

# Quiz 1

## Solution & Marking Scheme

The mark breakdown and solution of Quiz 1 are shown below.

**If you have questions regarding the marking scheme, please contact:**

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**After contacting the TA, if you are still not satisfied with your quiz marking, please contact Prof. Hamoui.**

**Note: This quiz was marked out of 36, but your mark for Quiz1 was taken out of 30.  
So, for example, if you scored 36 here,  
your mark for Quiz 1 in your final grade will be  $36/30 = 120\%$ .**

□ BJT Parameters:

- npn BJT:  $V_{BEon} = 0.7V$ ,  $V_{BCon} = 0.4V$ ,  $V_{CEsat} = 0.3V$ ,  $\beta = 250$ ,  $V_A = 125V$ .
- pnp BJT:  $|V_{BEon}| = 0.7V$ ,  $|V_{BCon}| = 0.4V$ ,  $|V_{CEsat}| = 0.3V$ ,  $\beta = 50$ ,  $|V_A| = 80V$ .
- Thermal voltage:  $V_T = 25mV$ .

**Specifications:**

$$V_{CC} = +5V$$

$$I_{REF} = 0.5\text{mA}$$

$$R_E = 475\Omega$$

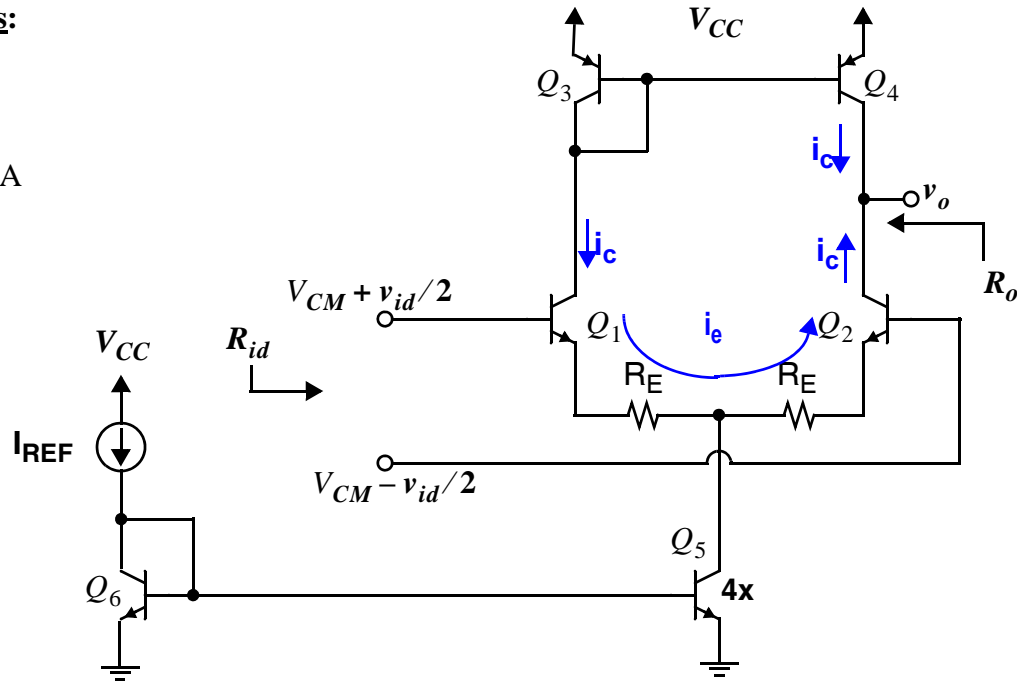


Fig. 1

**Question 1 [30 marks]**

**Note:** This question corresponds to the active-loaded differential pair with emitter-degeneration resistances (presented in Section 7.5.5, solved in class during Lecture # 6 on Jan. 22, and solved during the Tutorial for Prob. 7.68).

**1.1) [2 marks]**

$$I_{E1,2} \cong \frac{4 \times I_{REF}}{2} = \frac{4 \times 0.5\text{mA}}{2} = 1\text{mA}$$

$$r_{e1,2} = \frac{V_T}{I_{E1,2}} \cong \frac{25\text{mV}}{1\text{mA}} = 25\Omega$$

$$R_{id} = 2(\beta + 1)(r_{e1,2} + R_E) = 2(250 + 1)(25\Omega + 475\Omega) = 251\text{k}\Omega$$

**1.2) [4 marks]**

$\alpha \cong 1$ , since the base currents are neglected.

$$I_{C2,4} = \alpha I_{E2} \cong 1\text{mA}$$

$$r_{o2} = \frac{V_{An}}{I_{C2}} = \frac{125\text{V}}{1\text{mA}} = 125\text{k}\Omega$$

$$r_{o4} = \frac{V_{Ap}}{I_{C2}} = \frac{80\text{V}}{1\text{mA}} = 80\text{k}\Omega$$

$$R_o = r_{o2} \parallel r_{o4} = 125\text{k}\Omega \parallel 80\text{k}\Omega = 48.78\text{k}\Omega$$

**Solving directly on the circuit diagram:**

$$i_e = \frac{v_{id}}{2(r_e + R_E)} \quad (\text{see the circuit diagram})$$

$$i_c = \alpha i_e$$

$$v_o = +2i_c R_o \quad (\text{Note: the 2 factor is due to the current-mirror action of the active load Q3-Q4})$$

$$A_d = \frac{v_o}{v_{id}} = \alpha \frac{2R_o}{2(r_e + R_E)} = (1) \frac{(2 \times 48.78\text{k}\Omega)}{2(25\Omega + 475\Omega)} = +97.56\text{V/V}$$

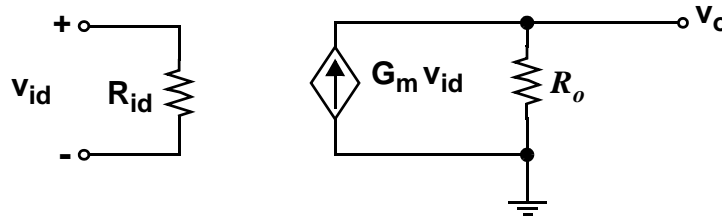
**1.3) [3 marks]**

$$G_m \equiv \left. \frac{i_o}{v_{id}} \right|_{R_L=0} = \frac{2i_c}{v_{id}} = \frac{\alpha}{r_e + R_E} \cong \frac{1}{25\Omega + 475\Omega} = 2\text{mA/V}$$

Note: you can also express  $G_m$  as:  $G_m \equiv \frac{\alpha}{r_e + R_E} = \frac{g_m}{1 + R_E/r_e}$

**1.4) [3 marks]**

The equivalent transconductance amplifier model:



**1.5) [6 marks]**

For Q1 in active mode:

$$\begin{aligned} V_{BC1} &\leq V_{BC,on} \\ \Rightarrow V_{CM} - V_{C1} &\leq V_{BC,on} \quad \text{where } V_{C1} = V_{CC} - |V_{BE,on}| \\ \Rightarrow V_{CM} &\leq V_{BC,on} + V_{CC} - |V_{BE,on}| \\ \Rightarrow V_{CM,max} &= 0.4\text{V} + (5\text{V} - 0.7\text{V}) = 4.7\text{V} \end{aligned}$$

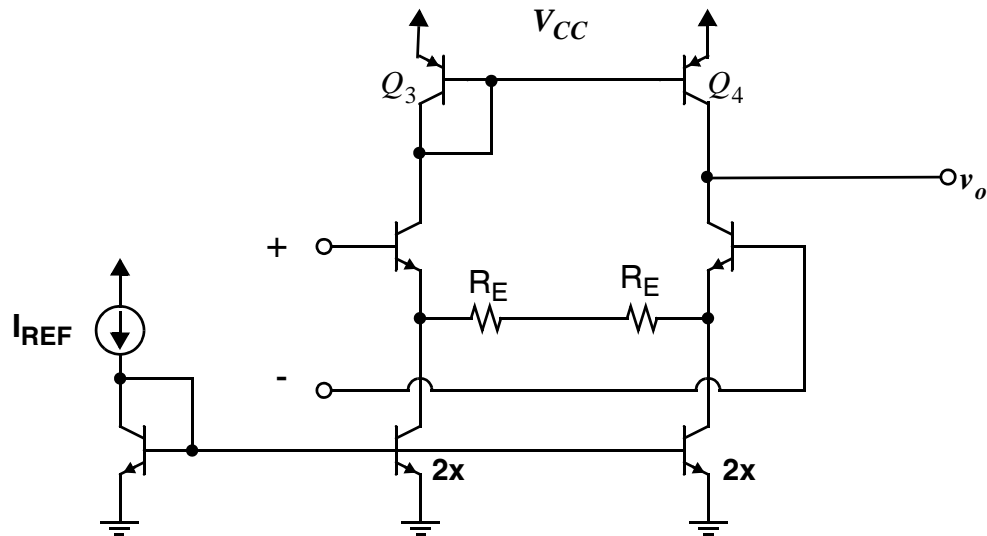
For proper operation of current source (Q5 in active mode):

$$\begin{aligned} V_{CE5} &\geq V_{CE,sat} \\ \Rightarrow V_{CM} - (V_{BE,on} + I_{E1}R_E) &\geq V_{CE,sat} \\ \Rightarrow V_{CM} &\geq V_{CE,sat} + \left( V_{BE,on} + \frac{4 \times I_{REF}}{2} R_E \right) \\ \Rightarrow V_{CM,min} &= 0.4\text{V} + (0.7\text{V} + 1\text{mA} \times 475\Omega) = 1.475\text{V} \end{aligned}$$

Therefore, the common-mode input range is:  $1.475\text{V} \leq V_{CM} \leq 4.7\text{V}$

**Note:** The input common-mode range of the BJT differential pair (section 7.4.4 in the textbook) was derived in class during Lecture #5 on Jan. 20, and solved during the Tutorial for Prob. 7.68, 7.37, and 7.38)

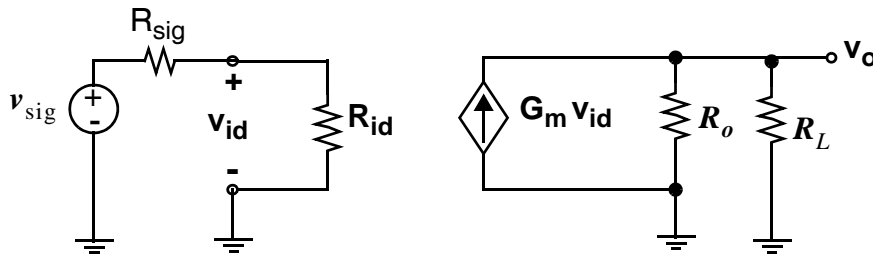
1.6) [6 marks]



Here, no dc current flows through \$R\_E\$. Hence, \$V\_{CM,min}\$ is increased.

**Note:** This idea was presented in class during lecture #10 on Feb. 5 and in the tutorials through Prob. 7.37 and 7.38.

1.7) [6 marks]



$$v_{id} = \frac{R_{id}}{R_{sig} + R_{id}} v_{sig}$$

$$v_o = + (G_m v_{id})(R_o \parallel R_L)$$

$$A_{d, sig} \equiv \frac{v_o}{v_{sig}} = \frac{R_{id}}{R_{sig} + R_{id}} \cdot G_m \cdot (R_o \parallel R_L) = \frac{251k}{251k + 50k} \cdot 2m \cdot (48.78k \parallel 100k) = + 54.68V/V$$

**Question 2: [6 marks]**

**2.1) [3 marks]**

Although there are many advantages to using transistors as active loads for the implementation of differential amplifier stages in an integrated circuit (IC), there is a major advantage in using resistors as loads, which is:

1. For small load values, resistances occupy smaller silicon area.
2. The matching between resistors is better than the matching between transistors.
- 3. The dc level at the output nodes can be accurately predicted.**
4. Less power is dissipated when resistors are used.

**2.2) [3marks]**

Which of the following 4 gain stages has the largest voltage-gain  $A_v = \left| \frac{v_o}{v_i} \right|$  ?

Assume identical transistors, same dc bias currents, and large values for the resistors.

You can ignore the finite output resistance of the BJT.

