

# Announcements

- Tutorials
  - Group A (Prof. Chromik)
  - Group B (Mr. Arya Fatehi)
  - Group C (Mr. Andreas Klintner)
- Office hours (Wong 2100)
  - Tuesdays 1:30 – 3:00 PM or by appt.
  - Open door policy
- WebCT quiz to appear by tomorrow AM, due Friday by 5 PM.
- Additional Ch. 3 problems to be assigned via WebCT (check tomorrow or Friday)

# What will the quiz be on?

Lecture (DD/MM/YY)	Lecture Topic	Readings	Assignments
03-01-07	Course description, Atoms, Periodic Table, Electronic Structure	1.1-1.6, 2.1-2.4	
08-01-07	Bonding and Crystal Structure	2.5-2.8, 3.1-3.7	
10-01-07	Crystal Structure and Defects	3.8-3.17, 4.1-4.11	WebCT Quiz Due 12-01-07
15-01-07	Diffusion	5.1-5.6	
17-01-07	Materials Fabrication and Microstructure	11.3-11.6	Tutorial Quizzes
22-01-07	Phase Diagrams and Microstructure I	9.1-9.19	
24-01-07	Phase Diagrams and Microstructure II	9.1-9.19	WebCT Quiz Due 26-01-07

# Bonding SUMMARY (from last time)

- Types of bonding
  - ‘Strong’ bonds: covalent, ionic and metallic
  - ‘Weak’ bonds: van der Waals and dipole (hydrogen)
- Which bond type depends on what is bonding (e.g. groups of atoms find most stable electron configuration)

**WHY?**

Minimisation of energy!

# BONDING AND ENERGY

Potential  
energy

repel

attract

$E_0$

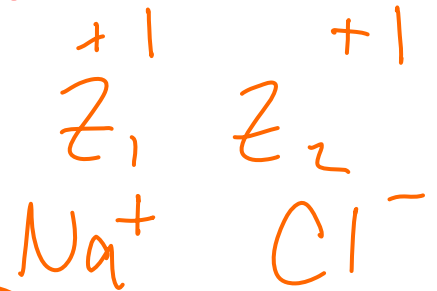
x or r

$$E_R = B/r^n$$

Callister 2.9

i.e. at equilibrium atomic separation

energy lowest



$$E_A = -A/r$$

Callister 2.8

This graph can be used to conceptualize any type of bond.

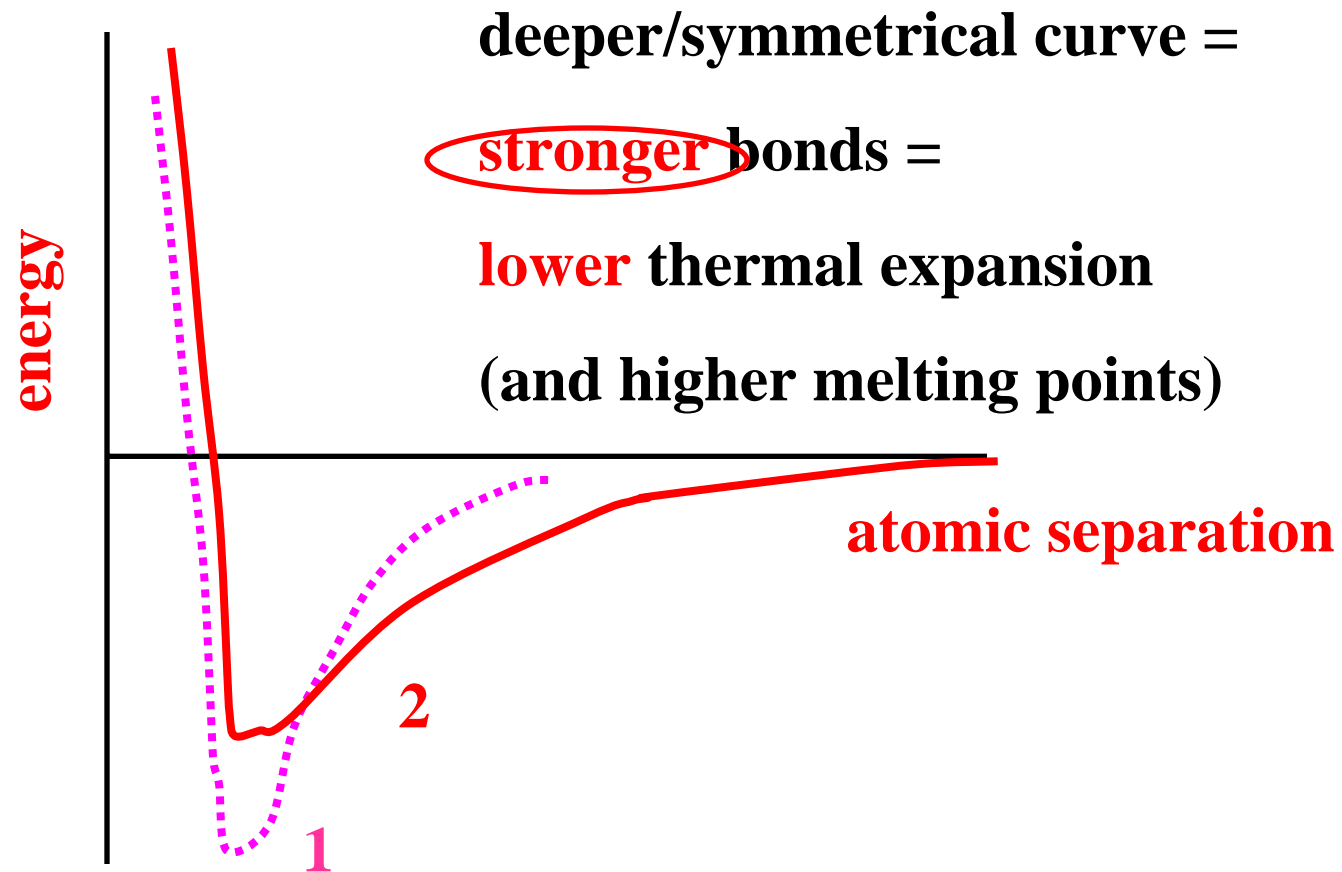
However, the functional form of  $E_A$  and  $E_R$  would differ based on bond type – changing the shape of this curve.

## Homework 2.15

Note: 2.14 being worked out in tutorials

$$E_A(r) = \frac{-|Z_1 Z_2| q^2}{4\pi\epsilon_0 r}$$

# RELATION BETWEEN ATOMIC BONDING AND THERMAL EXPANSION



Material 1 has stronger bonds, less thermal expansion and higher melting point than material 2.

# Bond Energies

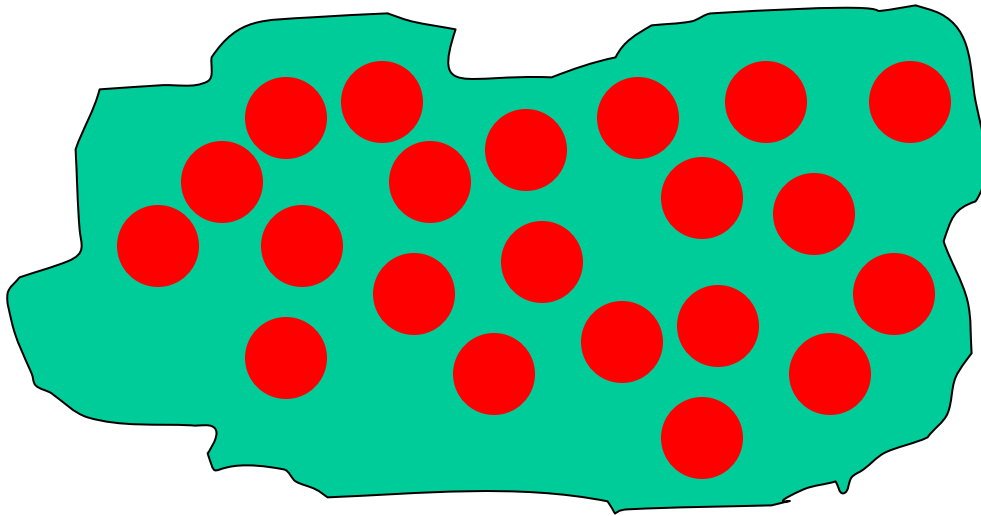
<i>Bonding Type</i>	<i>Substance</i>	<i>Bonding Energy</i>		<i>Melting Temperature (°C)</i>
		<i>kJ/mol</i>	<i>eV/Atom, Ion, Molecule</i>	
Ionic	NaCl	640	3.3	801
	MgO	1000	5.2	2800
Covalent	Si	450	4.7	1410
	C (diamond)	713	7.4	>3550
Metallic	Hg	68	0.7	-39
	Al	324	3.4	660
	Fe	406	4.2	1538
	W	849	8.8	3410
van der Waals	Ar	7.7	0.08	-189
	Cl <sub>2</sub>	31	0.32	-101
Hydrogen	NH <sub>3</sub>	35	0.36	-78
	H <sub>2</sub> O	51	0.52	0

**Ionic bonds are generally the strongest. But, as you can see here, the bond energy varies: (1) from type-to-type, (2) within each bond type.**

## Metallic bonds

All **valence** electrons **freed** up to form electron 'cloud'

All atoms share all electrons in cloud ← Someone asked,  
each atom reaches lower energy state "How can this be  
TRUE?"



Cloud attracts metal  
ions (ion 'cores')

Non-directional forces, therefore close packed

Forces can be weak or strong  
(melting points vary by 1000s of degrees)

# The metallic bond

- Consider sodium, Na ( $1s^2 2s^2 2p^6 3s^1$ )
  - Ionic bond?  $(Na^+)_7 Na^{7-}$
  - Covalent bond? Two Na share their  $3s^1$  electrons.
  - Start adding more Na and continue sharing...
    - Eventually, the electrons 'delocalize' and are shared (*unequally*) with all of the Na ions

**Insulator → metal transition**

**or sometimes**

**Insulator → metal catastrophe!**



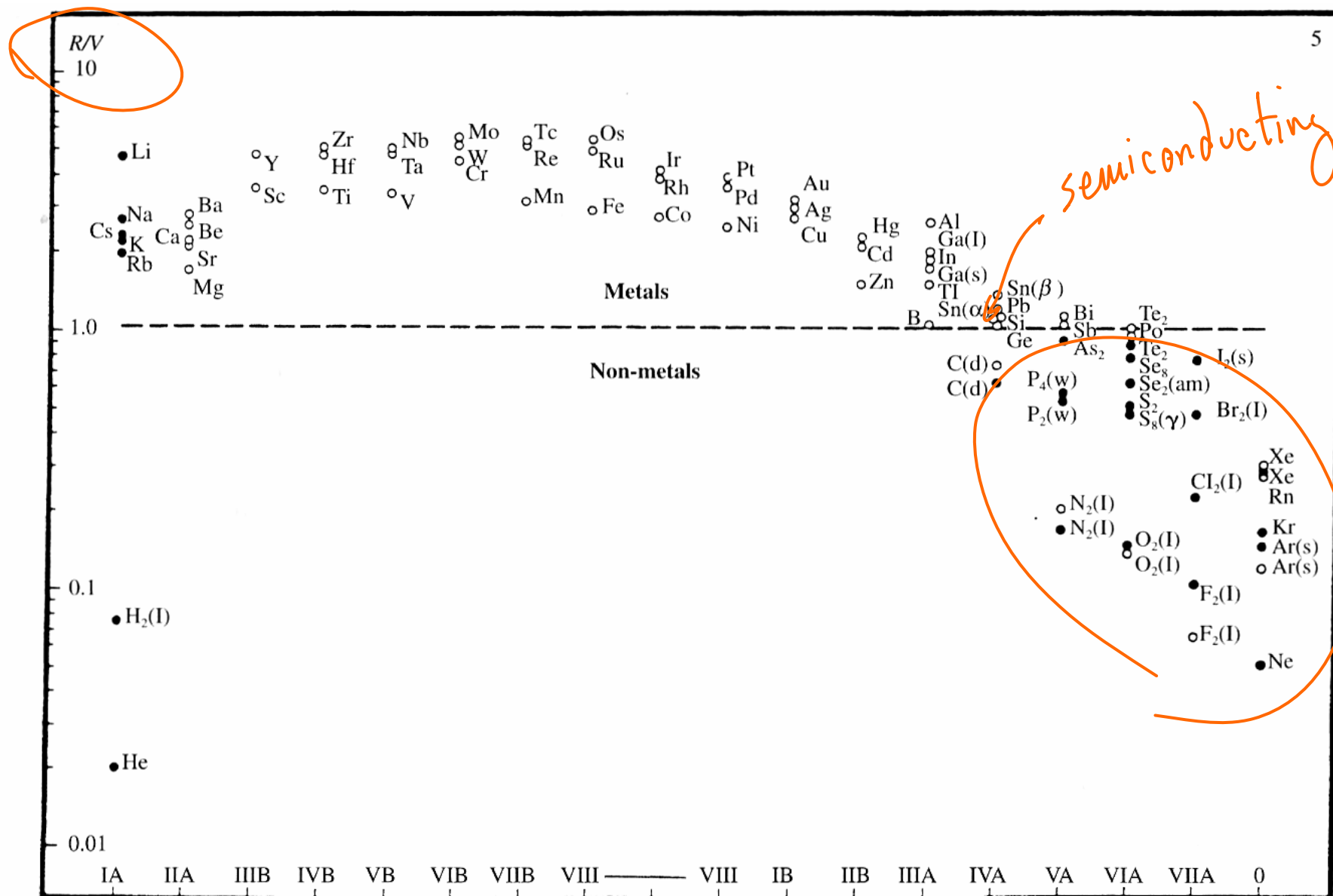
# One way to consider why this happens

- Polarizability
  - Many insulators may be polarized in an electric field. This creates tiny dipole moments that enhance the total field.
  - In a metal, the first step is polarization, but the valence electrons are weakly bound. They escape into the ‘electron cloud.’
- Metal vs. Insulator
  - Dependence on polarizability has been epitomized by the ratio of

$$\frac{R}{V}$$

Molar refractivity (optical property that is tied strongly to polarizability)

Molar volume



**fig. 1.13** The ratio  $R/V$  (see text) predicts very successfully which elements are metals and which are not. The filled circles are for elements which  $R$  and  $V$  are both known. The open circles are for elements for which  $R$  has had to be calculated. (Taken from P.P. Edwards and A.J. Sienko (1982). *Acc. Chem. Res.* **15**, 87.)

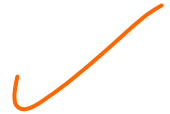
## This says...

- Everything would be a metal if it were dense enough (i.e. its molar volume were small.)

$$\frac{R}{V}$$

## This predicts...

- The hydrogen at the center of Jupiter is metallic.



# Summary

- Yes, there is really an electron cloud (more accurately called a conduction band).
- A metal atom 'loses' electrons from the unfilled shells to the conduction band
  - K  $1s^2 2s^2 2p^6 3s^2 3p^6 (4s^1)$  K loses one electron and becomes like Ar
  - Mg  $1s^2 2s^2 2p^6 (3s^2)$  Mg loses two electrons to the conduction band *Ne*
  - Cu  $1s^2 2s^2 2p^6 3s^2 3p^6 (3d^{10} 4s^1)$ 
    - Lose 11 electrons to become like Ar?
    - Lose the  $4s^1$  electron?

# ANIMATION

- Auburn website listed on WebCT

**But now, moving on to crystal structure**

# ATOMIC PACKING

## Fundamental Concepts

- Bonding can lead to very big molecules

- The atoms can be arranged either;

- randomly** (**amorphous** (latin? without form) **structure**)

or,

*short range order*

- ordered** (**crystalline** structure)

i.e. repeating or periodic arrangement of atoms

over large distances

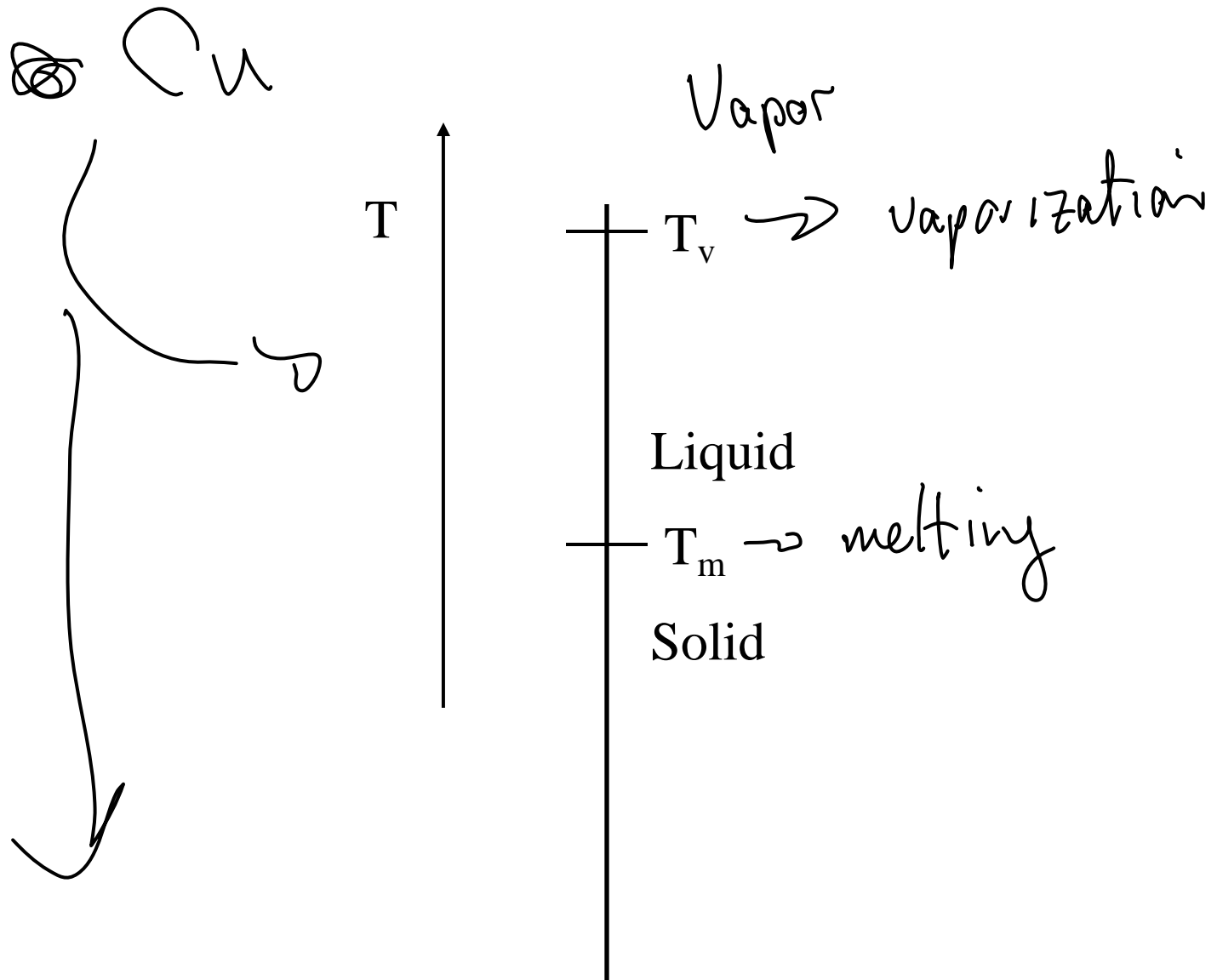
*long range order*

# Crystal structure?

- Liquid
  - No crystal structure
  - Shape defined by a containing vessel
- Solid
  - Most solids form in organized arrays of atoms
  - Shape defined by the thermal and mechanical history (i.e. how we made it!)



# Phase diagram for a pure metal?



An amorphous structure is favoured **when**

the 'bonding' takes place rapidly

**because:**

ordering takes more time\*

**BUT:**

Under normal (i.e. industrial) circumstances

**'simple' materials are crystalline,\***

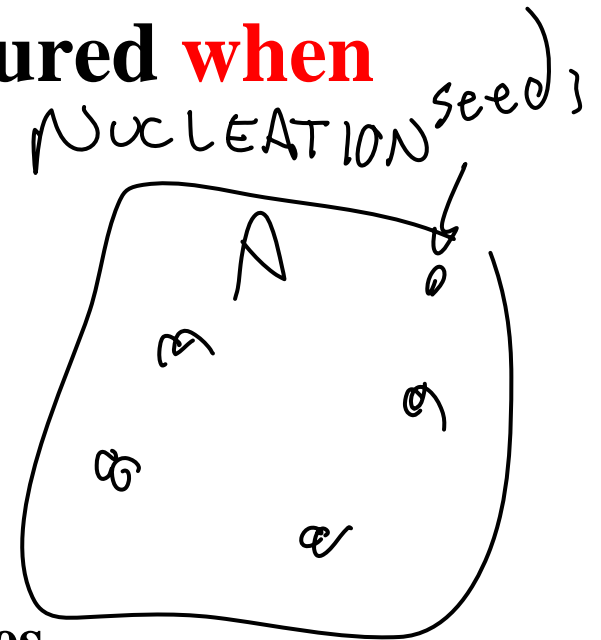
e.g. all metals or simple compounds (e.g. NaCl)

**'Complex' materials** (e.g. multi-element **compounds**)  $NiZr$

are likely to be **amorphous**,

or a mix of amorphous and crystalline **because**

there is more constraint on relative positions of atoms



# CRYSTAL STRUCTURES

(defines stacking of atoms)

Split the large number of atoms

(the **crystal** or the **lattice**)

into small, equal 3D groups of atoms (**unit cells**)

(parallelopipeds or prisms:

i.e. 3\* sets of parallel faces (or **planes**))

- groups must all have the same 3D pattern

Joining up all the unit cells **should** form the crystal

**-unit cells have the**

**'highest level of geometric symmetry'**

**and /or\***

**the smallest number of atoms**

**-key to using unit cells is geometry**

# METALLIC CRYSTAL STRUCTURES

**Simplest because of**  
**omni directional bonding;**  
**and single component**  
**therefore no restriction** (geometric or coulombic)  
**to number and positioning** of nearest neighbour  
**atoms.**

**High number of nearest neighbors = dense packing.**

**Three common unit cells:** FCC HCP BCC

*(hard sphere = ion core).*

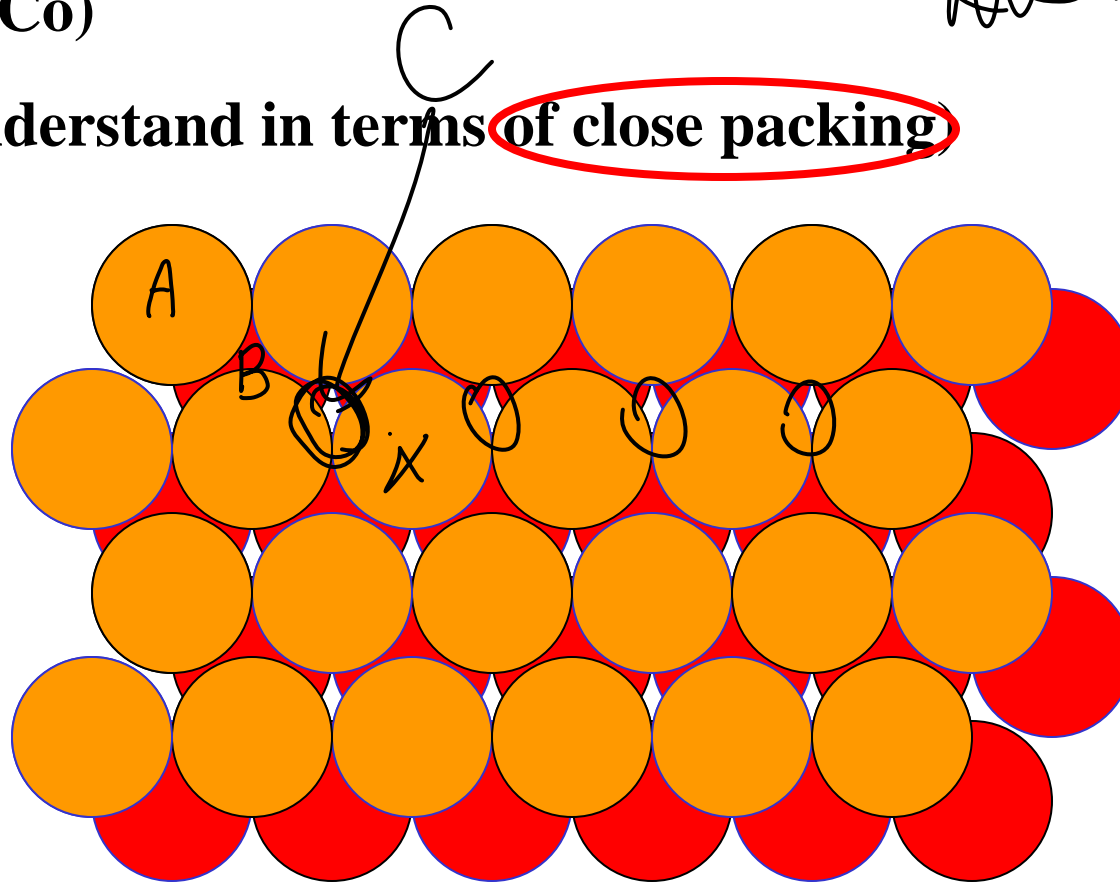
# 1. Hexagonal Close Packed (HCP)

(e.g. Ti, Zn, Co)



(easiest to understand in terms of close packing)

**Next atom of  
next layer?**



# CRYSTAL STRUCTURES

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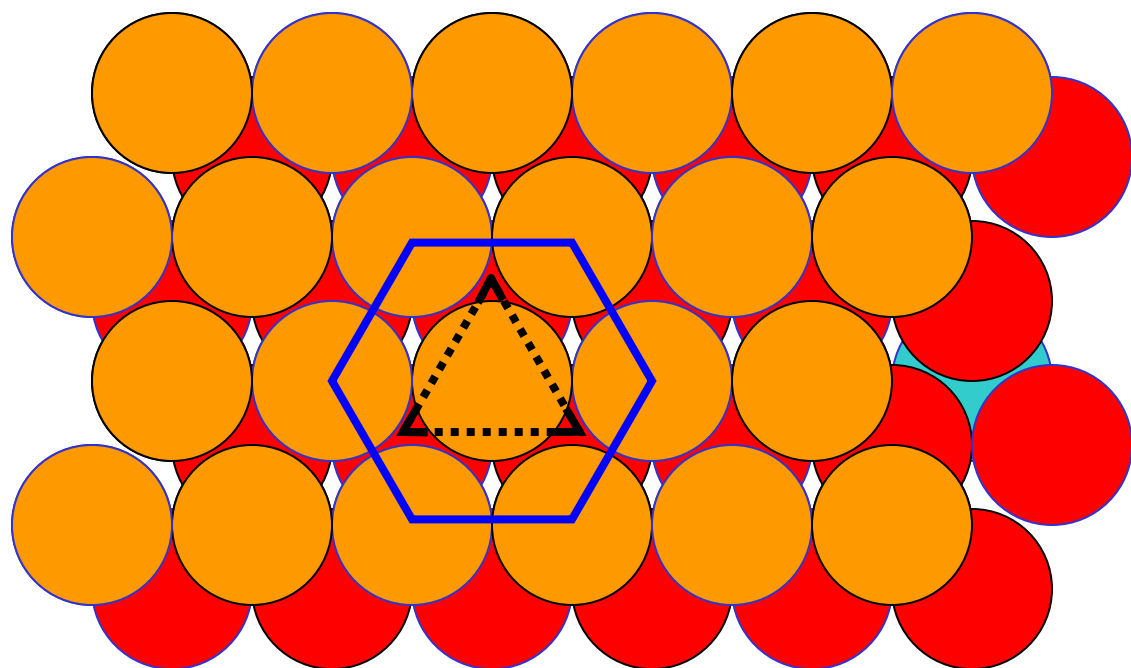
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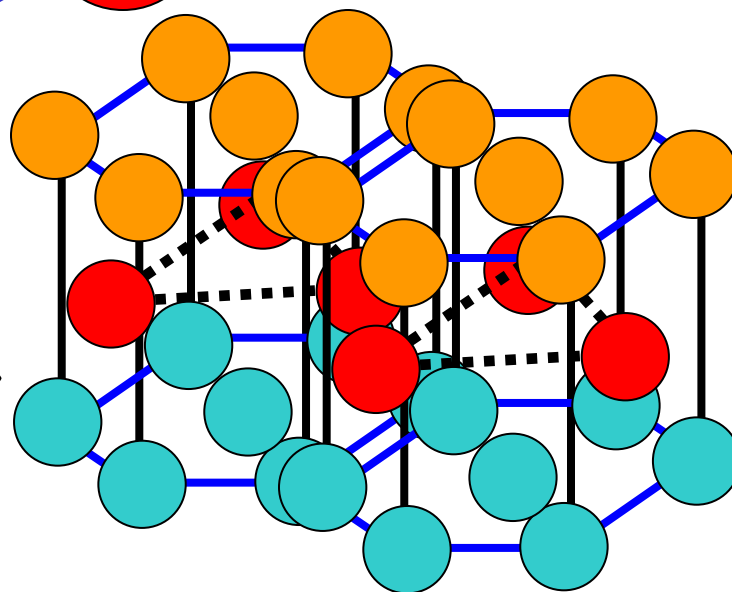
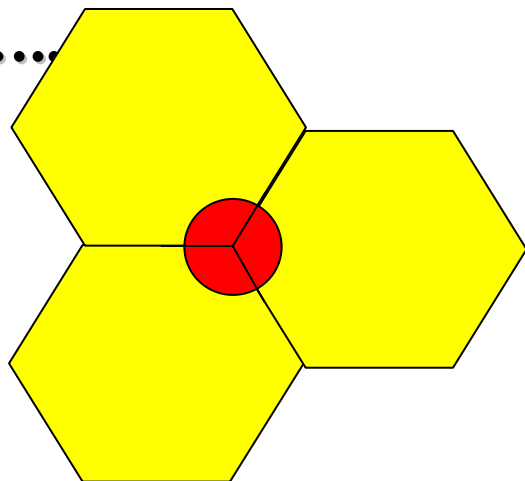


lattice

basis

Where  
are the  
atoms

**THIS DOESN'T QUITE  
WORK.....**

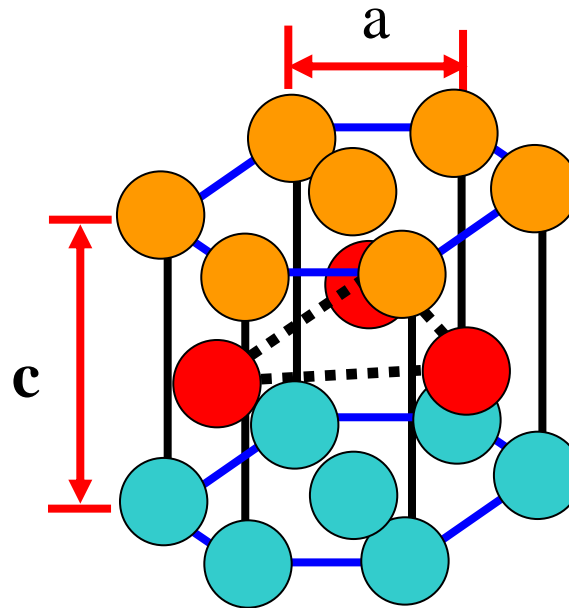


Joining up all the unit cells **should** form the crystal



## Description of hexagonal unit cell

size of unit cell: (lattice parameters)



obtain  $c$  and  $a$  in terms of  $R$ , atom radius

ideal  $c/a$  ratio = 1.633 but some deviation in real life

Geometry!

Define **any** shape

Define **any** dimension in terms of  $R$

**number of atoms per unit cell = 6**

(1/6 of each of the 12 'corner' atoms

1/2 of each of the 2 face centered atoms

3 center atoms)

(mathematically?)

**atomic packing factor**

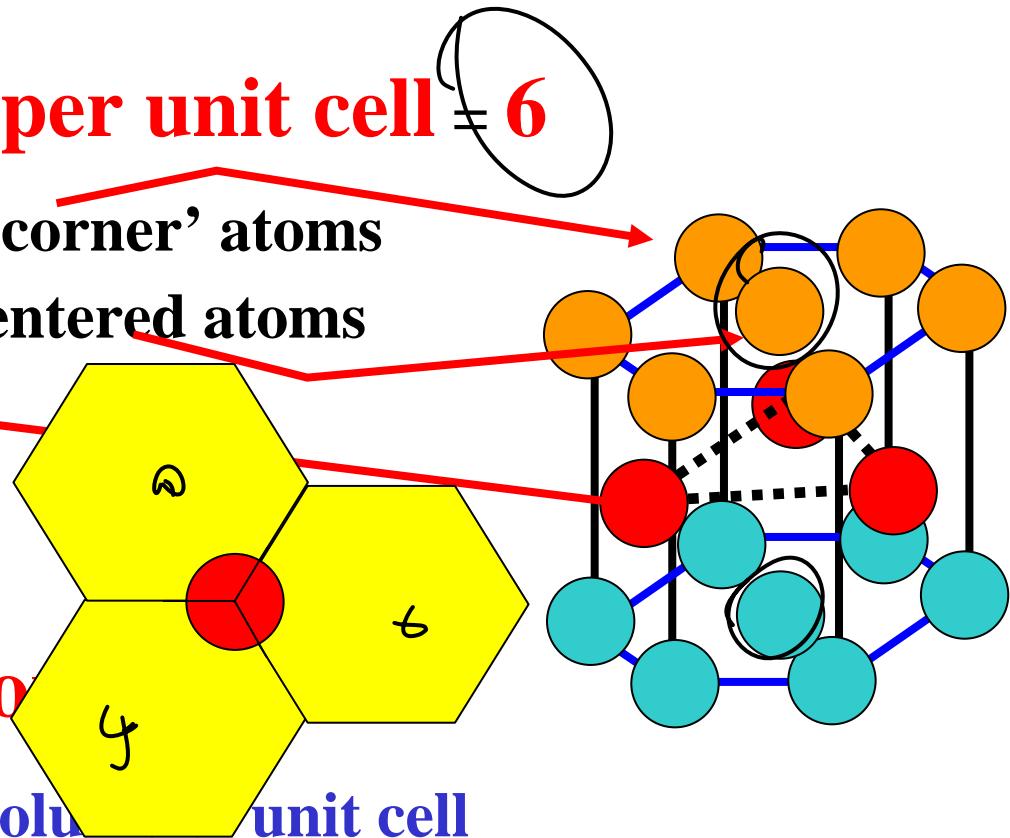
volume of solid (spheres)/volume of unit cell

APF = 0.74\*  $\left( \frac{\# \text{ atoms}}{\text{volume of 1 sphere}} \right)$

**-coordination number**

(number of atoms touching or nearest neighbours)

(by inspection of centre atom, above) = **12**



# Closest Packing

Equal sized spheres

“Closest Packed”

Hexagonal array:

6 nearest neighbors  
in the plane

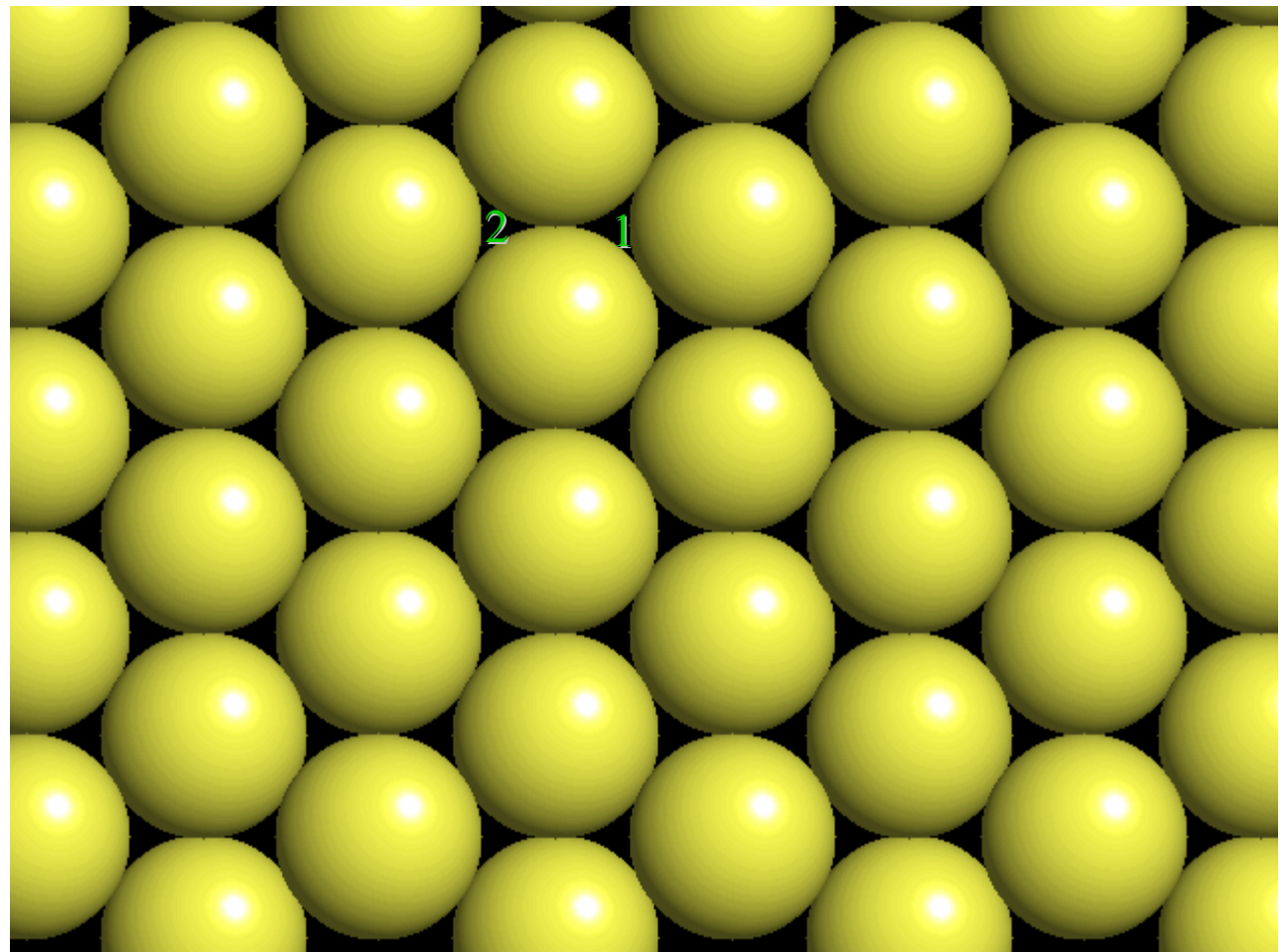
Note dimples in which  
next layer atoms will  
settle

Two dimple types:

Type 1 point NE

Type 2 point SW

They are **equivalent** since  
you could rotate the  
whole structure  $60^\circ$  and  
exchange them



# Closest Packing

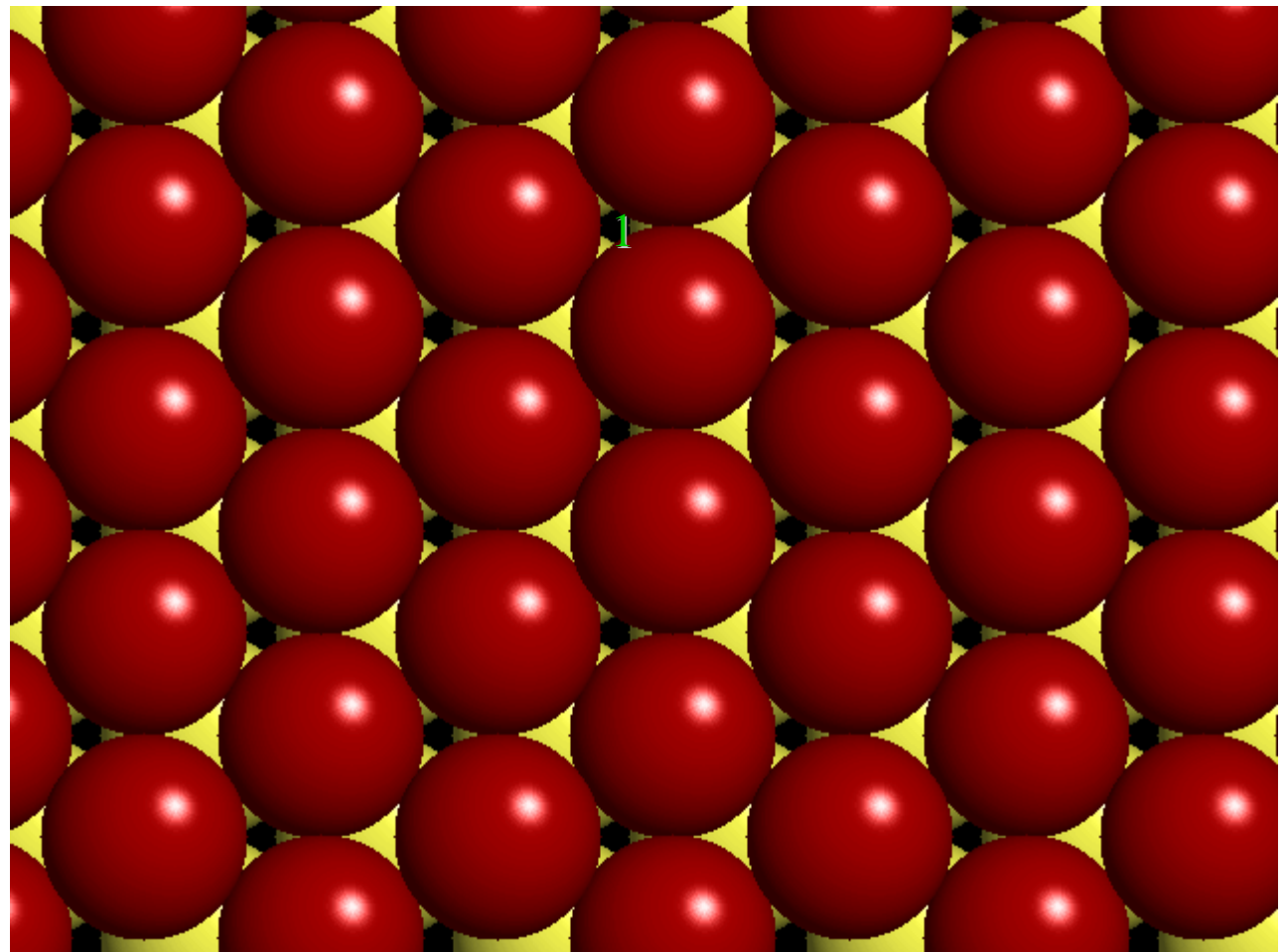
Add next layer (red)

Red atoms can only  
settle in one  
dimple type

Both types are  
identical and red  
atoms could  
settle in either

Once first red atom  
settles in, **can  
only fill other  
dimples of that  
type**

In this case filled all  
type 2 dimples



# Closest Packing

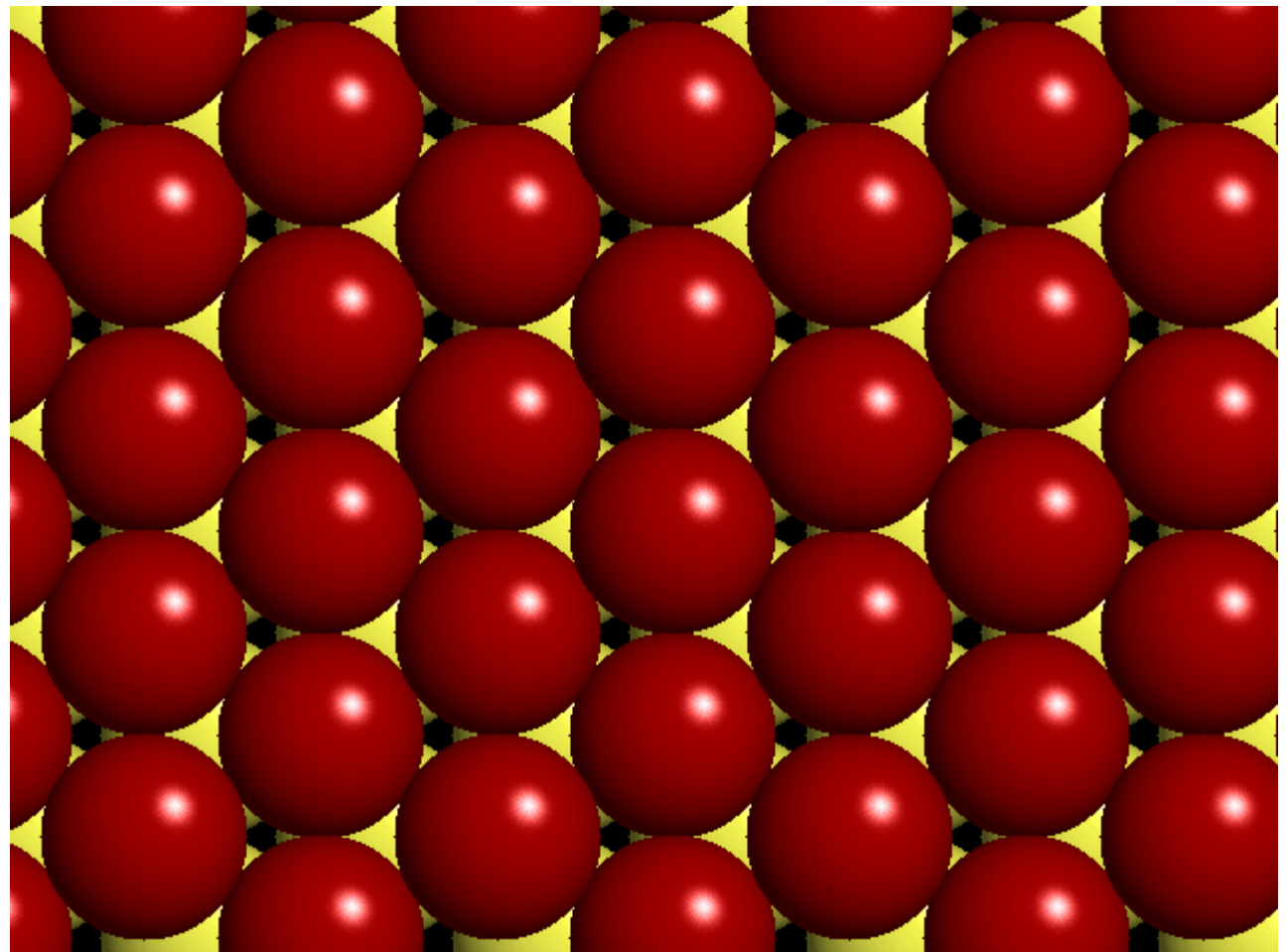
Third layer ??

Third layer dimples  
are now different!

Call layer 1 **A sites**

Layer 2 = **B sites** (*no matter which choice of dimples is occupied*)

Layer 3 can now occupy A-type site (directly above yellow atoms) or **C-type site** (above voids in both A and B layers)

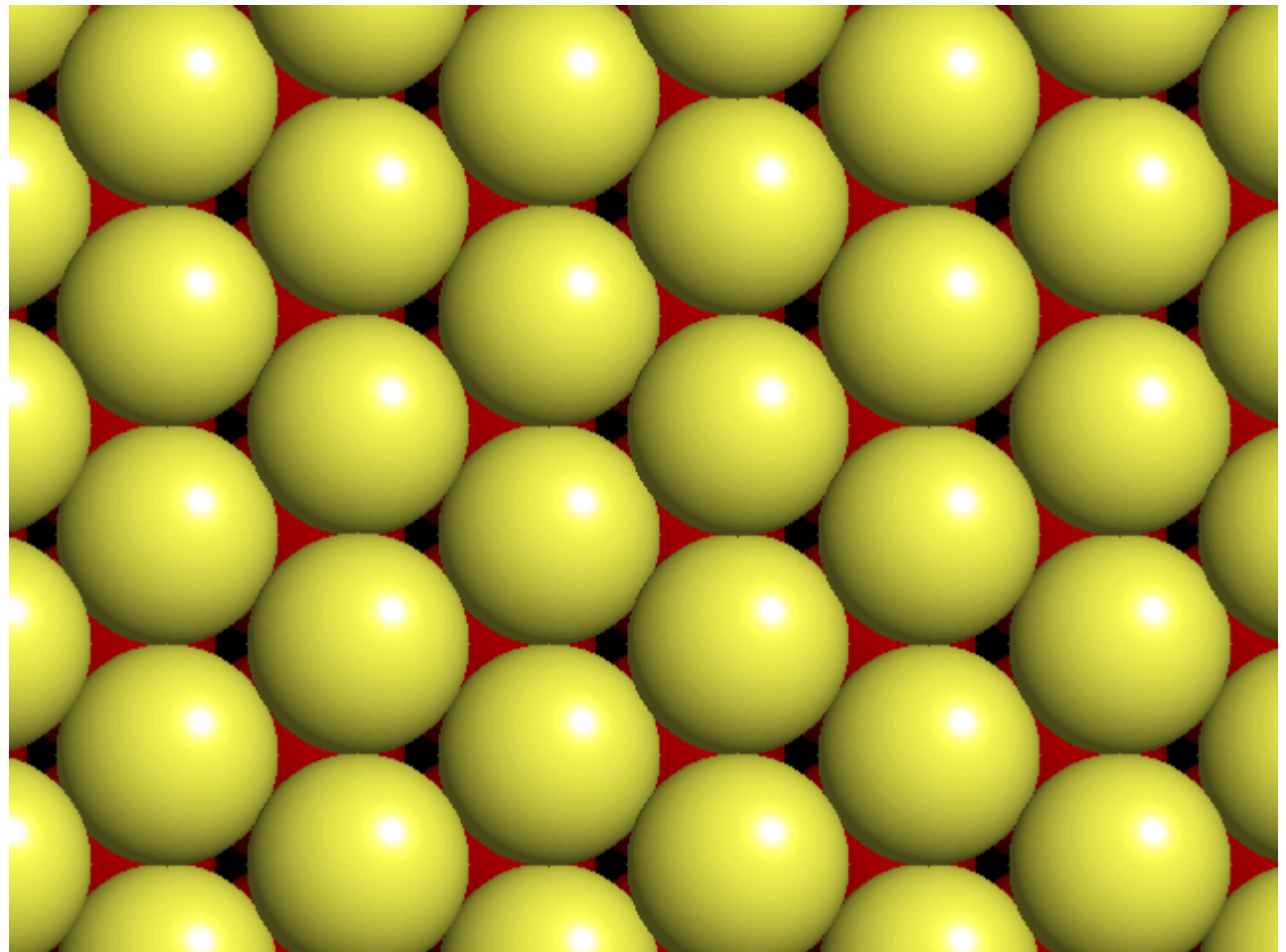


# Closest Packing

Third layer:

If occupy A-type site  
the layer ordering  
becomes A-B-A-B  
and creates a  
hexagonal closest  
packed structure  
(HCP)

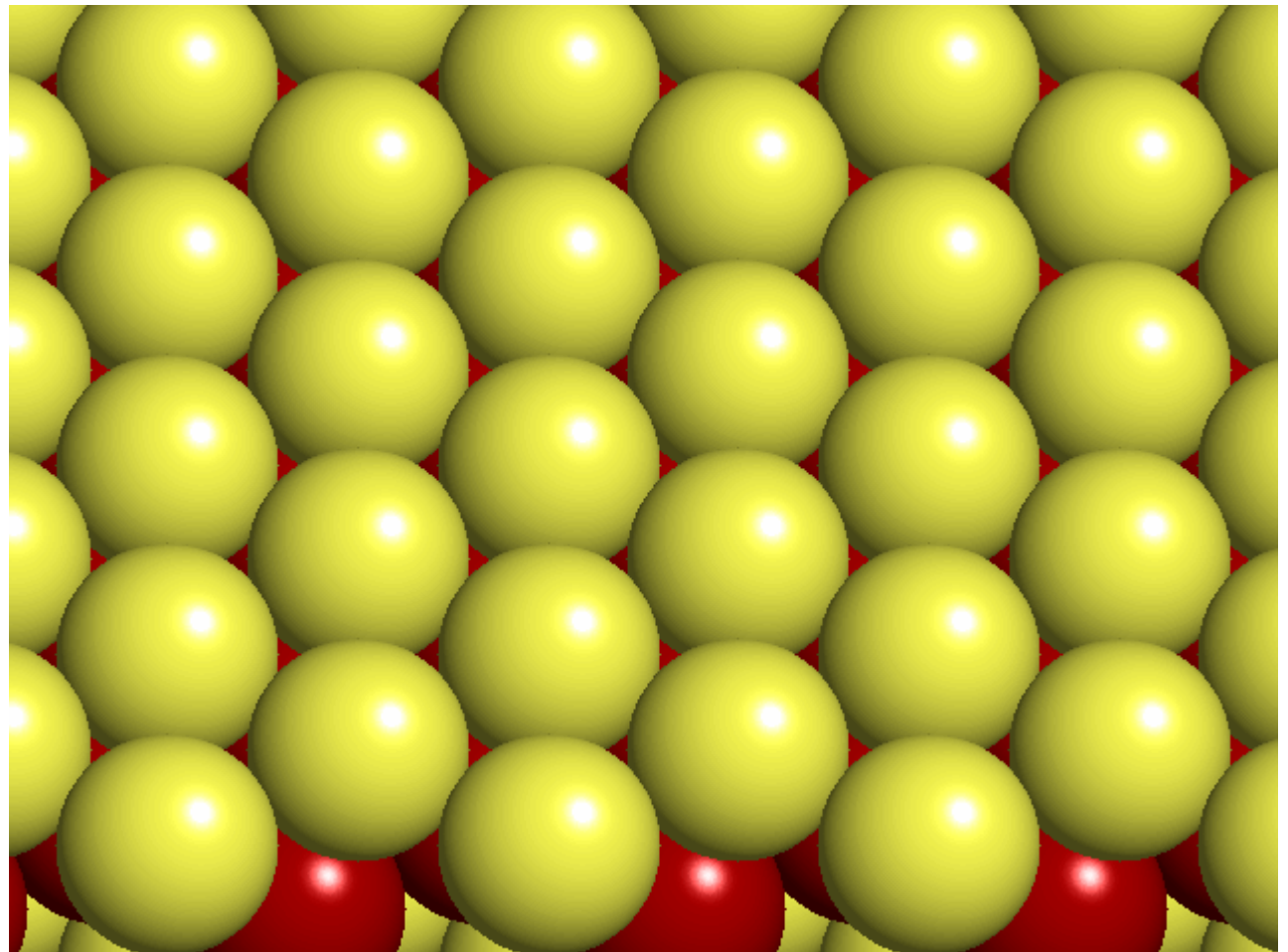
Coordination number  
(nearest or touching  
neighbors) = 12  
6 coplanar  
3 above the plane  
3 below the plane



# Closest Packing

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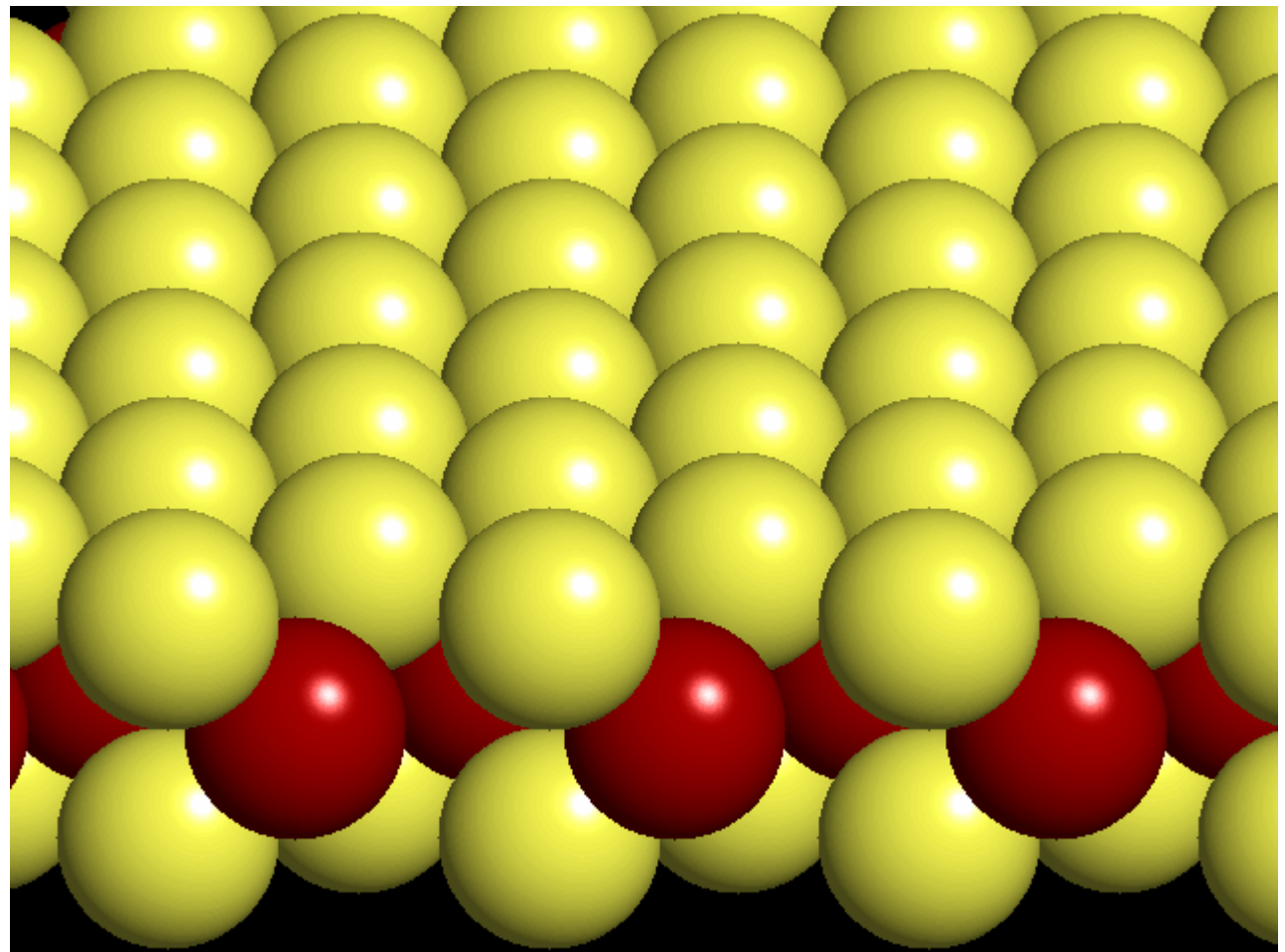




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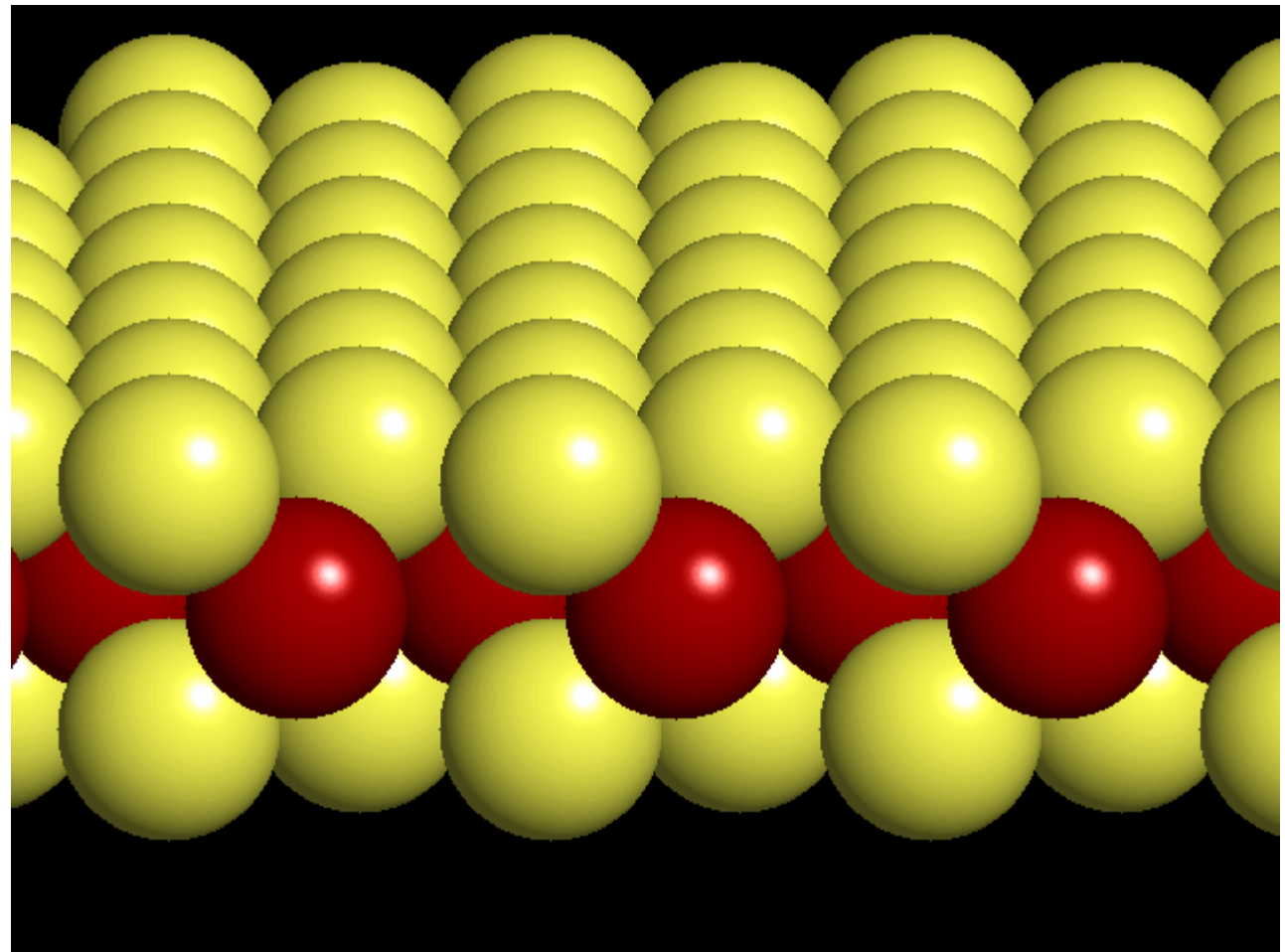




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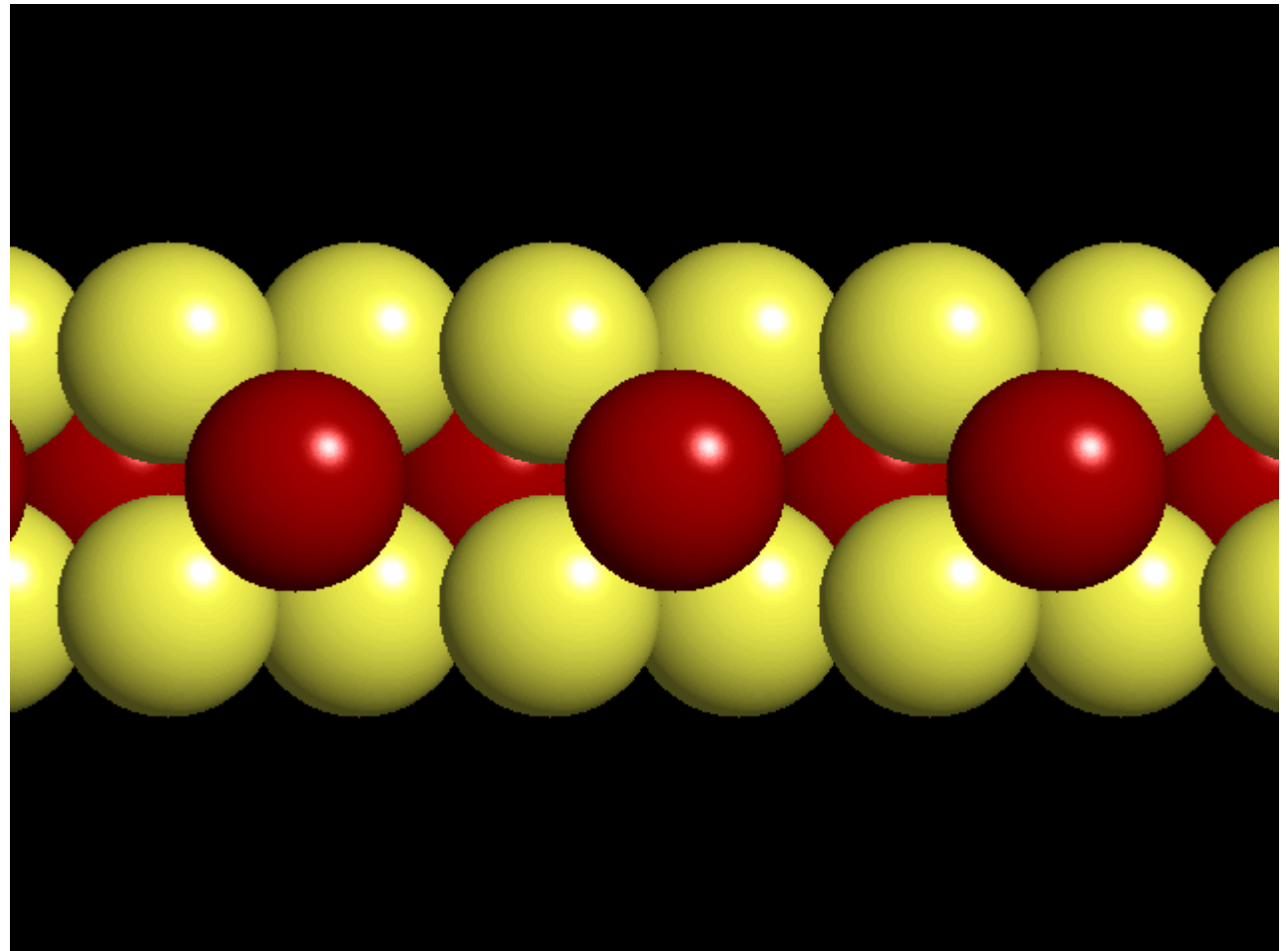


# Closest Packing

Third layer:

If occupy A-type site  
the layer ordering  
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and creates a  
hexagonal closest  
packed structure  
(HCP)

Note top layer atoms  
are directly above  
bottom layer atoms



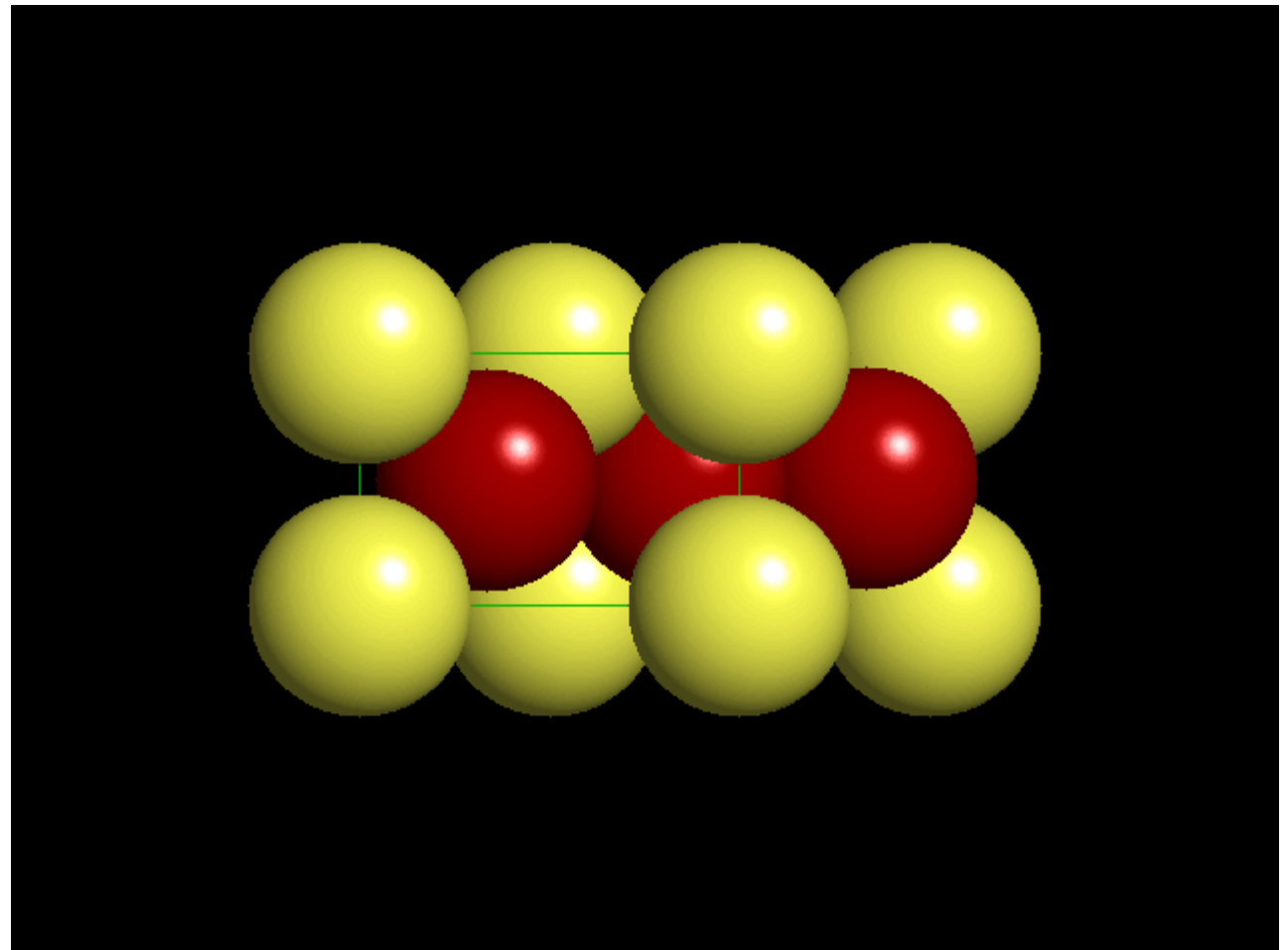
*J. Winter*

*Whitman College*

# Closest Packing

Third layer:

Unit cell



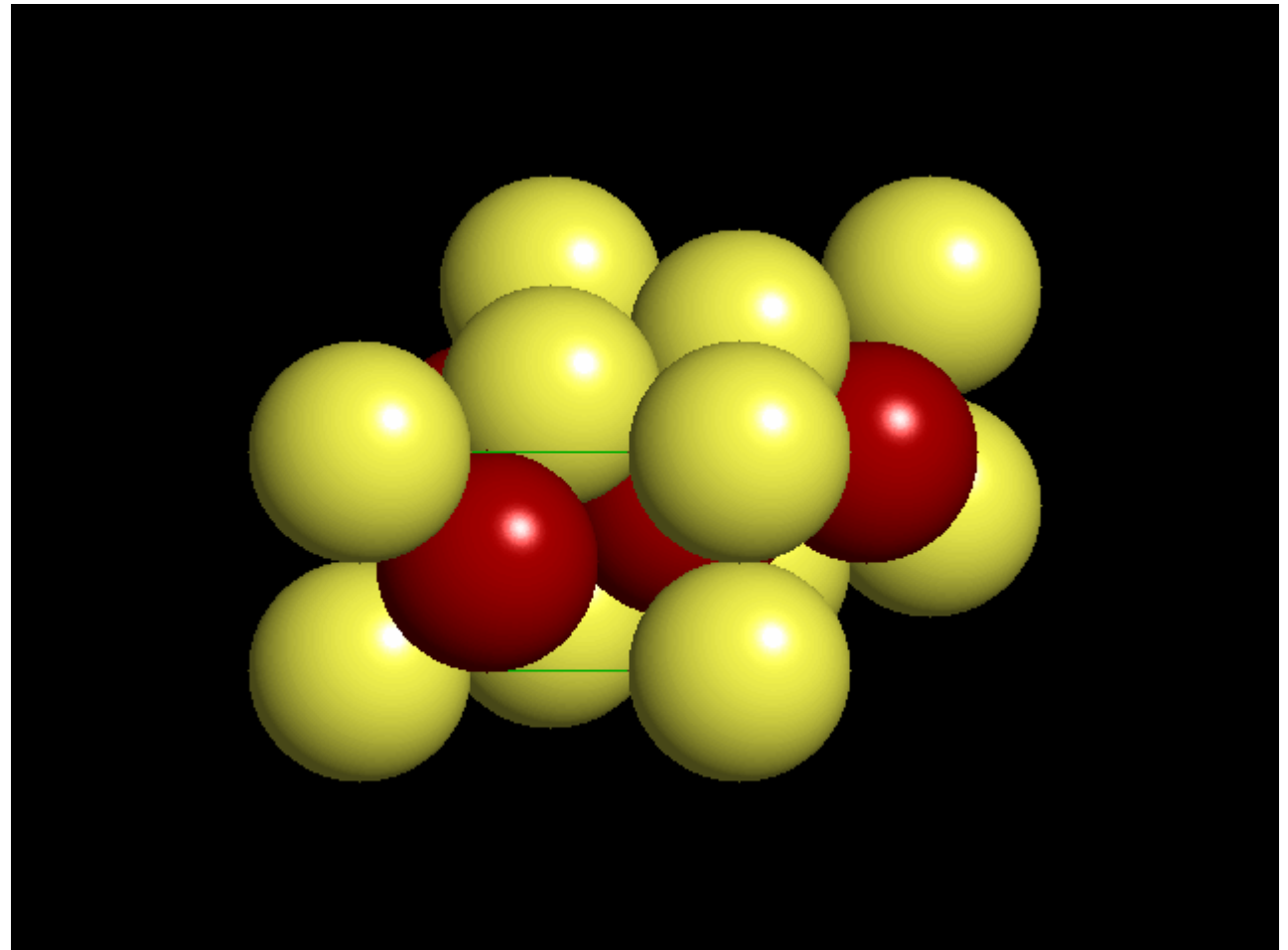
*J. Winter*

*Whitman College*

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Third layer:

Unit cell



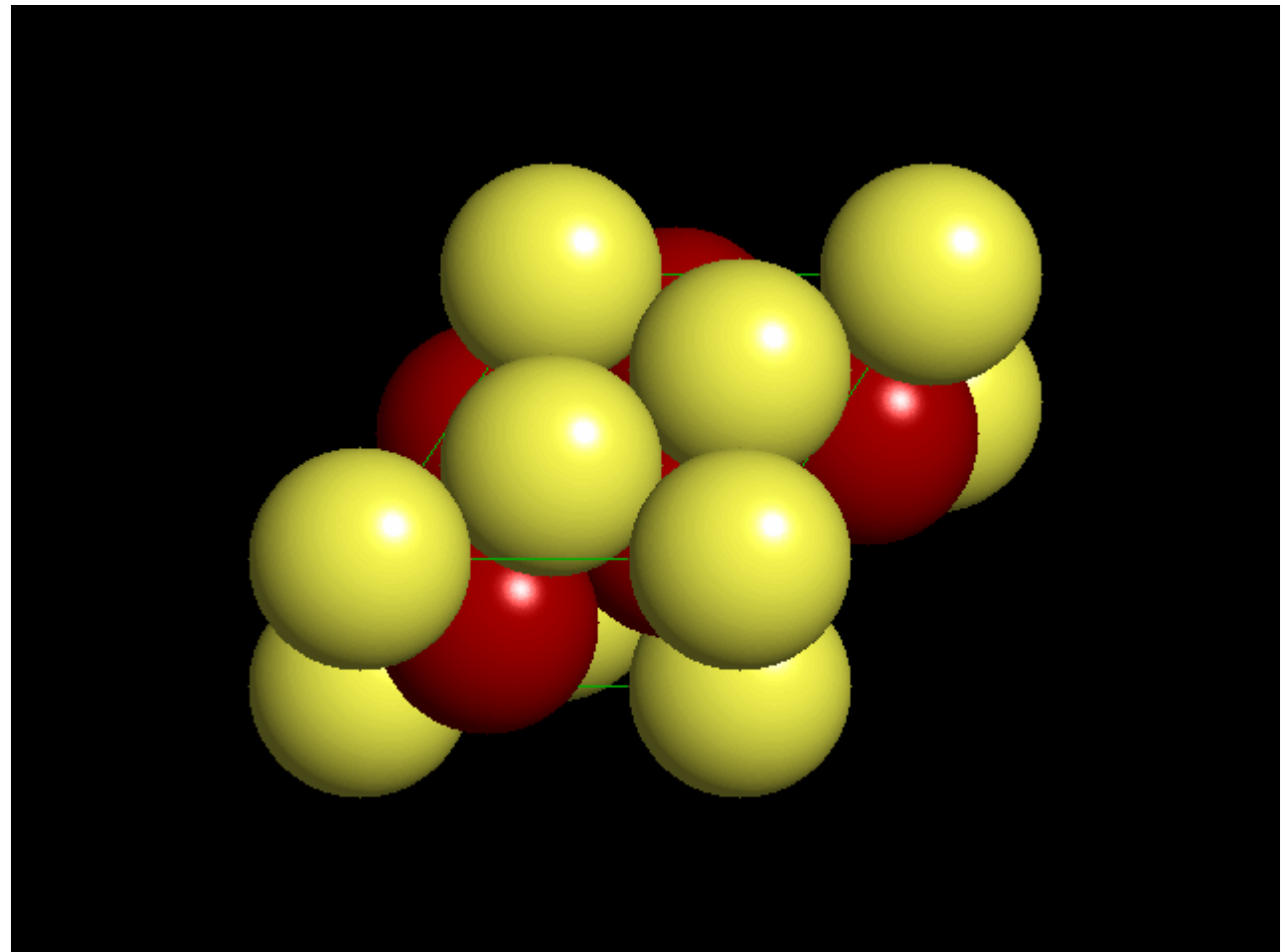
*J. Winter*

*Whitman College*

# Closest Packing

Third layer:

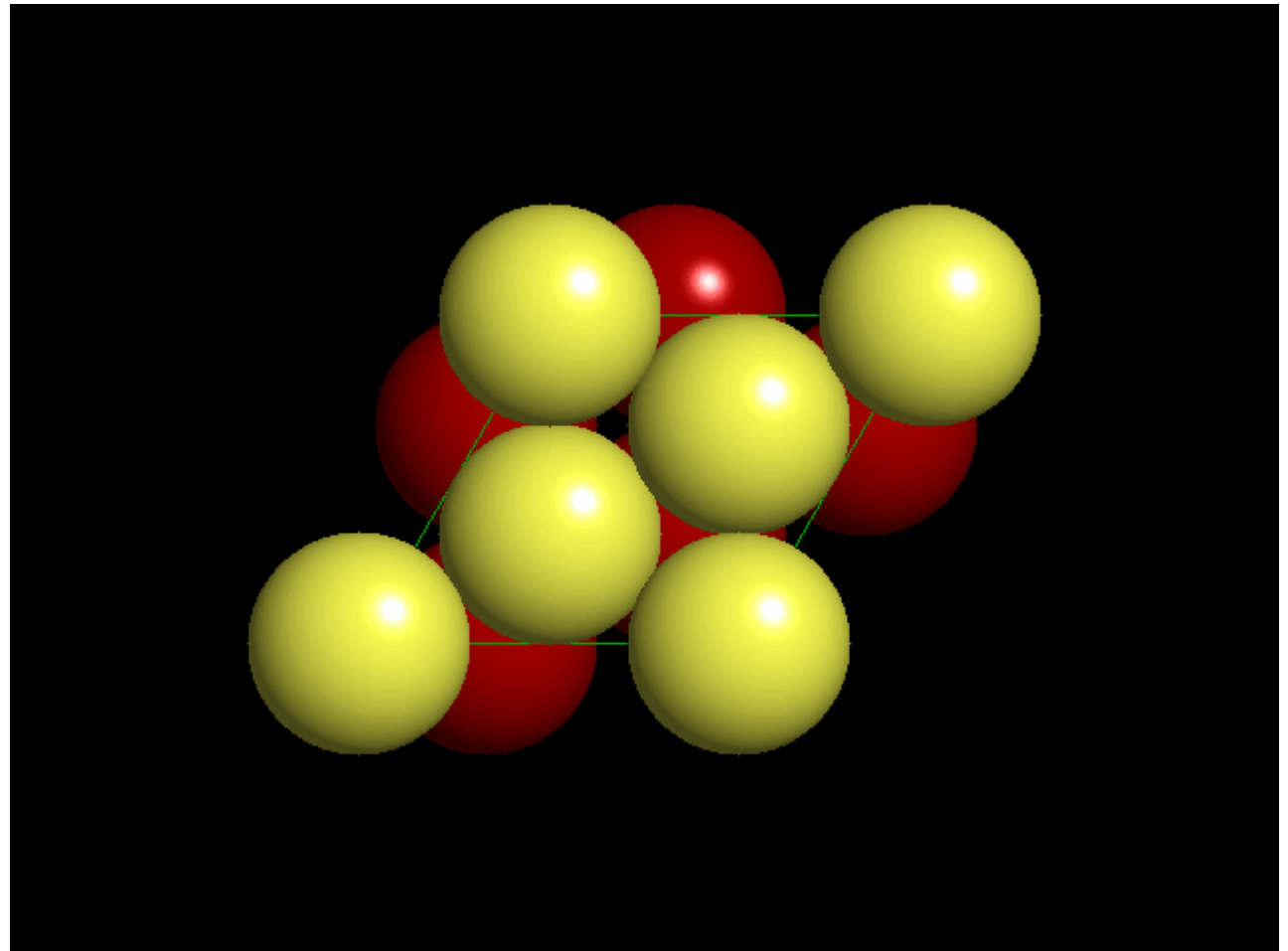
Unit cell



# Closest Packing

Third layer:

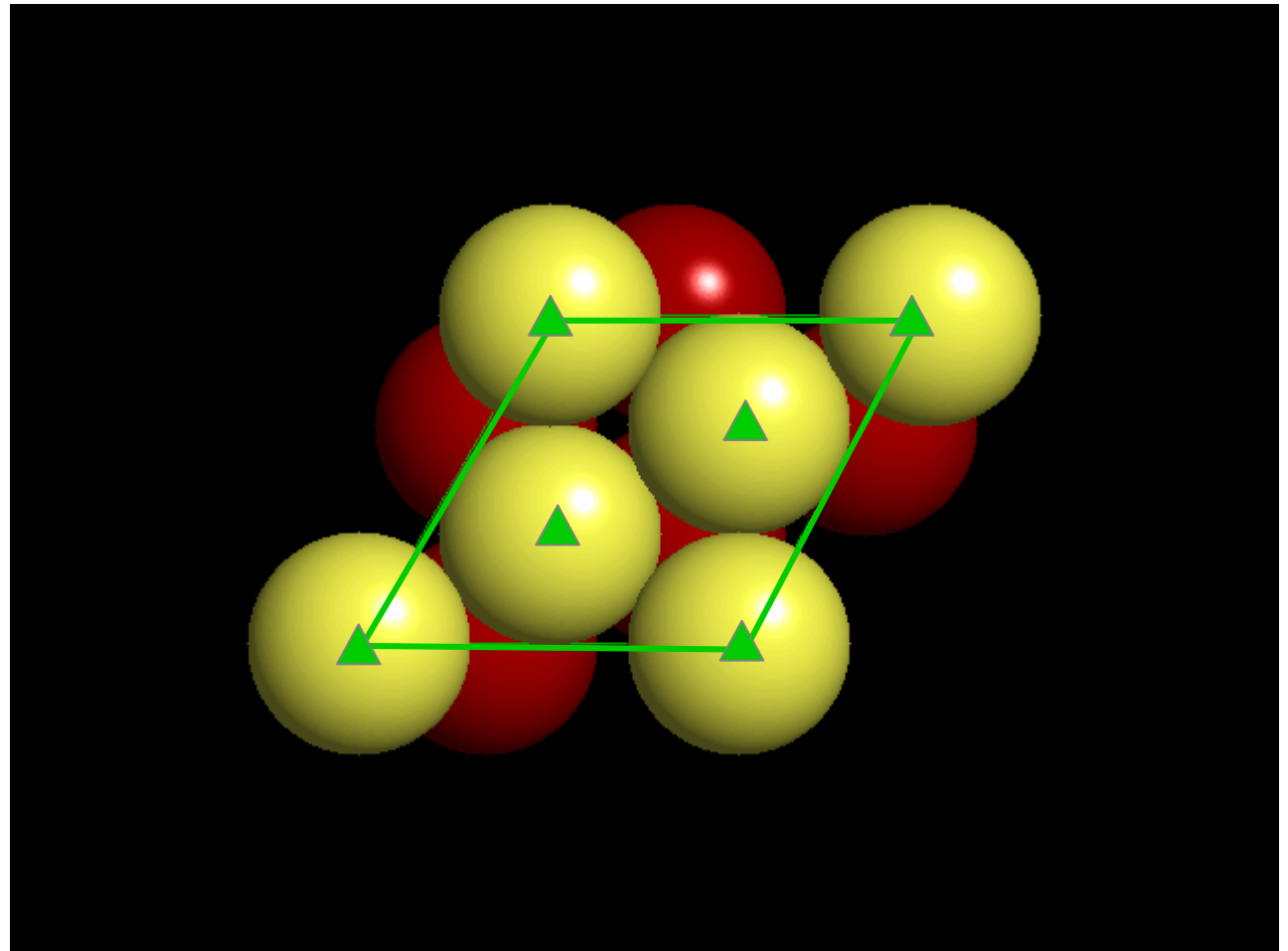
View from top shows  
hexagonal unit cell



# Closest Packing

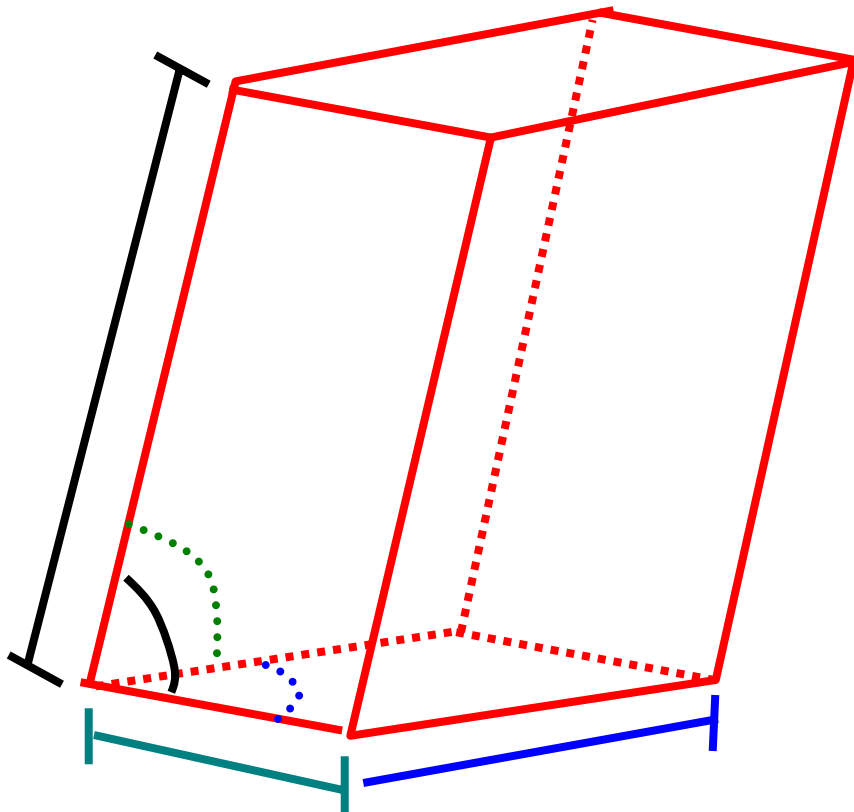
Third layer:

View from top shows  
hexagonal unit cell

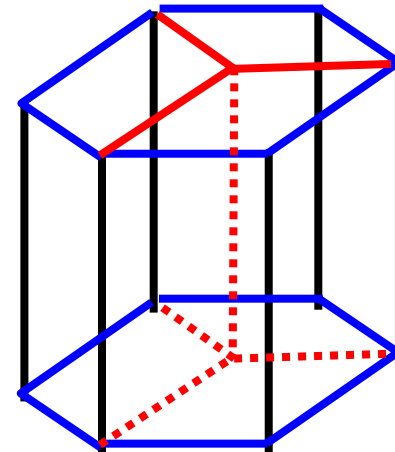


# OTHER CRYSTAL SYSTEMS (UNIT CELLS)

are defined by 6 parameters, the three axial lengths  
and the three interaxial angles



*(note HCP can be broken down into 3 parallelopipeds)*

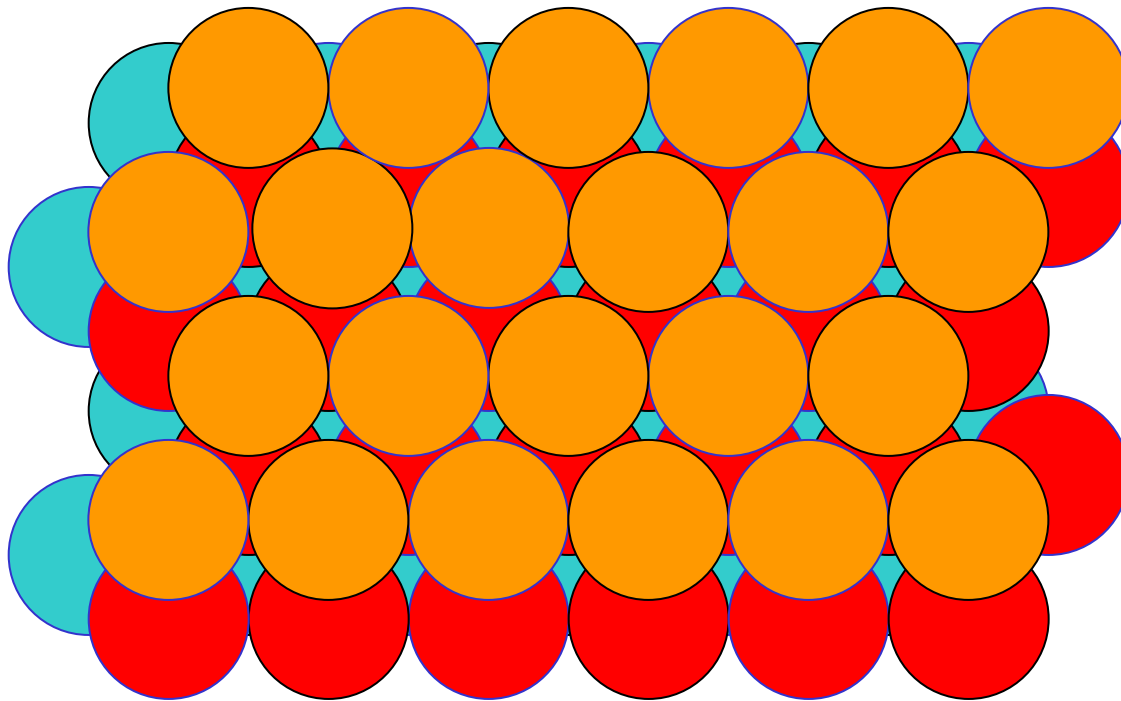


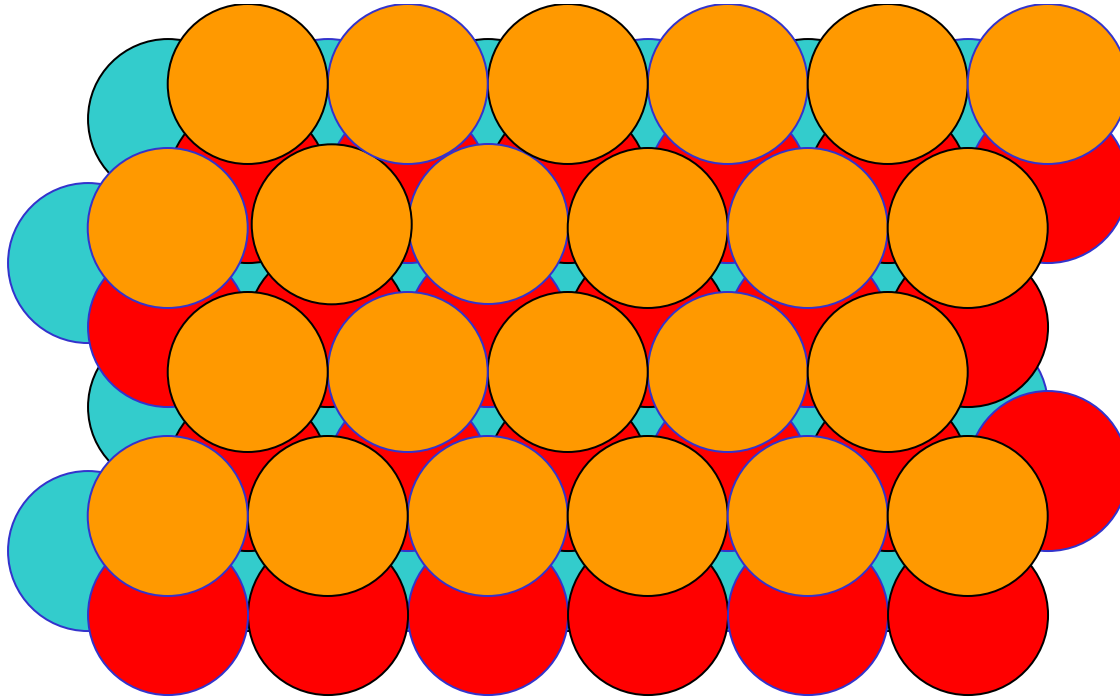


## 2. FACE CENTERED CUBIC (FCC)

(e.g. Cu, Al, Ag)

next easiest to understand in terms of **CLOSE PACKING**





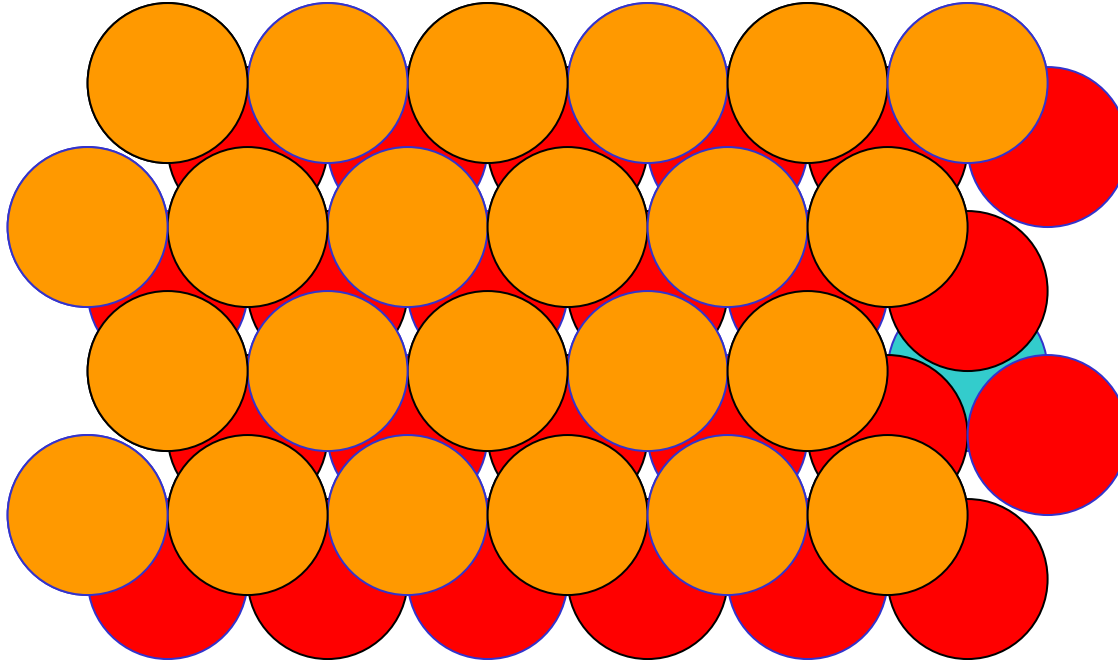
packing often  
described in  
terms of  
**‘stacking’** of  
close packed  
layers

FCC stacking is:

**abcabcabc....**

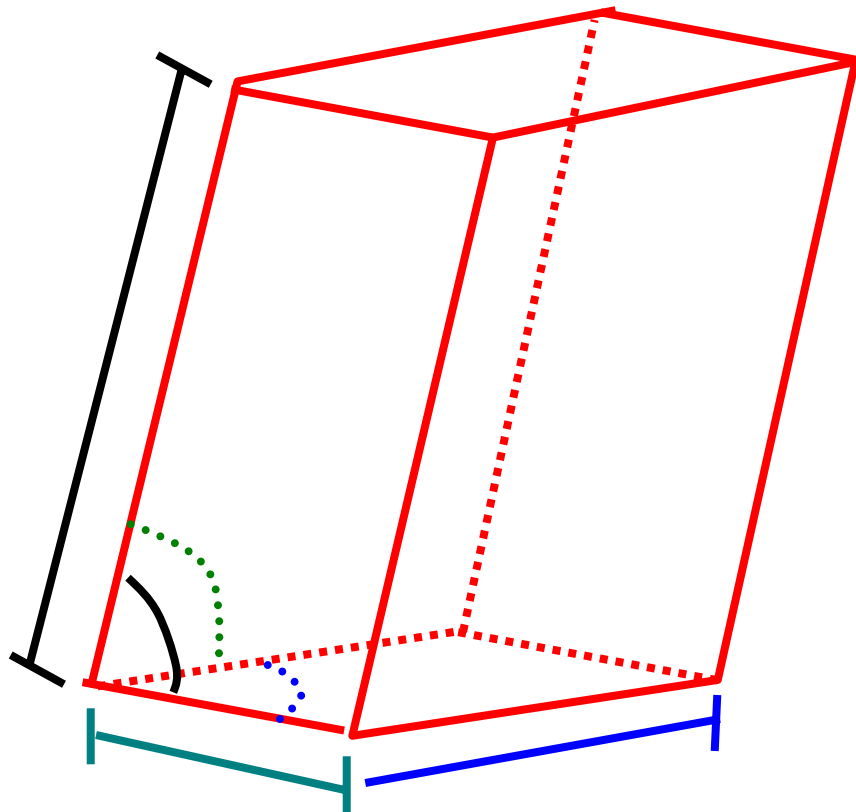
HCP is:

**abababab....**

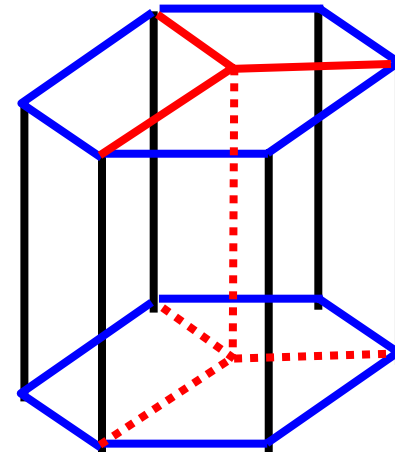


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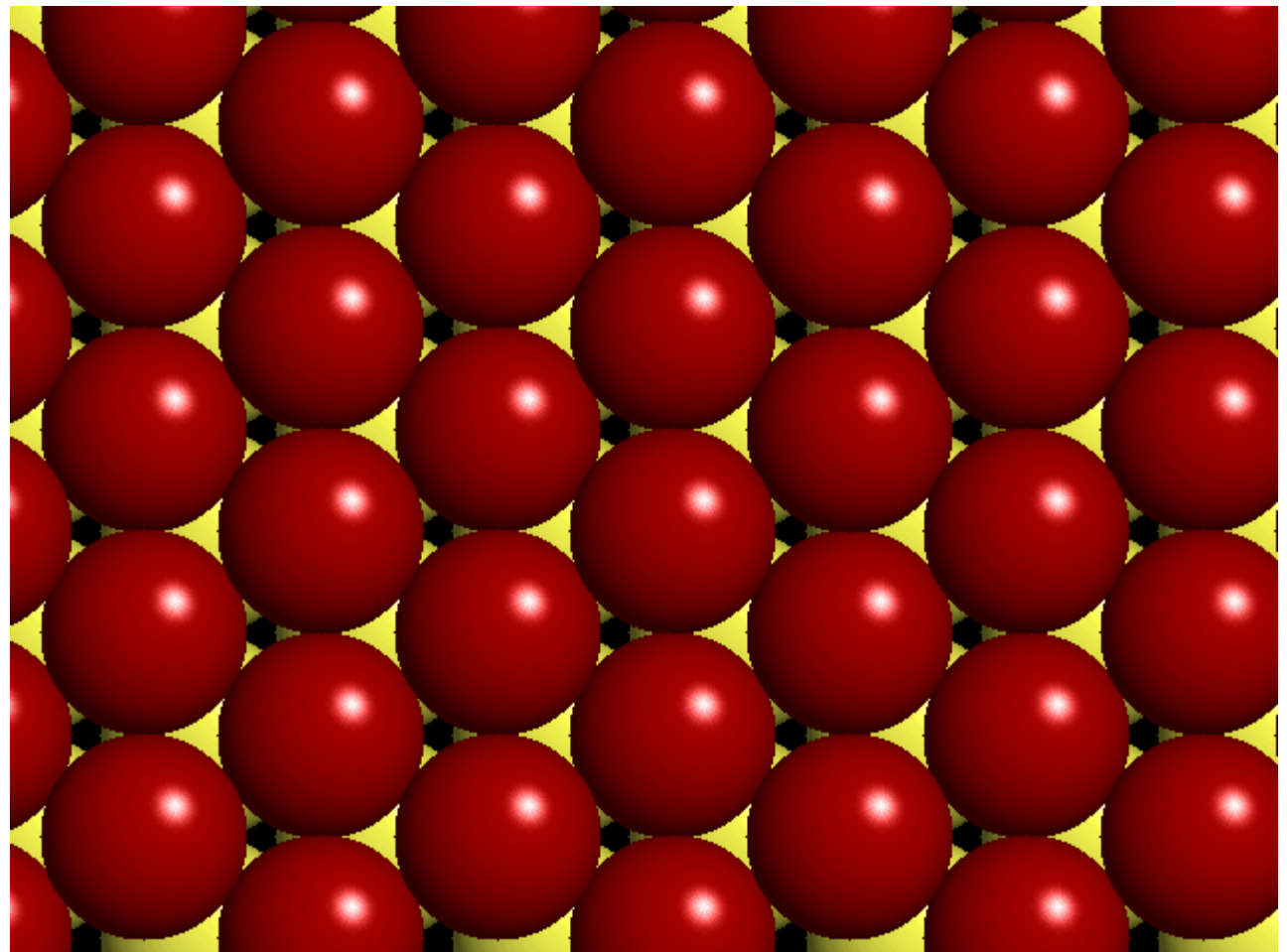


*(HCP can be broken  
down into 3  
parallelopipeds)*



# Closest Packing

Alternatively we could place the third layer in the **C-type site** (above voids in both A and B layers)

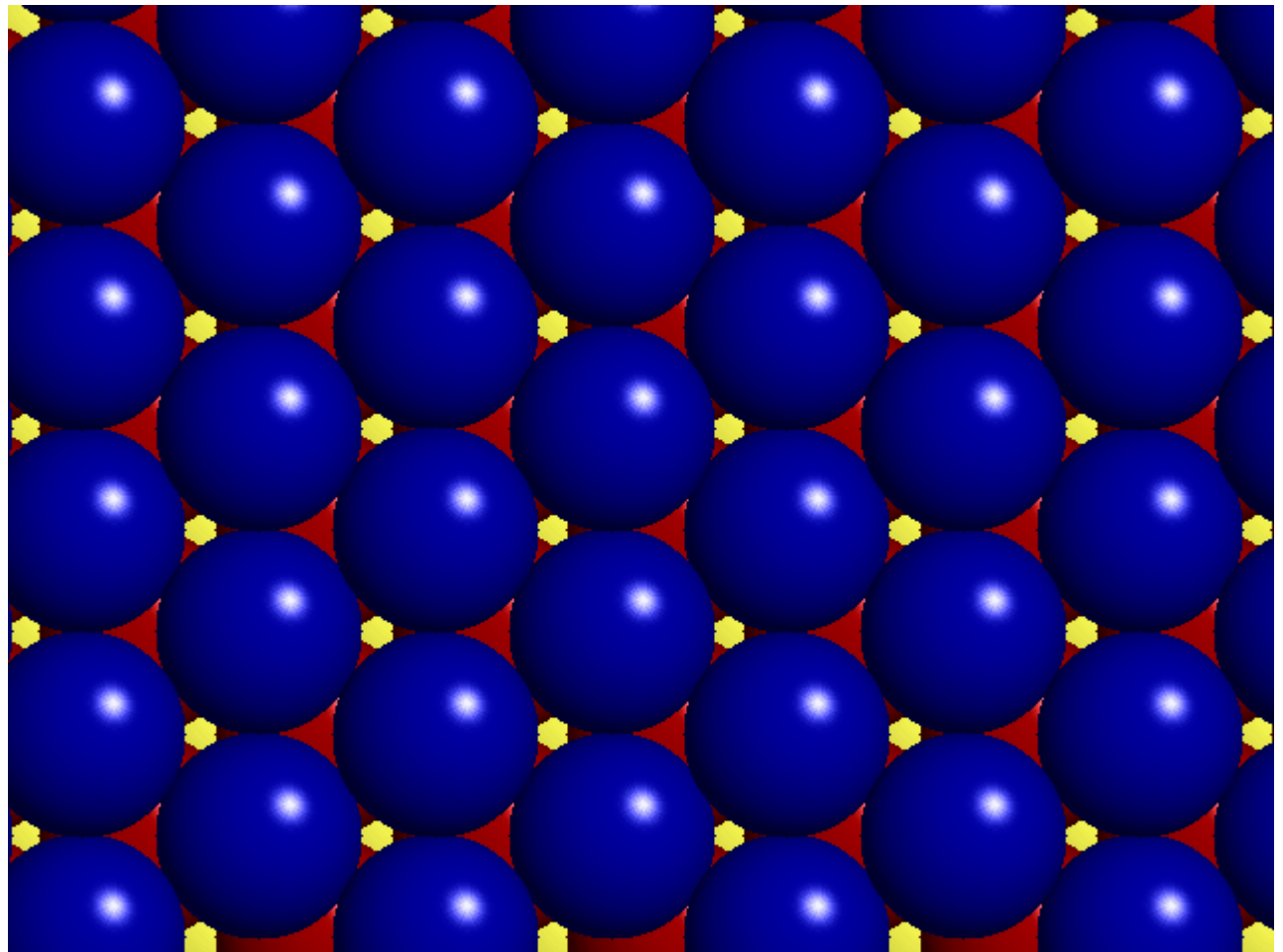


# Closest Packing

Third layer:

If occupy **C-type site**  
the layer ordering is  
A-B-C-A-B-C and  
creates a **cubic  
closest packed  
structure (CCP)**

Blue layer atoms are  
now in a unique  
position above voids  
between atoms in  
layers A and B

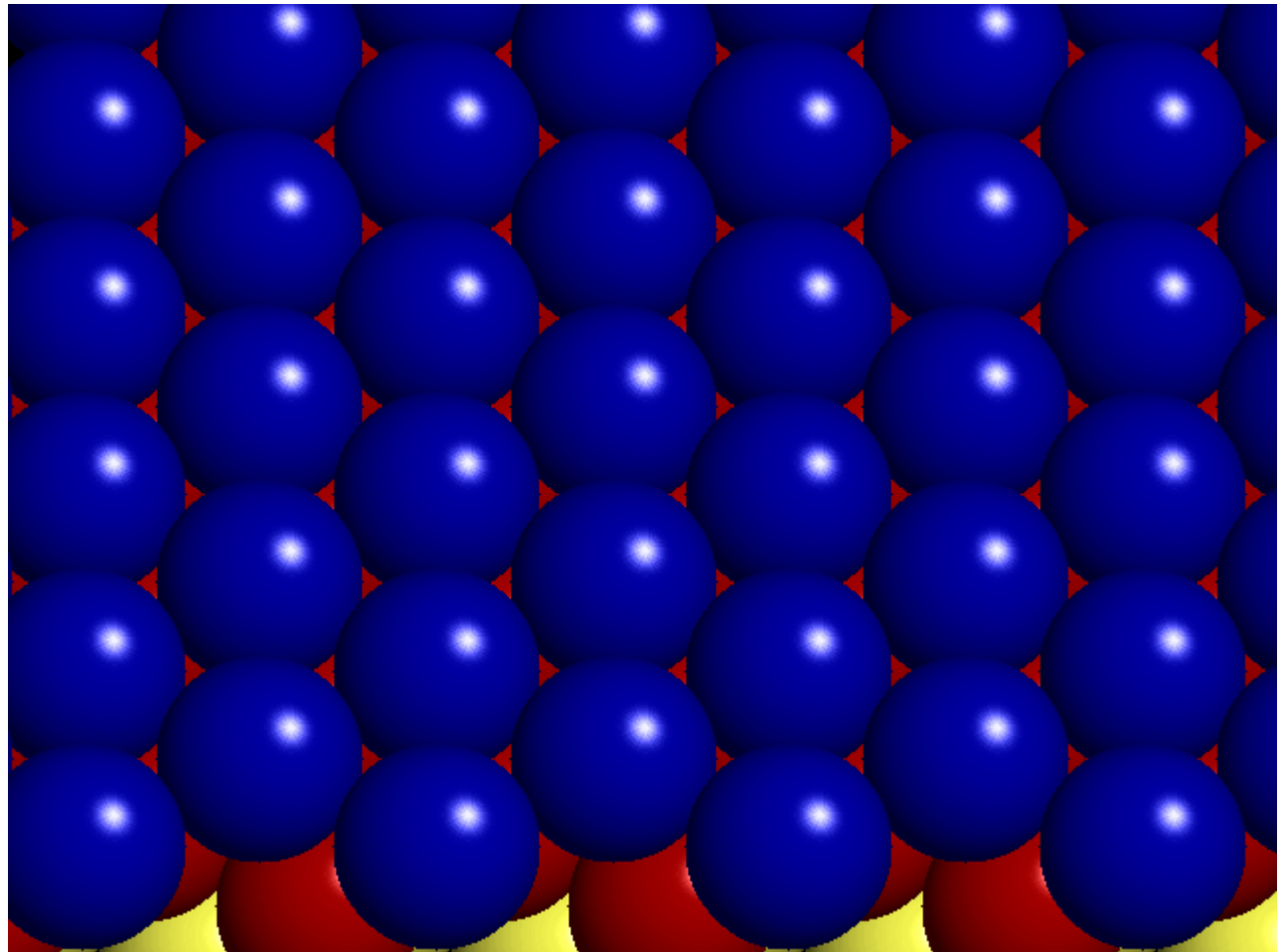


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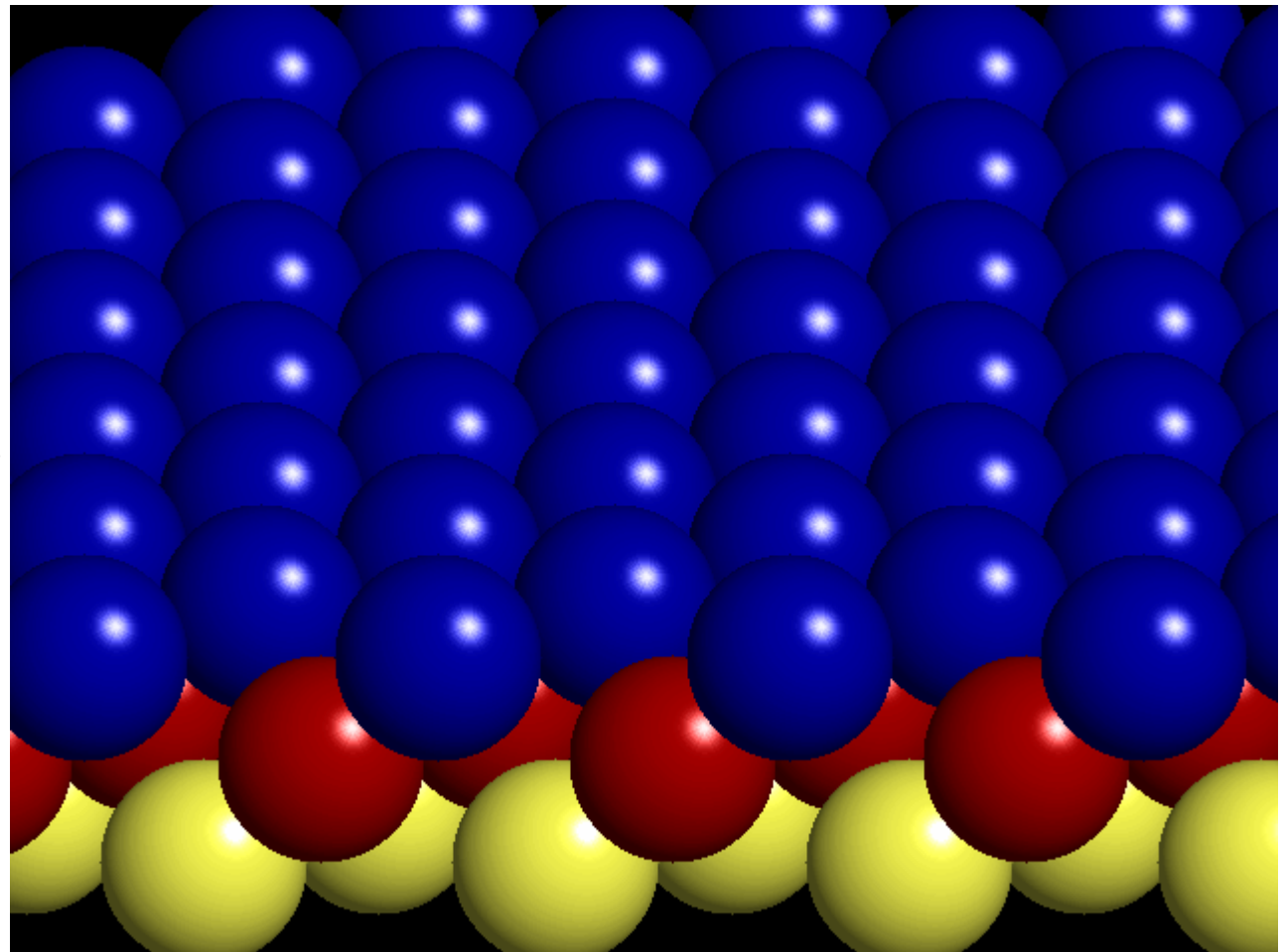


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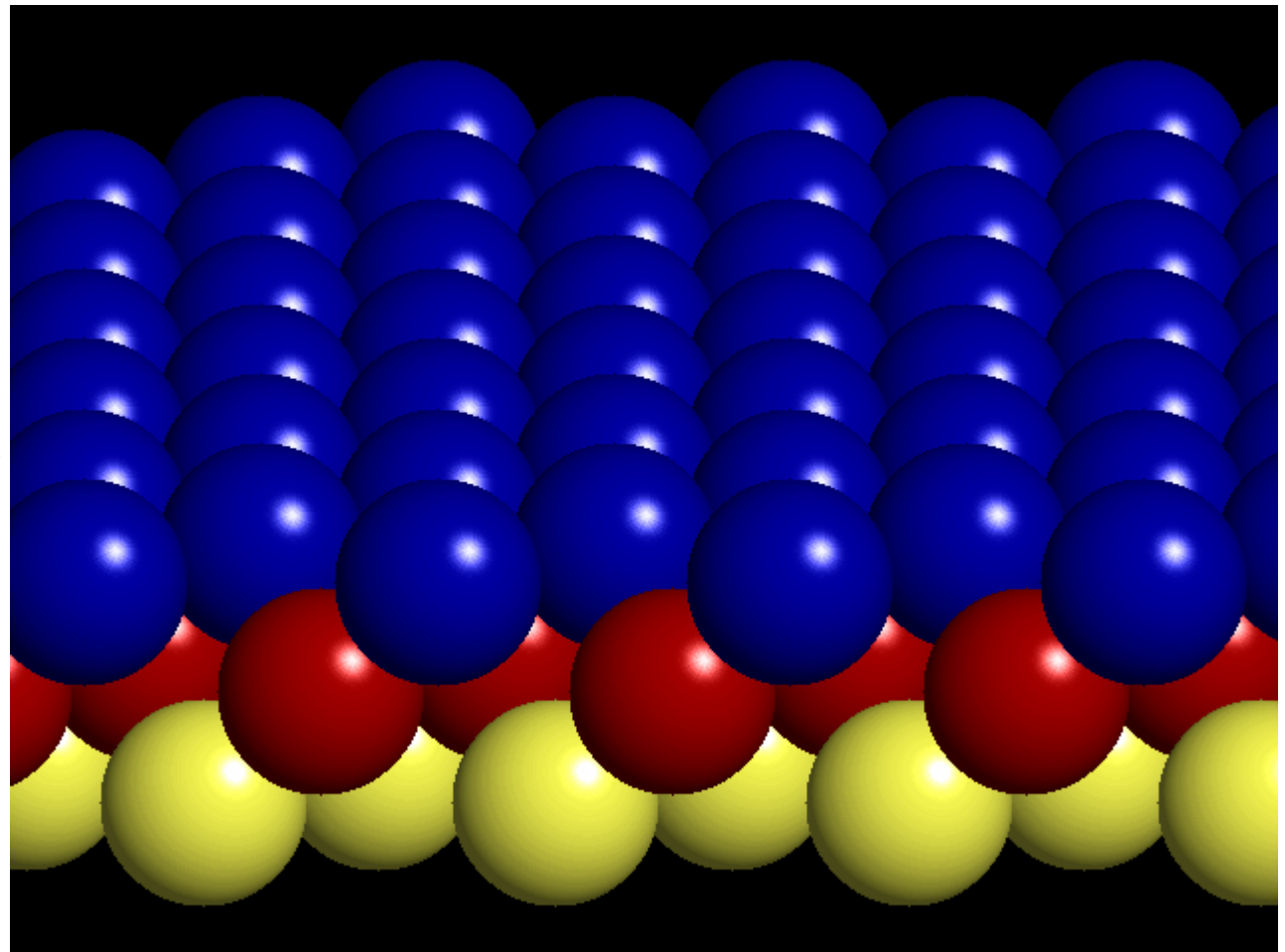


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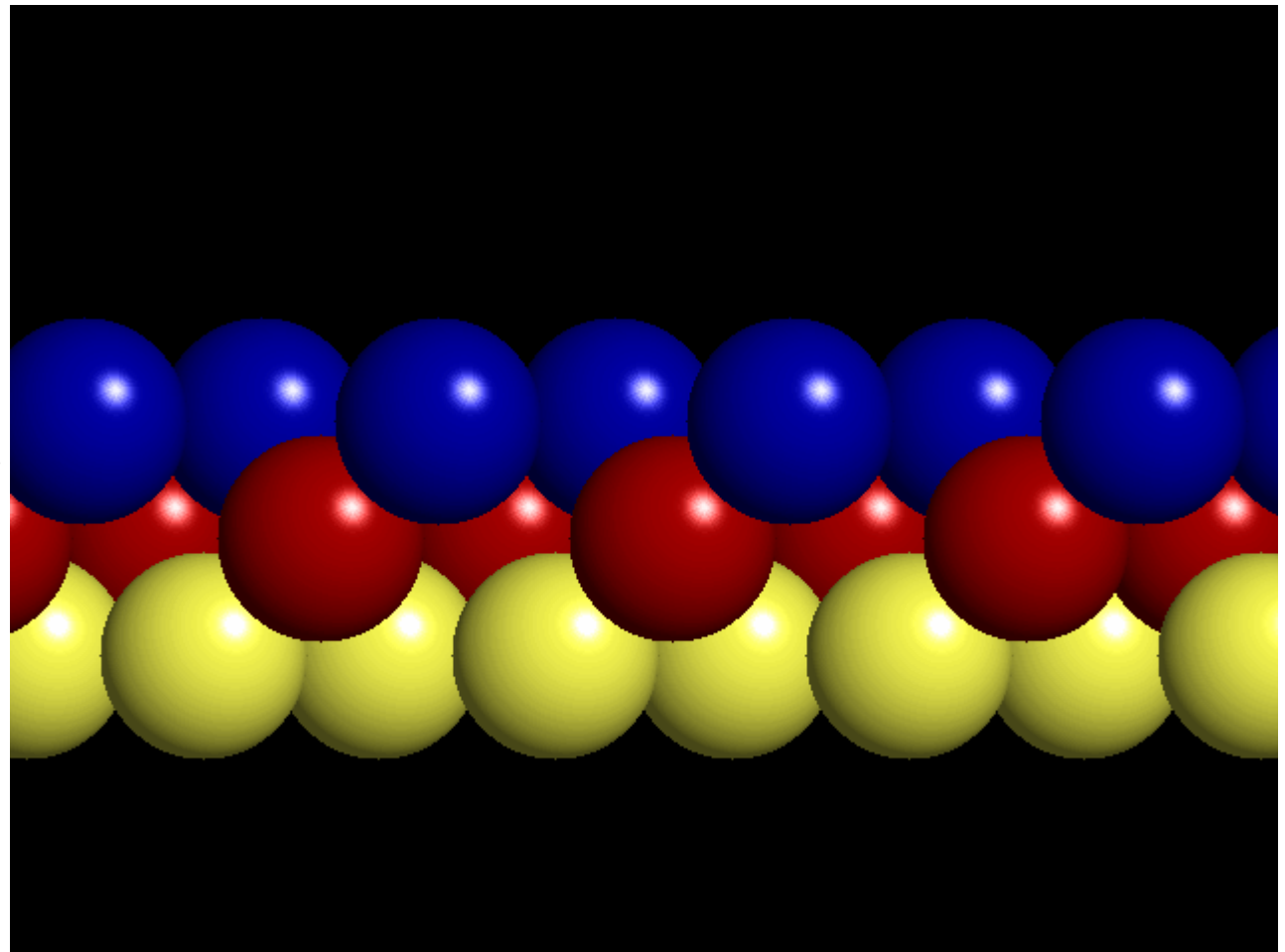


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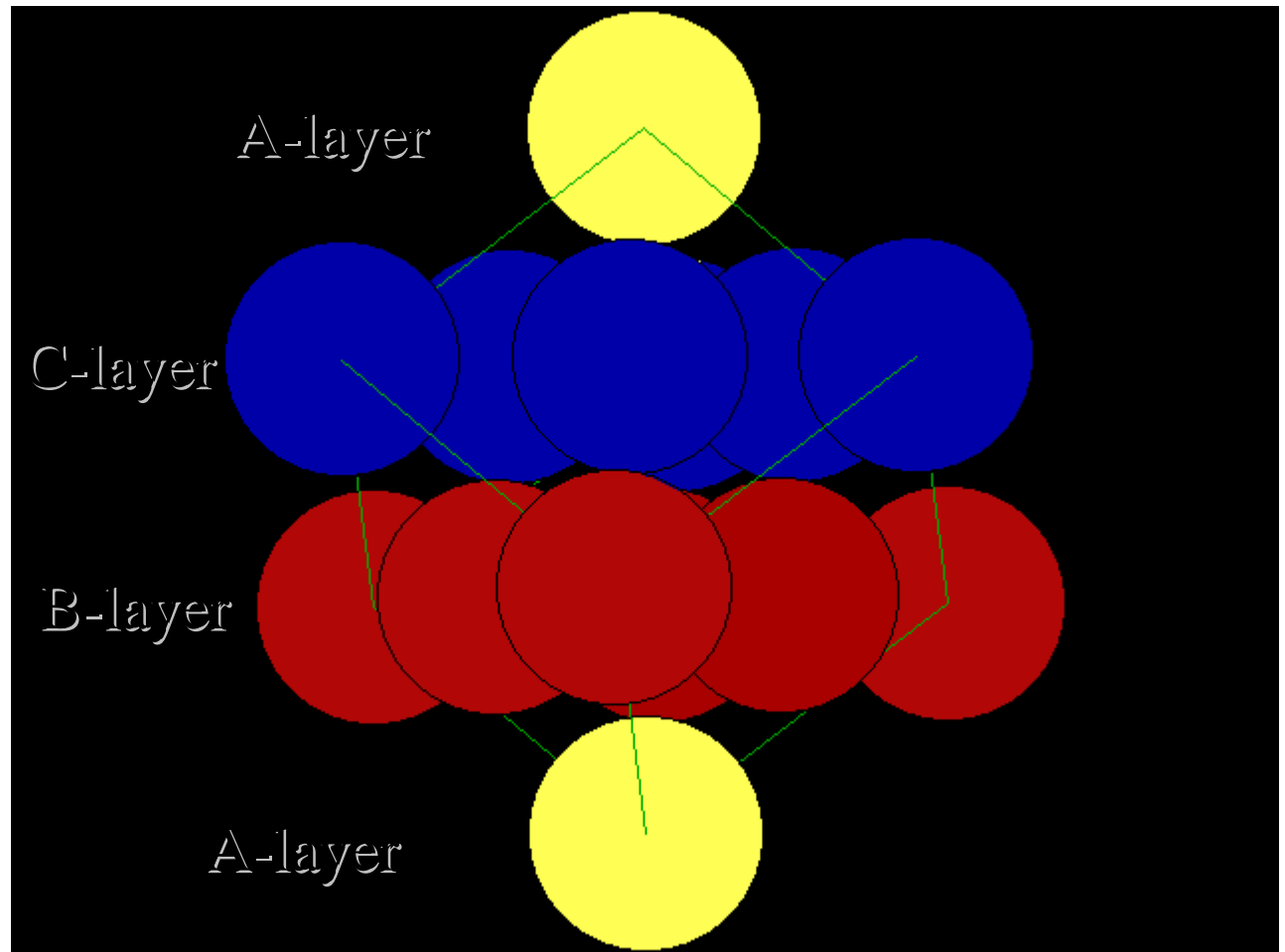
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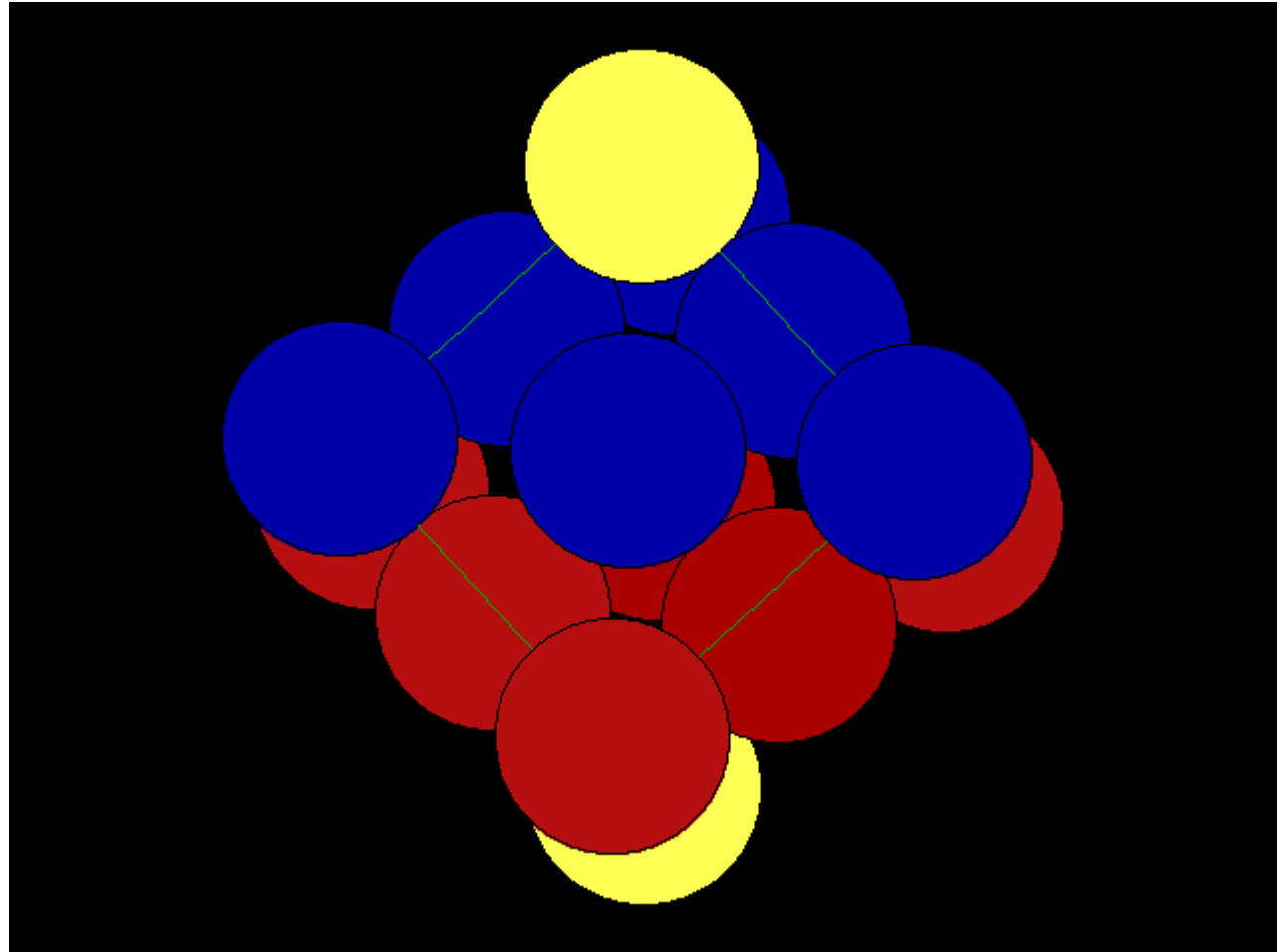
View from the same side  
shows the **face-  
centered cubic** unit  
cell that results.

The atoms are slightly  
shrunk to aid in  
visualizing the  
structure



# Closest Packing

Rotating toward a top  
view

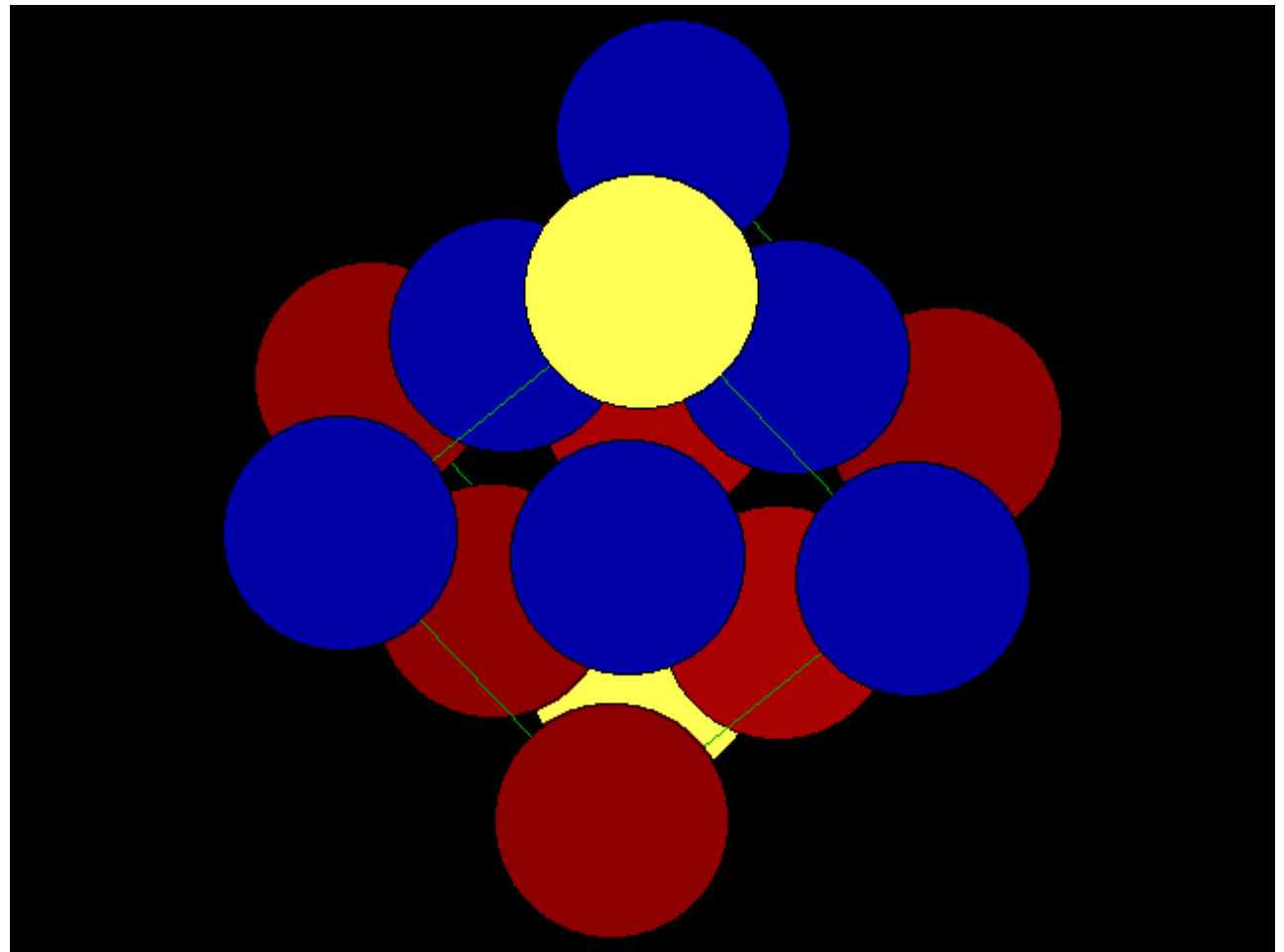


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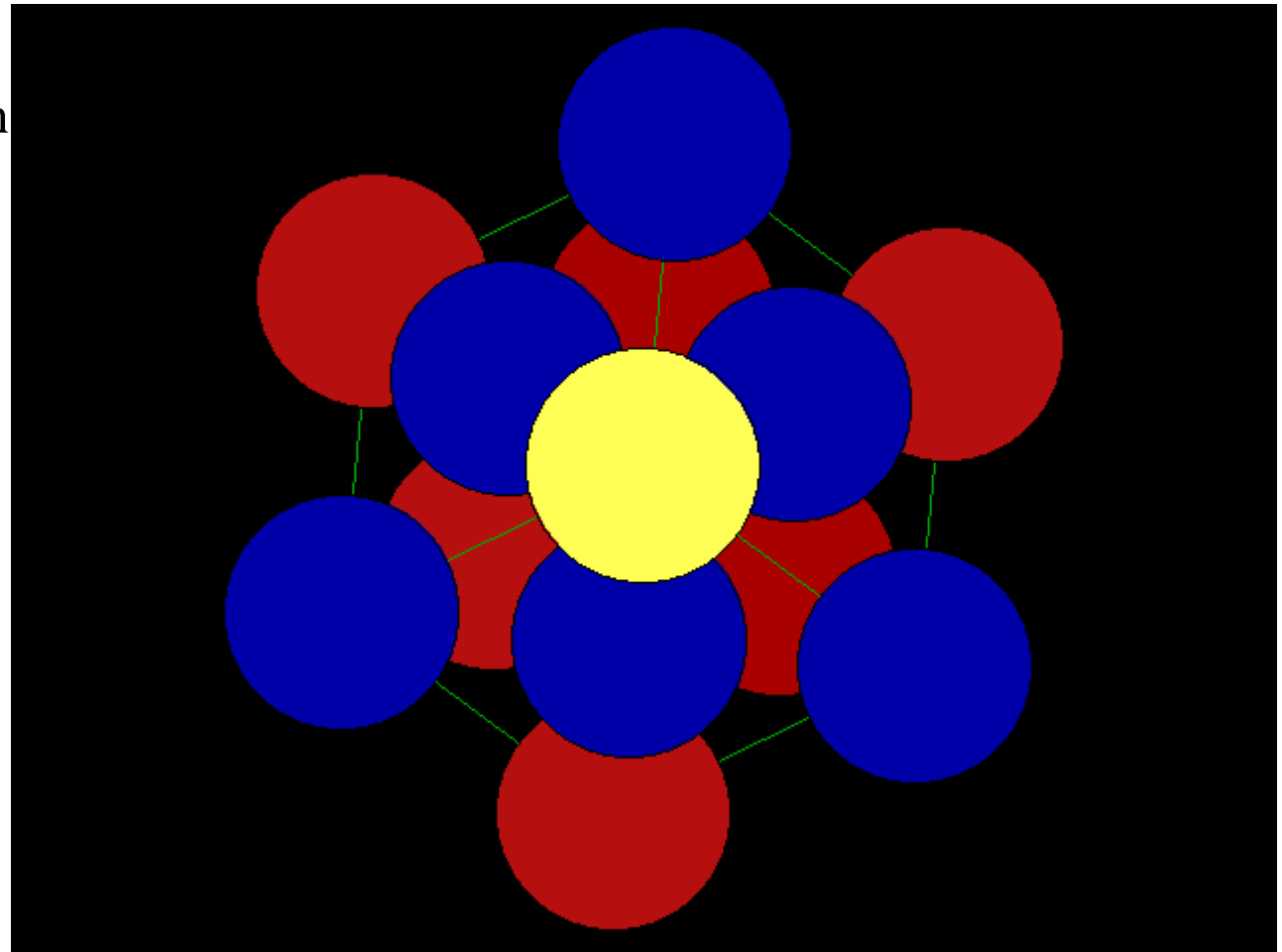
# Closest Packing

Rotating toward a top  
view



# Closest Packing

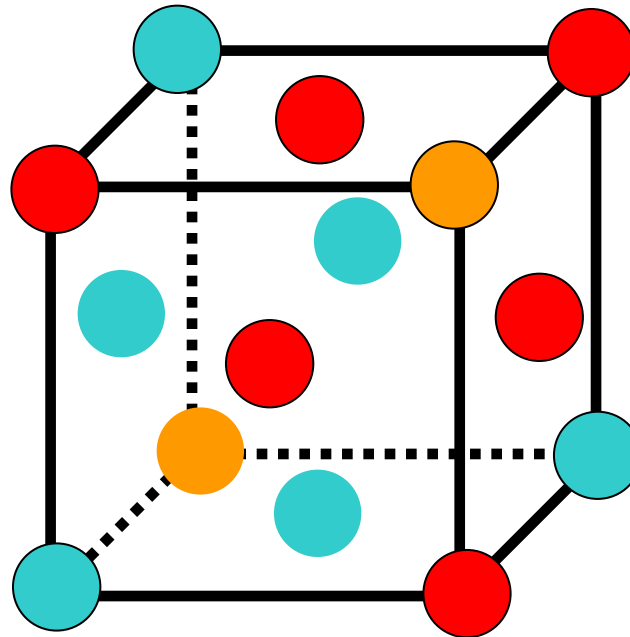
You are looking at a top  
yellow layer A with a  
blue layer C below,  
then a red layer B and  
a yellow layer A again  
at the bottom



## UNIT CELL

Atom on each  
corner

Atom in center of  
each face of the  
cube



Cubic unit cell  
(shape)

spheres touch  
across face  
diagonals  
(?)

MODEL VIEW:

lattice parameter

cube edge 'a'

$$a = 2R\sqrt{2}$$

## number of atoms per unit cell

1/8 of each of the 8 corner atoms

1/2 of each of the 6 face centered atoms

= 4\*

atomic packing factor (APF)

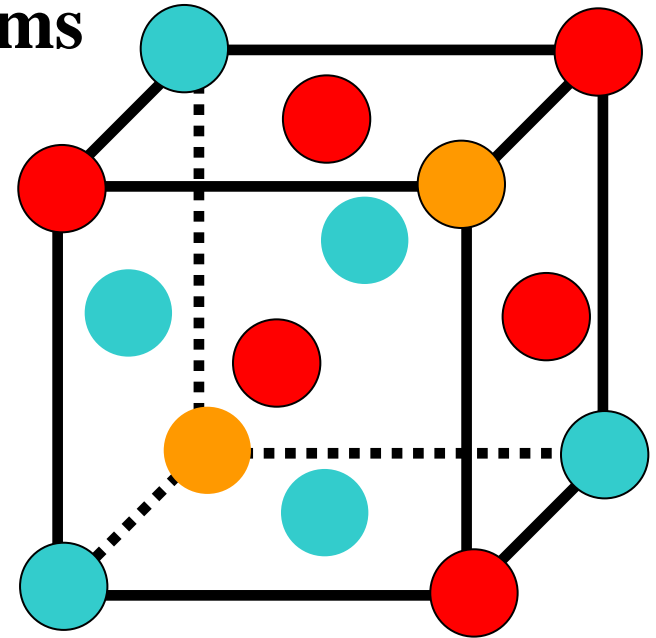
APF = 0.74

-coordination number ?????

*(by inspection of front face)*

4 on corners and 4 on front and rear face centres

= 12\*



### 3. BODY CENTERED CUBIC (BCC)

(e.g. Fe, Cr, W)

Cubic unit cell

(center and corner atoms touch across **cube diagonal** )

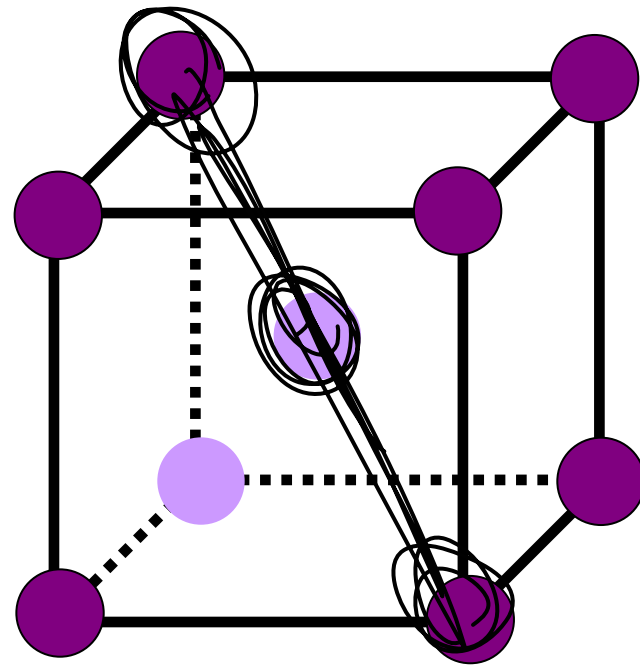
(Not close packed)

lattice parameter

cube edge 'a'

$$a = \frac{4R}{\sqrt{3}}$$

APF  $\rightarrow$  HCP  
FCC





**number of atoms per unit cell =**

$$\frac{8 \text{ corner}}{8 \text{ cubes}}$$

**1/8 of each of the 8 corner atoms**

**1 center atom**

**=2**

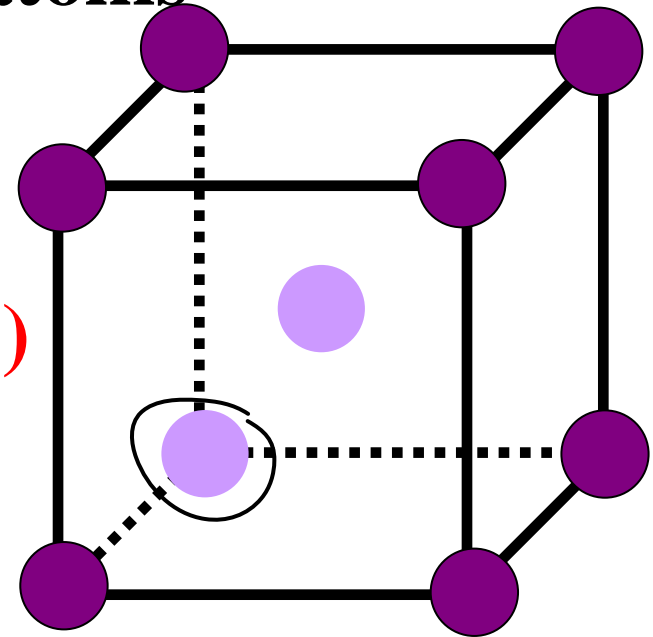
**atomic packing factor (APF)**

**APF = 0.68**

**-coordination number**

*(by inspection of center atom)*

**= 8**



**Check the Wiley website for a decent animation for BCC.**

-crystallographic structure depends on external conditions

(e.g. temp, pressure).....

how it's made → thermal & mechanical  
and the alloying elements

-Change in crystal structure = change in some props

## NOMENCLATURE

### Allotropes and Phases

-an **allotrope** is a crystallographic variant of a **pure** element

-e.g. graphite and diamond are allotropes of carbon

-a **polymorph** (or **phase**) is a crystallographic variant of an **alloy**

-e.g. **martensite** is a phase of steel (Fe/C alloy)