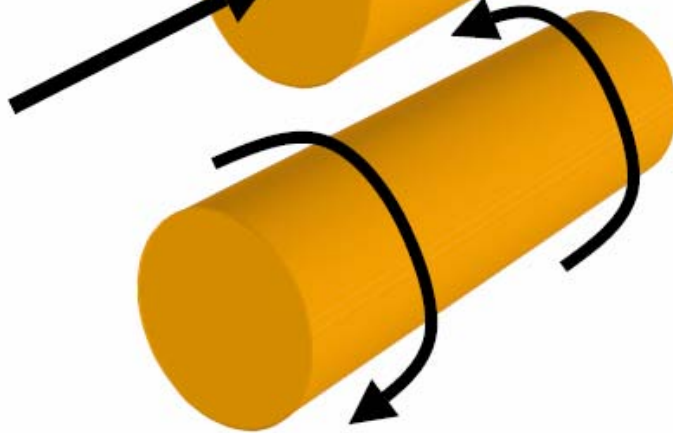
*Tension*



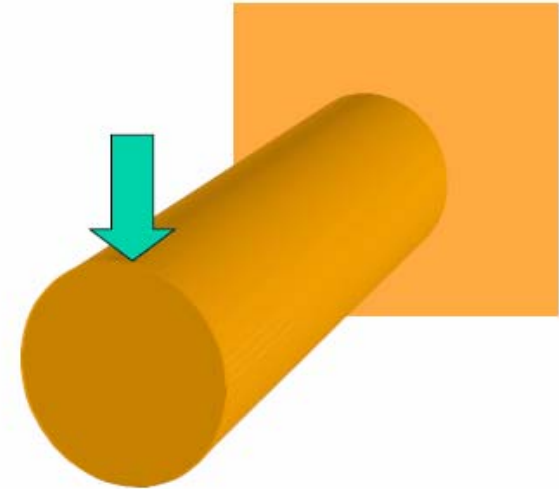
*Compression*



*Torsion*

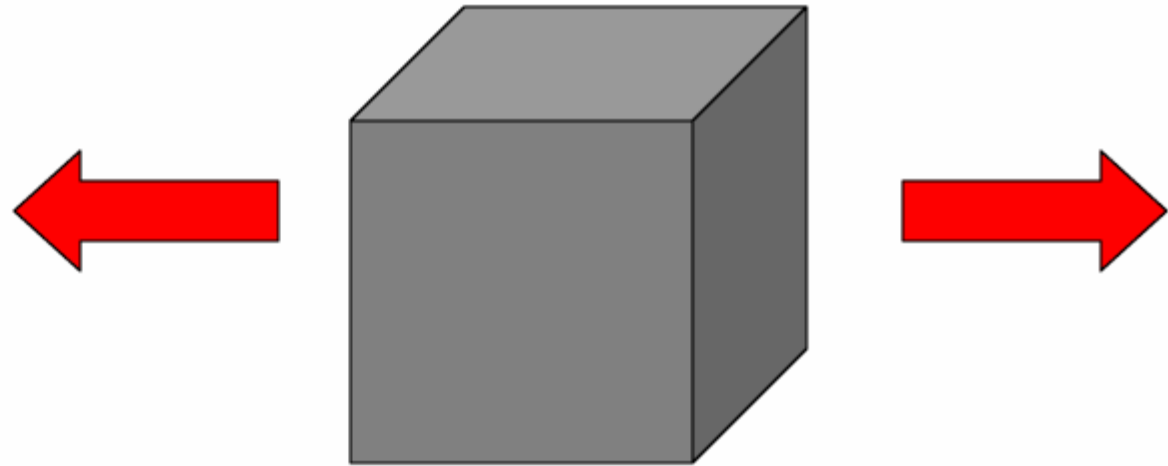


*Bending*



## **EXTREME example**

### **Tensile loading of iron**





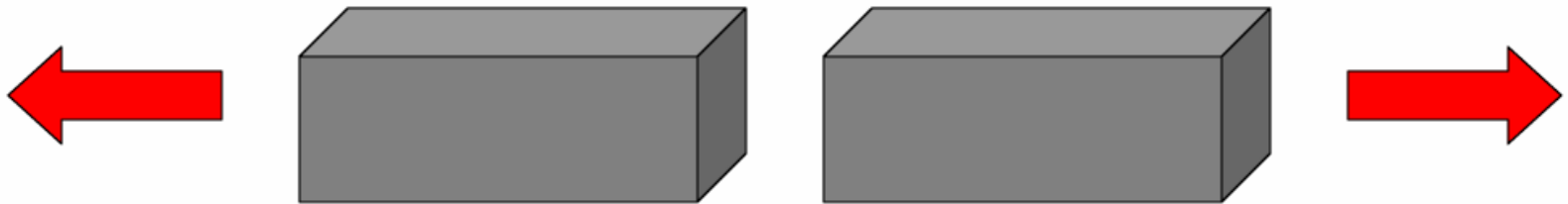
# EXTREME example

Tensile loading of iron

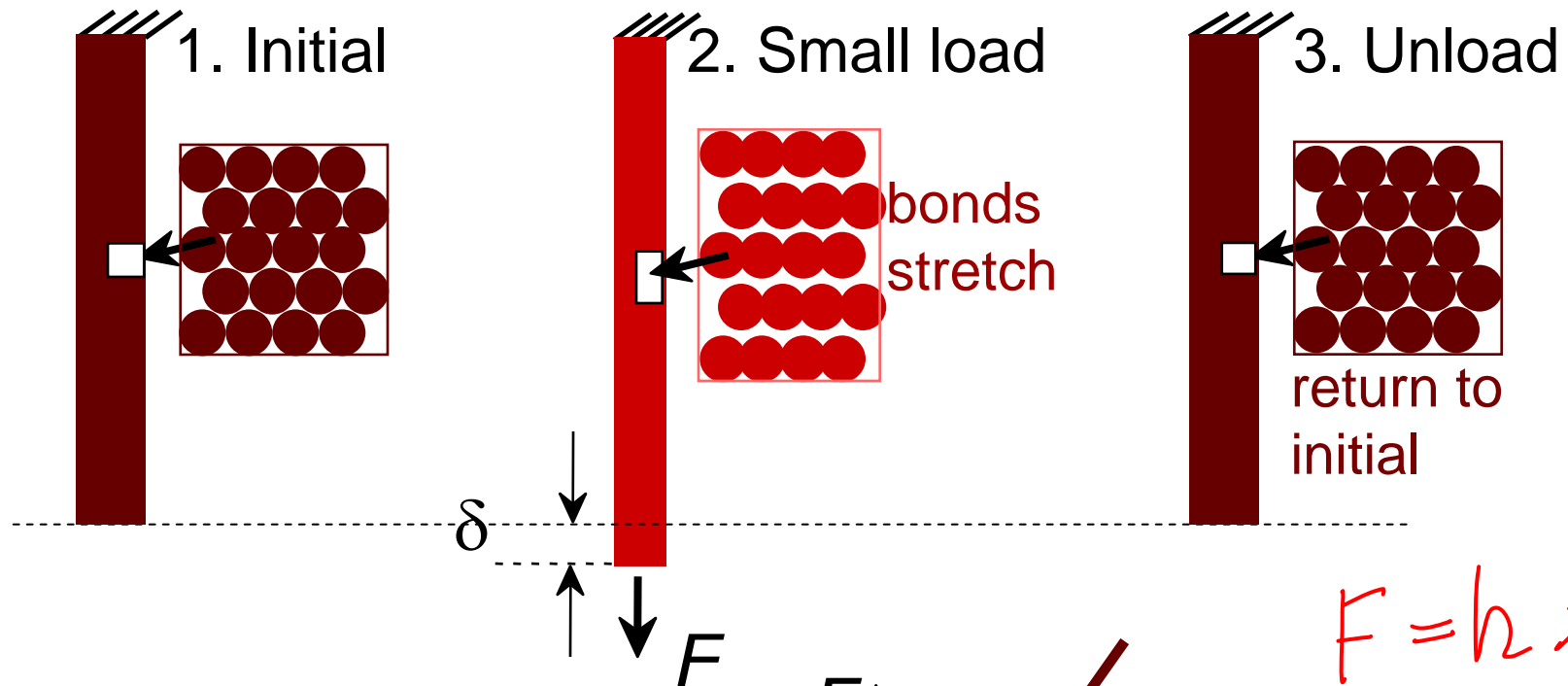


# EXTREME example

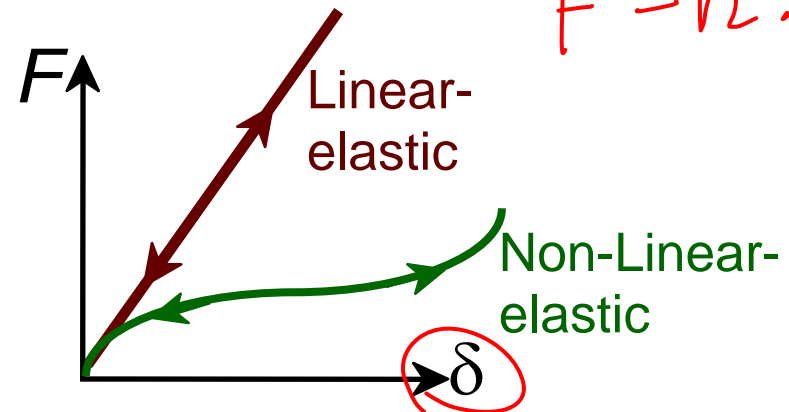
Tensile loading of iron



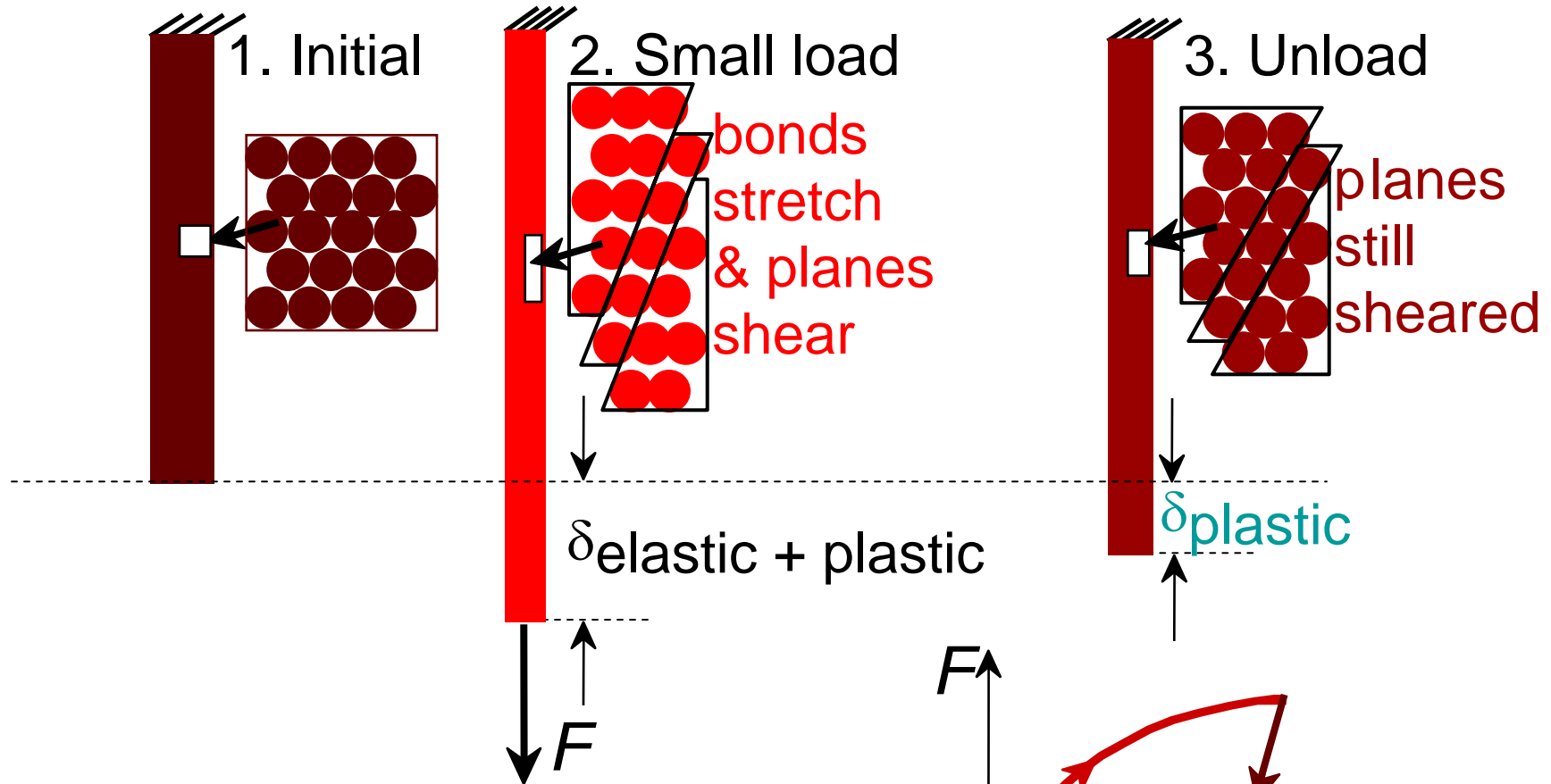
# Elastic Deformation



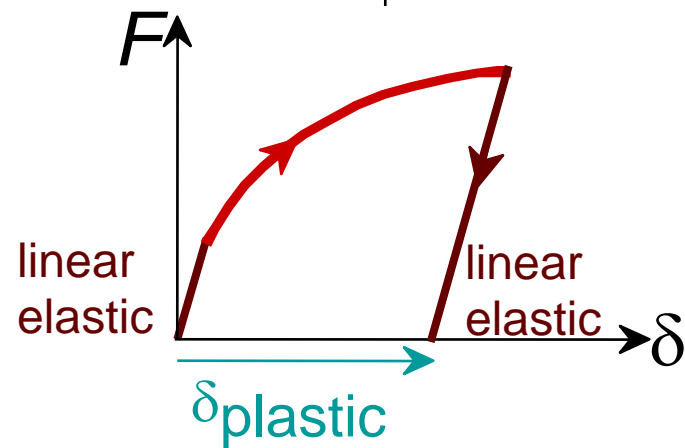
Elastic means **reversible**!



# Plastic Deformation (Metals)

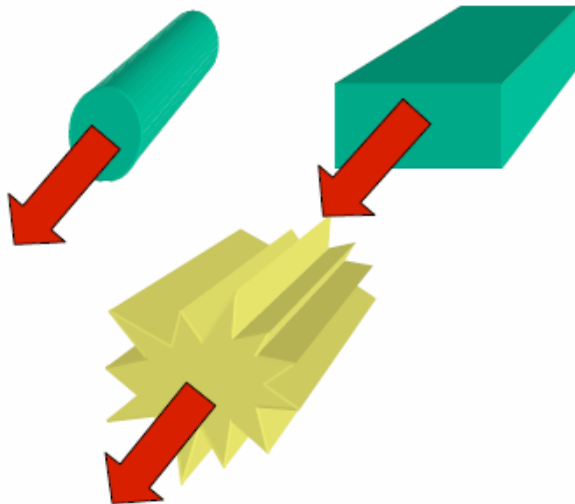
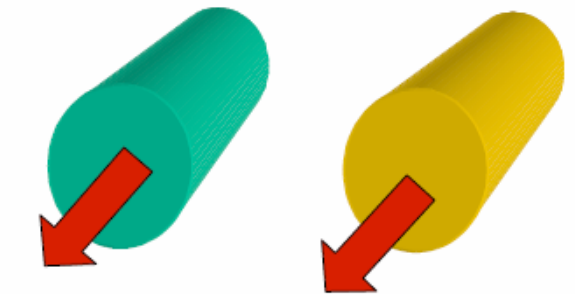


Plastic means **permanent**!



## Material vs. structural properties

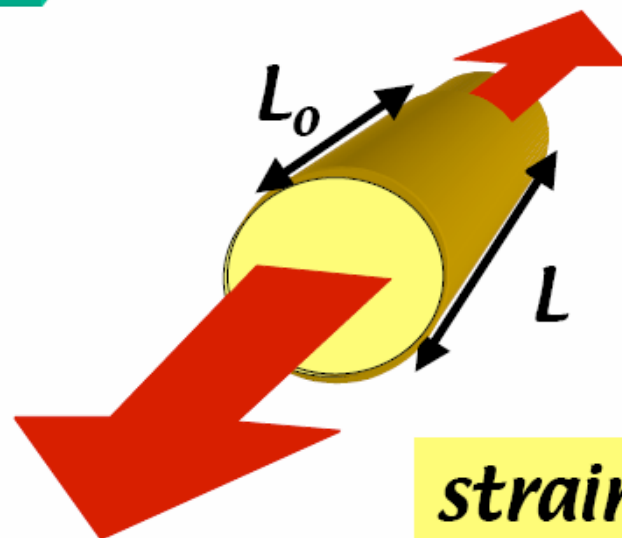
*Need to eliminate the effect of size and shape to define material properties.*



*stress ( $\sigma$ ) = Force/Area*

$$\sigma = F/A$$

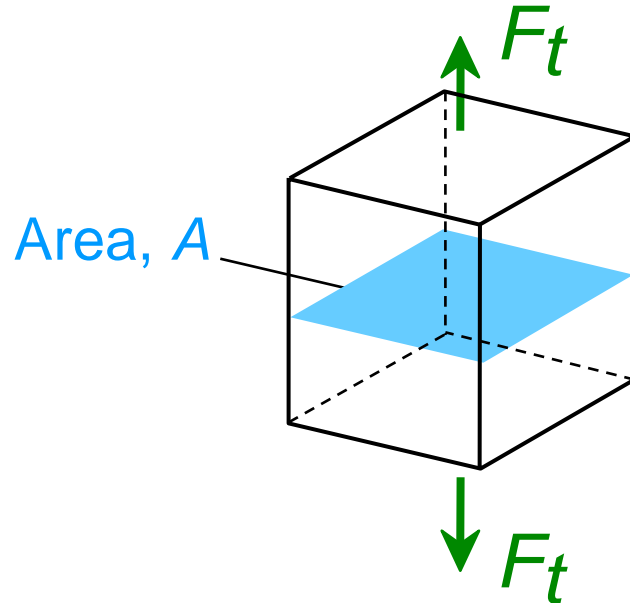
$$\text{Pa} = \text{N/m}^2$$



$$\text{strain } (\epsilon) = (L - L_0)/L_0$$

# Engineering Stress

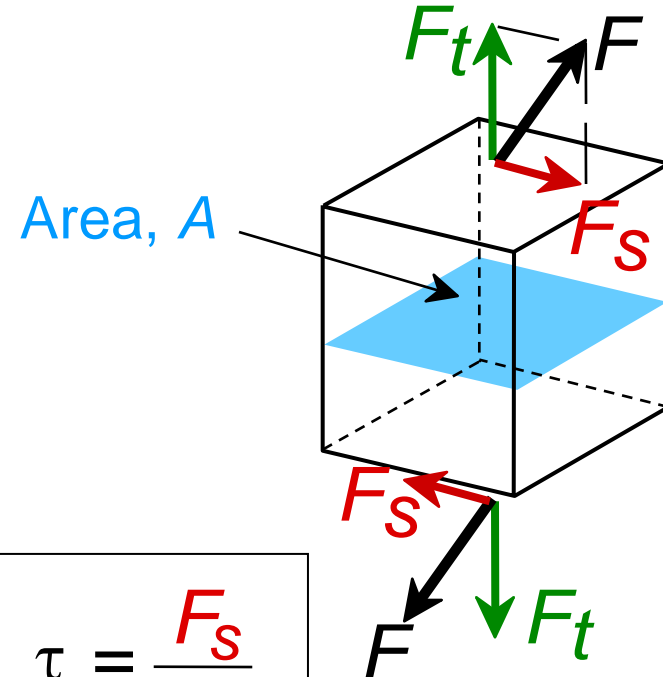
- Tensile stress,  $\sigma$ :



$$\sigma = \frac{F_t}{A_o} = \frac{\text{lb}_f}{\text{in}^2} \text{ or } \frac{\text{N}}{\text{m}^2}$$

original area  
before loading

- Shear stress,  $\tau$ :



$$\tau = \frac{F_s}{A_o}$$

$\therefore$  Stress has units:  
 $\text{N/m}^2$  or  $\text{lb}_f/\text{in}^2$

# Common States of Stress

- **Simple tension:** cable

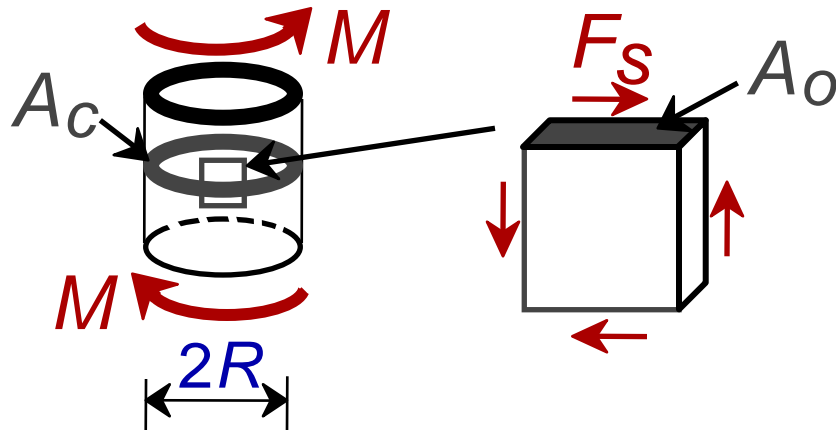


$A_0$  = cross sectional area (when unloaded)

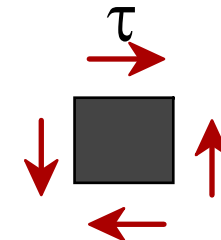
$$\sigma = \frac{F}{A_0}$$



- **Torsion** (a form of shear): drive shaft



$$\tau = \frac{F_s}{A_0}$$

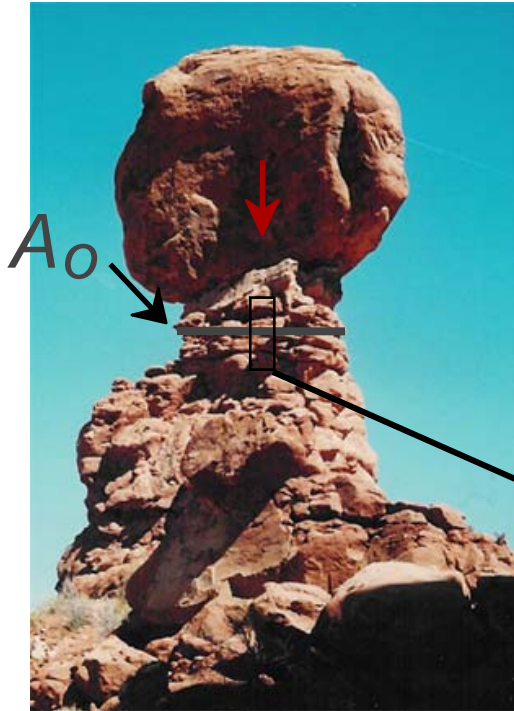


Note:  $\tau = M/A_c R$  here.

Ski lift (photo courtesy P.M. Anderson)

# OTHER COMMON STRESS STATES (1)

- **Simple** compression:



Balanced Rock, Arches  
National Park  
(photo courtesy P.M. Anderson)



Canyon Bridge, Los Alamos, NM  
(photo courtesy P.M. Anderson)

$$\sigma = \frac{F}{A_o}$$



Note: compressive  
structure member  
( $\sigma < 0$  here).

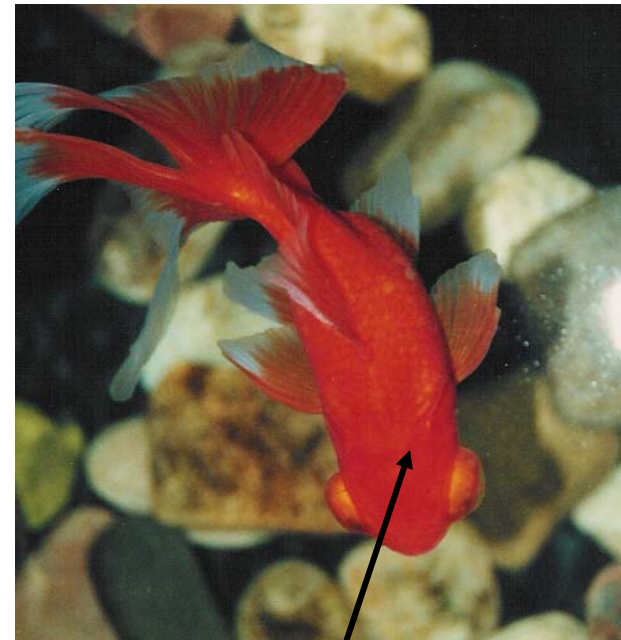
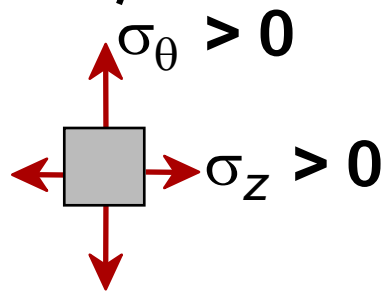


## OTHER COMMON STRESS STATES (2)

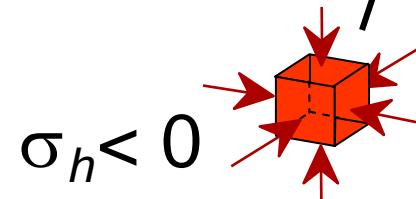
- **Bi-axial** tension:
- **Hydrostatic** compression:



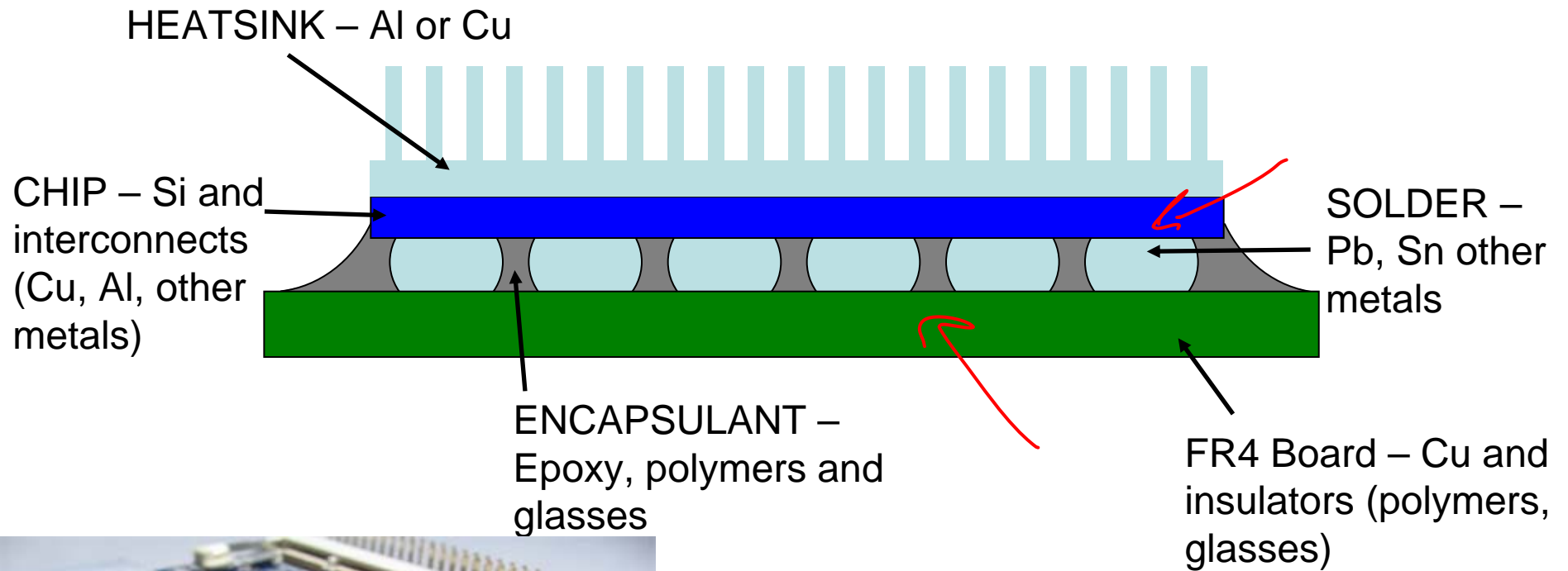
Pressurized tank  
(photo courtesy  
P.M. Anderson)



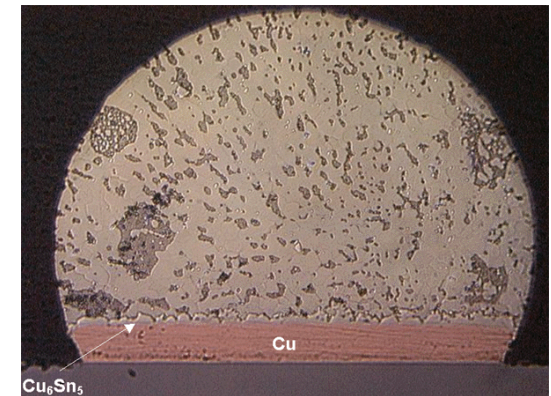
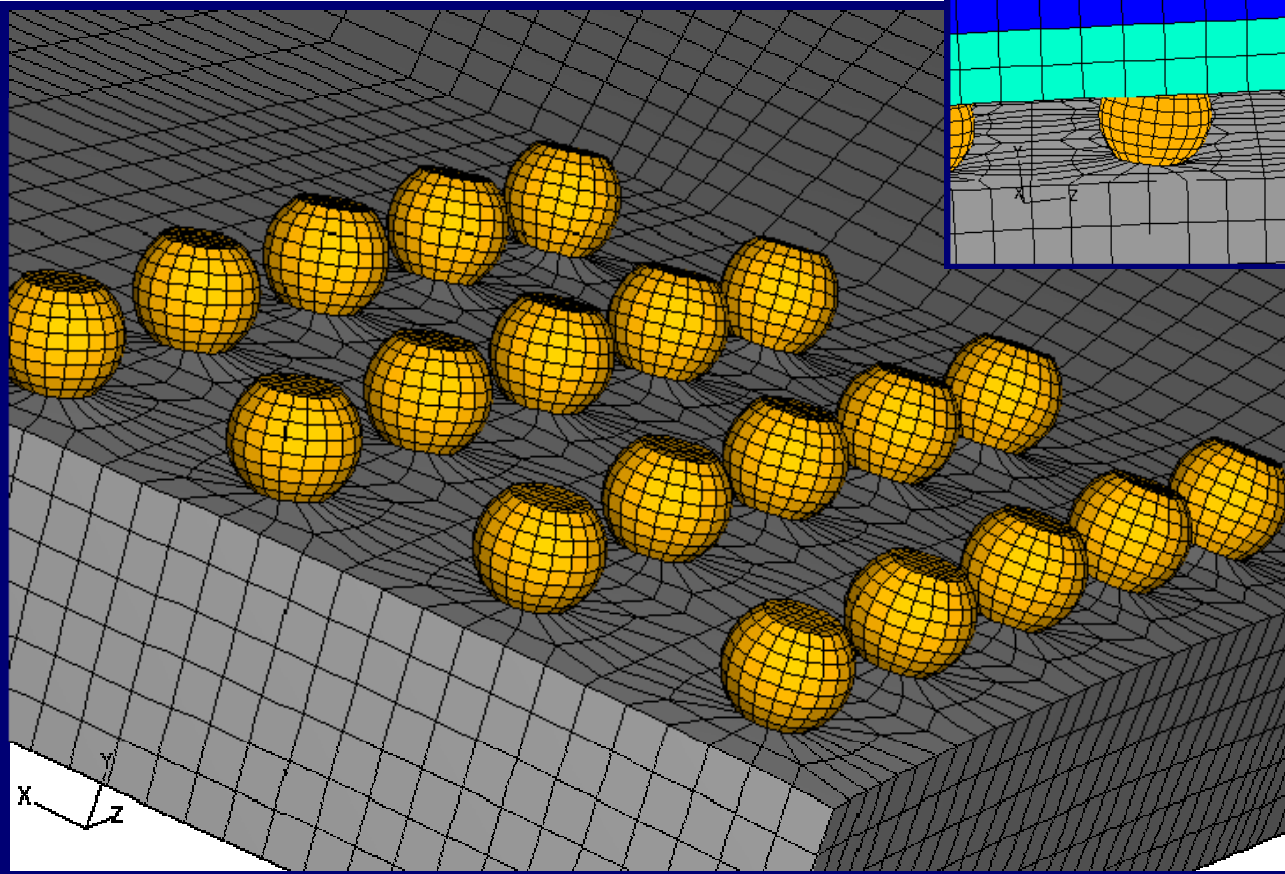
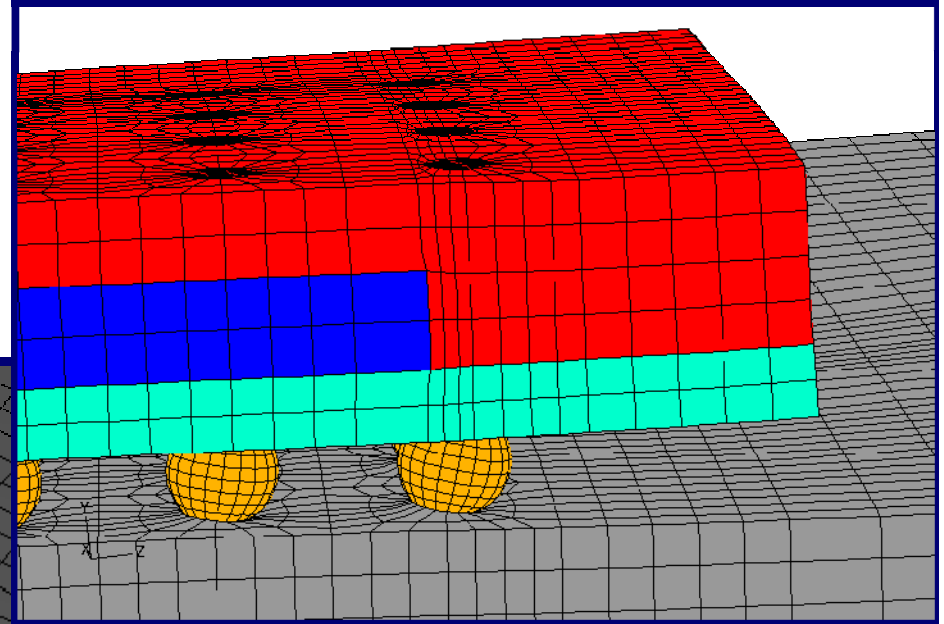
Fish under water  
(photo courtesy  
P.M. Anderson)



# FLIP CHIP BALL GRID ARRAY



# Reliability Modeling Pb-Sn Solders



H. Nied and M. Ozturk  
Mechanical Engineering

Lehigh Univ.

# Engineering Strain

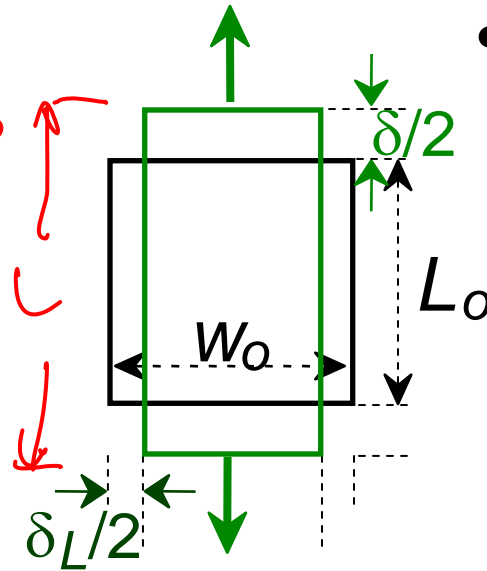
- **Tensile strain:**

$$\epsilon = \frac{\delta}{L_o}$$

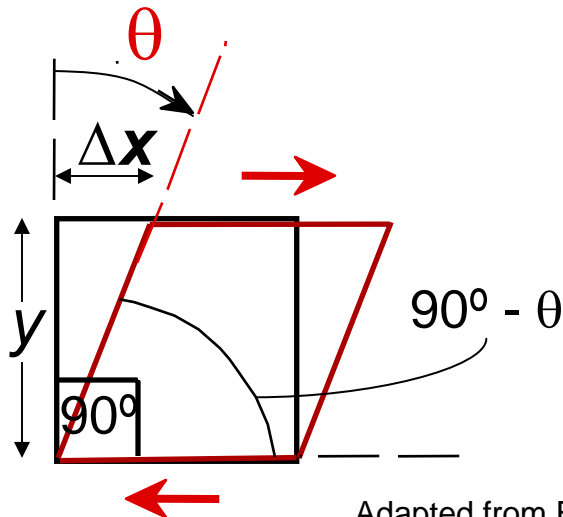
*Handwritten notes:*  $L - L_o$  (with an arrow pointing to the change in length),  $\delta$  (with an arrow pointing to the change in length), and "strain" (with an arrow pointing to the equation).

- **Lateral strain:**

$$\epsilon_L = \frac{-\delta_L}{W_o}$$



- **Shear strain:**



$$\gamma = \Delta x / y = \tan \theta$$

**Strain is always dimensionless.**

Adapted from Fig. 6.1 (a) and (c), Callister 7e.

# Material vs. structural properties

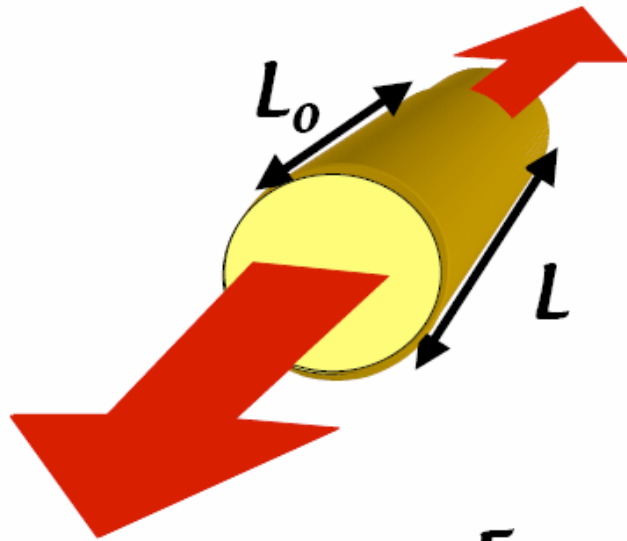
**stress ( $\sigma$ ) = Force/Area**

$$\sigma = F/A$$

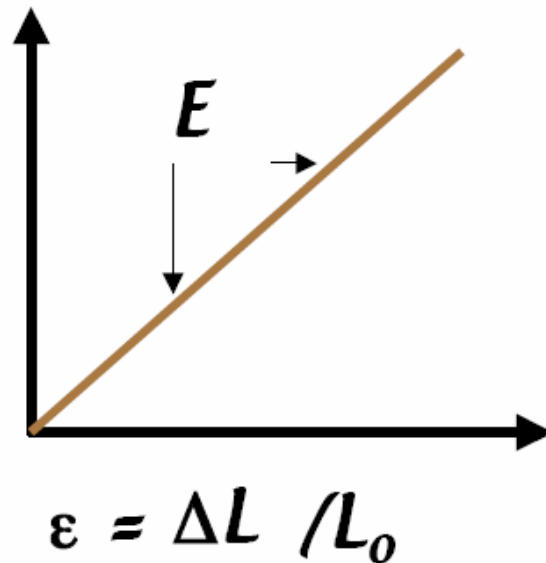
**strain ( $\epsilon$ ) =  $(L - L_0)/L_0$**

$$\epsilon_T = \int dL/L = \ln(L)$$

$$\lambda = L/L_0$$



$$\sigma = \frac{\text{Force}}{\text{Area}}$$



**Hooke's Law**  
 $F = k \Delta L$

**Young's modulus ( $E$ ) measures the stiffness of a material**

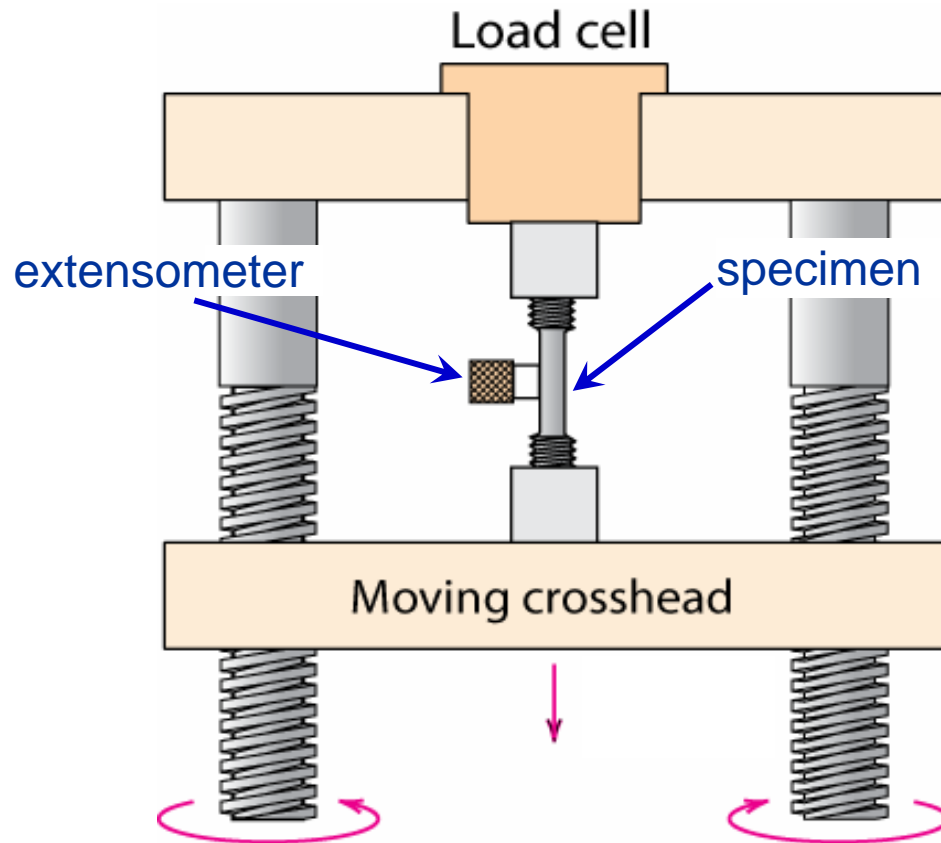
$$E = \sigma / \epsilon$$

$$\sigma = E \epsilon$$



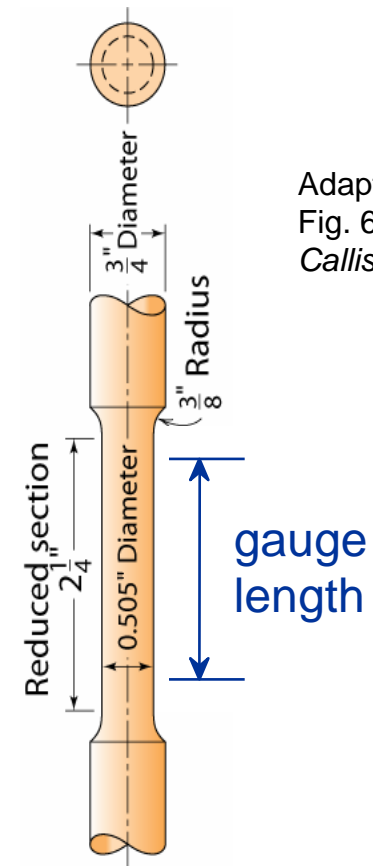
# Stress-Strain Testing

- Typical tensile test machine

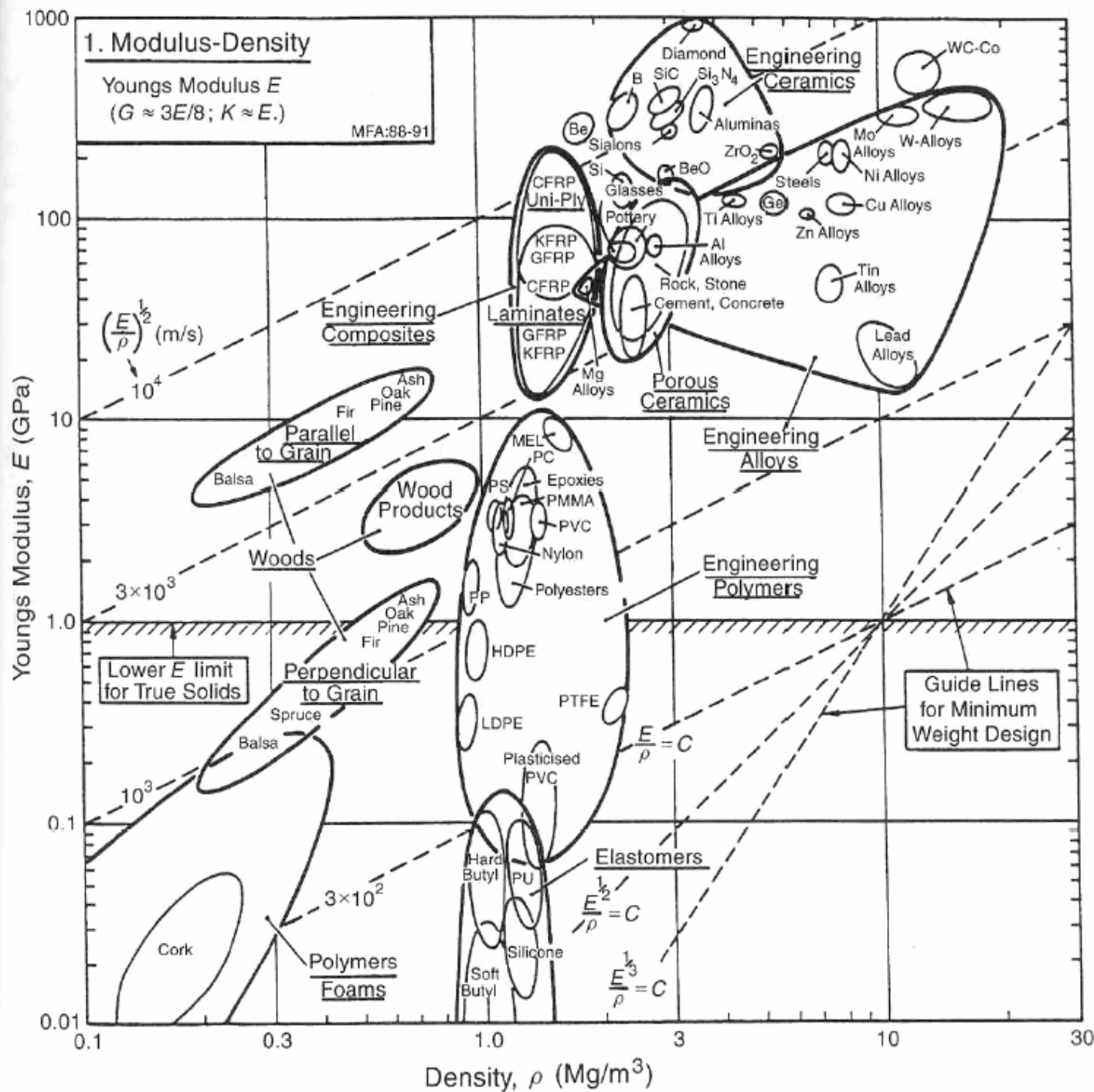


Adapted from Fig. 6.3, *Callister 7e*. (Fig. 6.3 is taken from H.W. Hayden, W.G. Moffatt, and J. Wulff, *The Structure and Properties of Materials*, Vol. III, *Mechanical Behavior*, p. 2, John Wiley and Sons, New York, 1965.)

- Typical tensile specimen

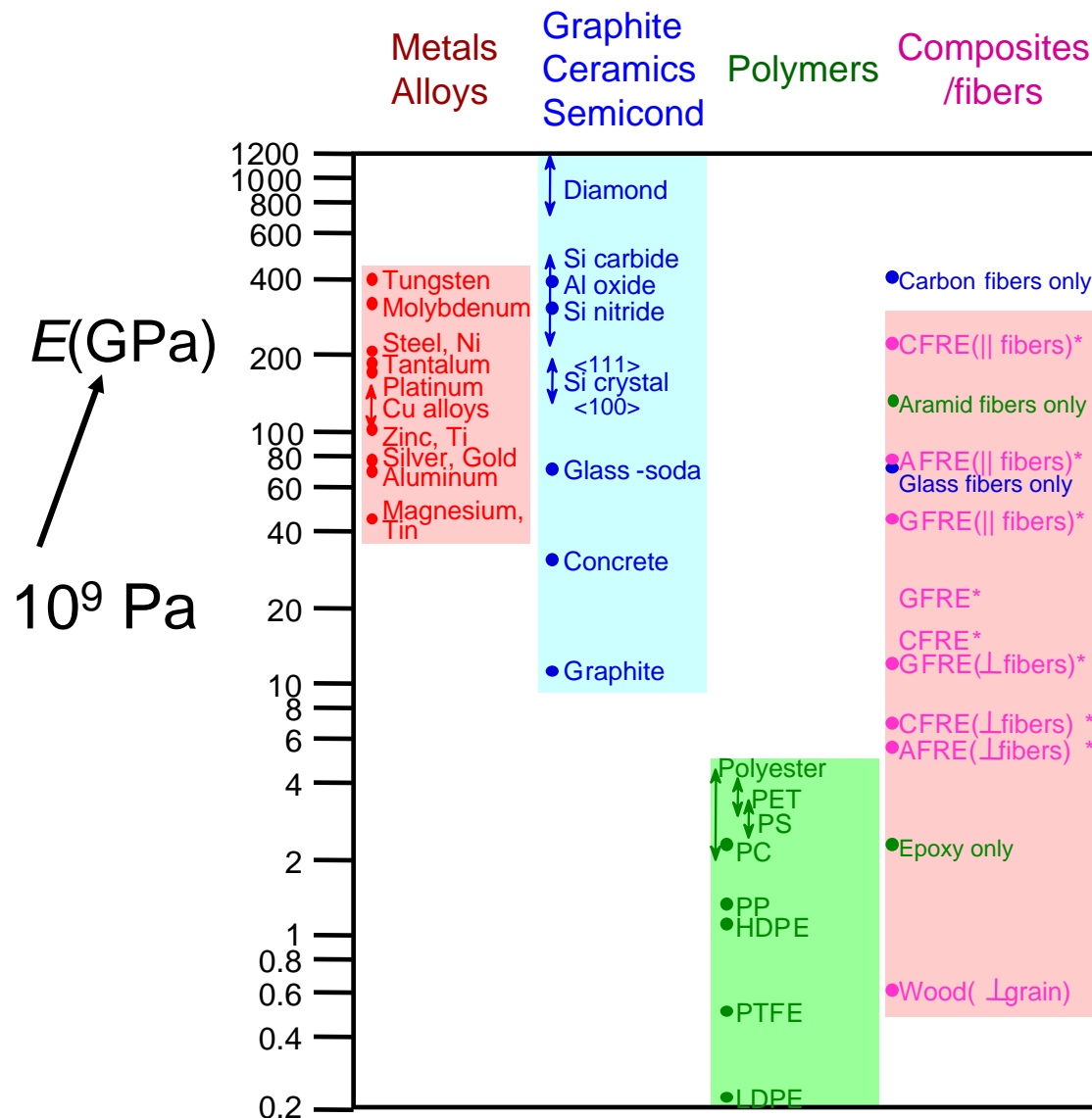


Adapted from  
Fig. 6.2,  
*Callister 7e*.



Ashby Plot

# Young's Moduli: Comparison



Based on data in Table B2,  
*Callister 7e.*

Composite data based on  
reinforced epoxy with 60 vol%  
of aligned  
carbon (CFRE),  
aramid (AFRE), or  
glass (GFRE)  
fibers.

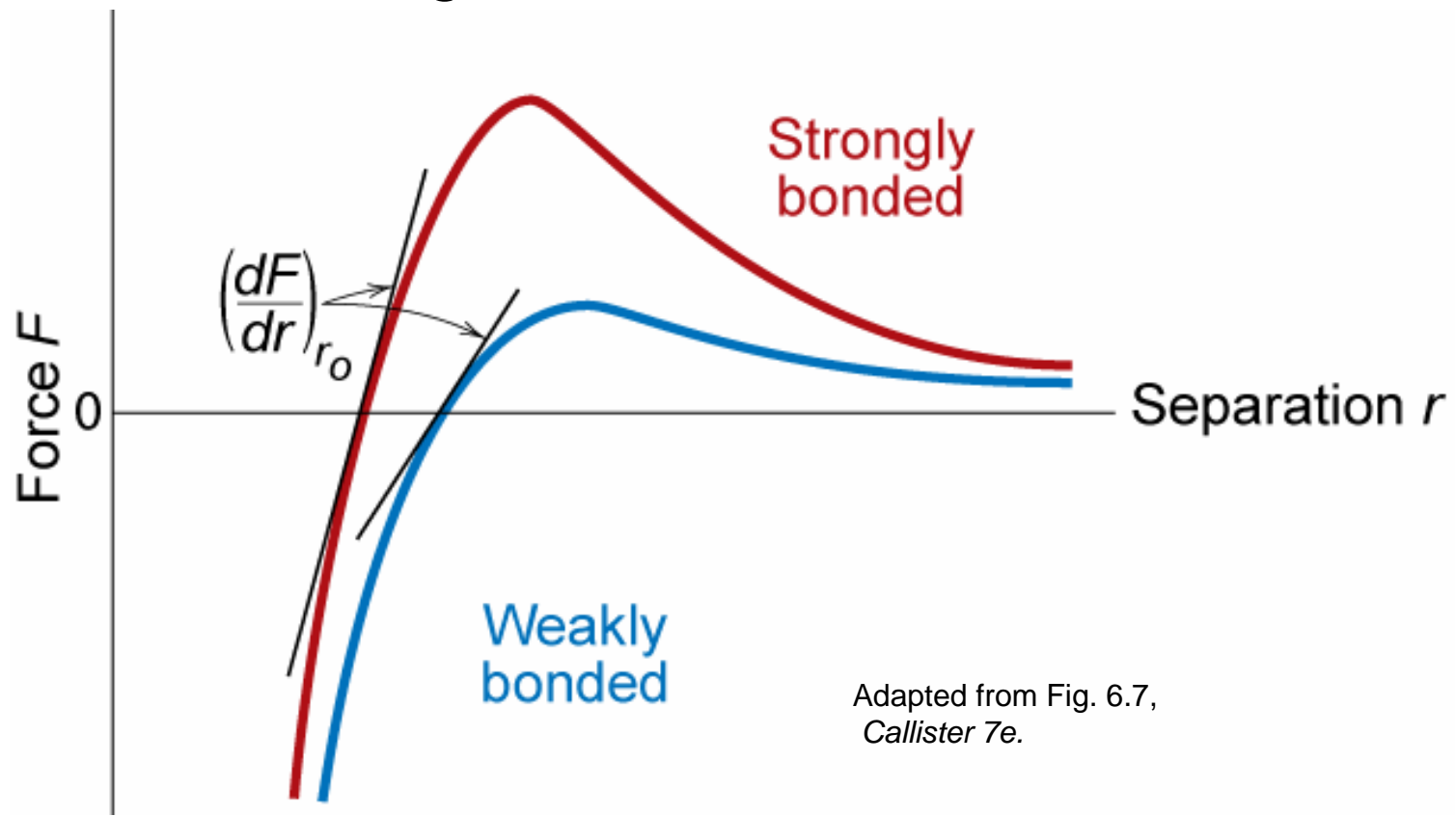


## Useful reference values

<b>Diamond</b>	<b>700-1200 GPa</b>
<b>Carbon fibre</b>	<b>230-400 GPa</b>
<b>Steel</b>	<b>200 GPa</b>
<b>Aluminium</b>	<b>70 GPa</b>
<b>Glass</b>	<b>70 GPa</b>
<b>Polyethylene</b>	<b>0.1-1 GPa</b>

# Mechanical Properties

- Slope of stress strain plot (which is proportional to the elastic modulus) depends on bond strength of metal



# Poisson's ratio, $\nu$ Auxetic

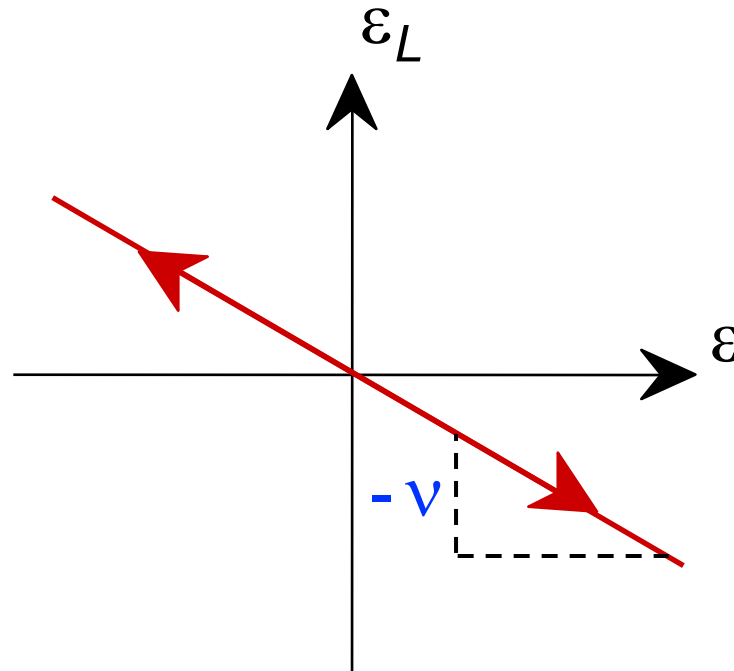
- Poisson's ratio,  $\nu$ :

$$\nu = -\frac{\epsilon_L}{\epsilon} \text{ lateral}$$

metals:  $\nu \sim 0.33$

ceramics:  $\nu \sim 0.25$

polymers:  $\nu \sim 0.40$



Units:

$E$ : [GPa] or [psi]

$\nu$ : dimensionless

$-\nu > 0.50$  density increases

$-\nu < 0.50$  density decreases  
(voids form)

## **Next time**

- **More about what actually happens in the material**
- **Strengthening (Ch. 7)**
- **More on behavior for specific materials**
- **Failure (Ch. 8)**
  - **Fracture**
  - **Creep**
  - **Fatigue**