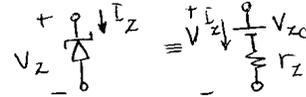


Question #1

(a) Find V_{z0} .

$V_z = 8 \text{ V} \mid @ I = 10 \text{ mA}$

$V_{z0} = V_z + r_z I_z \Rightarrow V_{z0} = 8 - 20 \times 10 \times 10^{-3} = 7.8$

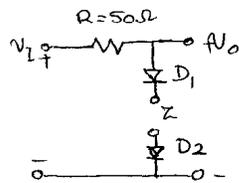


(b)

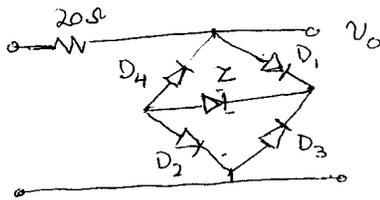
① if $0 < V_I < V_{z0} + 2V_D = 7.8 + 2 \times 0.7 = 9.2 \text{ V}$

- Z is reverse biased but not in breakdown.

- D_4 and D_3 : off



$\Rightarrow V_I = V_O$



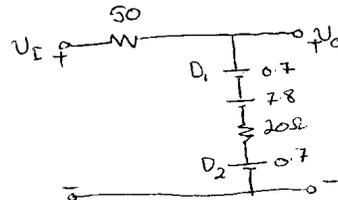
② if $V_I \geq V_{z0} + 2V_D = 9.2$

- D_4 and D_3 : off

- D_1 and D_2 : ON (CVDN)

- Z : Zener breakdown

$\Rightarrow V_O = 9.2 + (V_I - 9.2) \frac{20}{20 + 50}$



$\Rightarrow V_O = \frac{5 \times 9.2}{7} + V_I \frac{20}{20 + 50} = 6.57 + \frac{20}{7} V_I$

if $V_I = 20 \Rightarrow V_O = 9.2 + \frac{20 \times 7.2}{7}$
 $V_O = 12.28 \text{ V}$

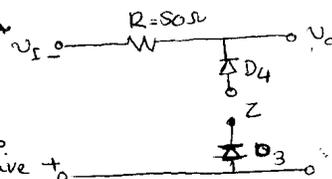
③ if $-9.2 < V_I < 0$

- Z is reverse biased but not in breakdown

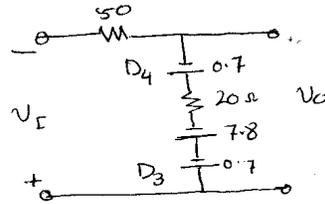
- D_1 and D_2 : off

$V_I = V_O$

V_I is negative

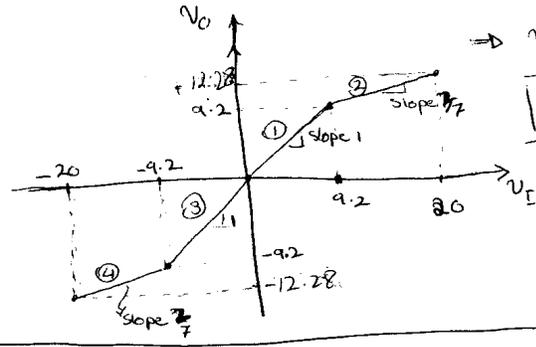


- ④. if $V_I < -9.2$
- D_1 and D_2 : off
- D_3 and D_4 : ON (CVDU)
- Z : Zener breakdown



$$\Rightarrow V_O = -9.2 + (V_I + 9.2) \frac{20}{50+20} = V_I \cdot \frac{2}{7} + 9.2(-1)$$

$$V_O = -6.57 + \frac{2V_I}{7} \quad (V_I \text{ is negative})$$



if $V_I = -20 \Rightarrow V_O = -9.2 + \frac{-20 + 9.2}{7}$

$$V_O = -12.28V$$

Question #2

(a) D_1 : off $\rightarrow \underline{I_{D1} = 0}$

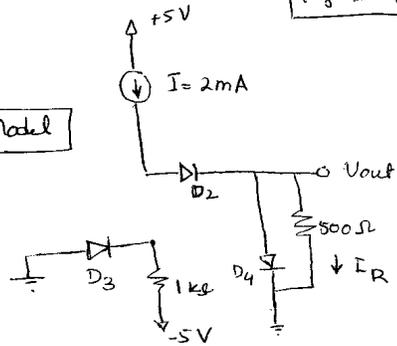
D_3 : $I_{D3} = \frac{-0.7 + 5}{1k} = \underline{4.3 \text{ mA}}$

D_2 : $\underline{I_{D2} = 2 \text{ mA}}$

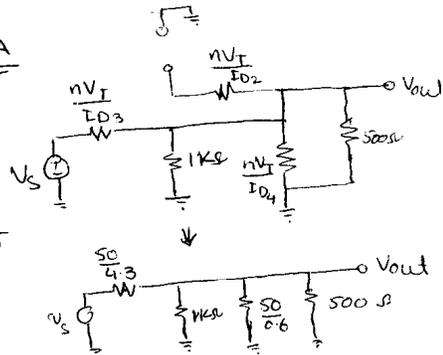
D_4 : $I_R = \frac{0.7}{500\Omega} = 1.4 \text{ mA}$

$I_{D4} = 2 - 1.4 = \underline{0.6 \text{ mA}}$

DC Model



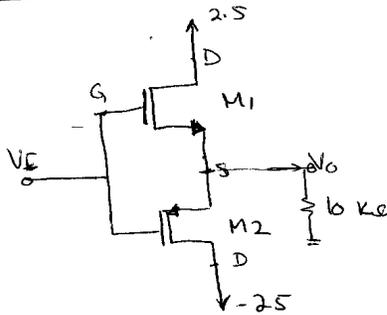
(b) small-signal model



$\frac{V_{out}}{V_s} = \frac{500 \parallel 1k \parallel 83.3}{500 \parallel 1k \parallel 83.3 + 11.63} = 0.85 \text{ V/V}$

Question #3

(a) $V_I = 0$



M1: nMOS

$$\text{sat. } \begin{cases} V_{GS} > V_{tn} \\ V_{DS} > V_{GS} - V_{tn} \\ V_D > V_G - V_{tn} \\ V_{GD} < V_{tn} \end{cases}$$

M2: PMOS

$$\text{sat. } \begin{cases} V_{GS} < V_{tp} \\ V_{DS} < V_{GS} - V_{tp} \\ V_D < V_G - V_{tp} \\ V_{GD} > V_{tp} \end{cases}$$

If $V_I = 0$ because of symmetry $\Rightarrow V_S = 0$

$$\begin{aligned} \Rightarrow M1: V_{GS1} = 0 < V_{tn} &\Rightarrow M1 \text{ Cutoff} \\ \Rightarrow M2: V_{GS2} = 0 > V_{tp} &\Rightarrow M2 \text{ Cutoff} \end{aligned} \Rightarrow I_{DN} = I_{DP} = 0$$

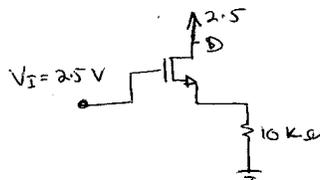
(b) $V_I = 2.5 \text{ V}$

M2: $V_{GD} = 2.5 - (-2.5) = 5 \text{ V}$

If M2 is not in cutoff then $V_{GS} < V_{tp} \Rightarrow V_G - V_S < V_{tp}$
 $\Rightarrow V_S > V_G - V_{tp} = 2.5 - (-1) = 3.5$
Not possible

Therefore, M2 is in cutoff $\Rightarrow I_{DP} = 0$

Assume M1



$$\begin{aligned} V_{GD} = 0 < V_{tn} = 1 \\ V_S < 2.5 \text{ V} \end{aligned} \Rightarrow \text{Assume M1 is in } \underline{\text{Saturation}}$$

$$I_{DN} = \frac{1}{2} k'_n \frac{W}{L} (V_{GS1} - V_{tn})^2$$

$$\downarrow$$

$$\frac{(V_G - V_S - 1)^2}{2.5}$$

$$V_S = I_{DN} 10k$$

$$\Rightarrow I_{DN} = 0.105 \text{ mA} \Rightarrow V_S = 1.04 \text{ V} \Rightarrow V_{GS} = 2.5 - 1.04 > V_{tn}$$

$$V_{DS} > 2.5 - 1.04$$

$$\Rightarrow \text{Saturation} \checkmark$$

b) Another discussion
Notice that

$$V_{GS1} = V_{GS2} = V_I - V_O = 2.5 - V_O.$$

So if $V_{GS1} > V_{tn} \Rightarrow V_{GS2} > 0 \Rightarrow V_{tp}$.

M_2 must be cut off.

And notice that for $V_I = 2.5V$.

$$V_{GS1} = V_{DS1} = 2.5 - V_O.$$

So if M_1 is ON, M_1 must be in saturation.

Assume M_1 sat. M_2 off.

$$\frac{1}{2} k_n' \frac{W}{L} (2.5 - V_O - 1)^2 = \frac{V_O}{10k}$$

$$\frac{1}{2} (1.5 - V_O)^2 = \frac{V_O}{10}$$

$$V_O^2 - 3.2V_O + 2.25 = 0$$

$$V_O = \begin{cases} 2.1V & \longrightarrow \text{drop. } V_I - V_O < V_E \\ 1.04V & \end{cases}$$

↓
Verify M_2

$$V_{GS2} = V_I - V_O = 1.16V > V_{tp} = -1V. \quad M_2 \text{ cutoff.}$$

So M_1 sat. M_2 off.

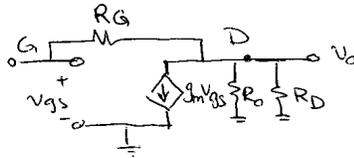
$$i_{DN} = \frac{1}{2} k_n' \frac{W}{L} (1.5 - 1.04)^2 = 0.105 \text{ mA}$$

$$i_{pp} = 0$$

Question #4

a) $\lambda = 0.05 \text{ V}^{-1}$ $V_{th} = 1 \text{ V}$

$V_{GS} = V_G - V_S = 3 - 1.5 = 1.5 > V_t = 1$
 $V_{DS} = V_D - V_S = 3 - 1.5 = 1.5 > V_{GS} - V_t = 1.5 - 1$
 \Rightarrow Saturation



$V_S = 1.5 \text{ V}$, $V_{out(DC)} = 3 \text{ V}$

$I_D = \frac{V_S}{R_S} = \frac{1.5}{7.5} = 0.2 \text{ mA} = \frac{5-3}{10 \text{ k}} = 0.2 \text{ mA}$

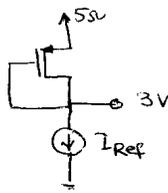
Assume $i_{G1} \rightarrow A_v = \frac{v_o}{v_{in}} = \frac{-g_m V_{GS} (R_D || R_o)}{v_{GS}}$

$g_m = \frac{2 I_D}{V_{GS} - V_t} = \frac{2 \times 0.2 \times 10^{-3}}{3 - 1.5 - 1} = \frac{0.4 \times 10^{-3}}{0.5} = 0.8$

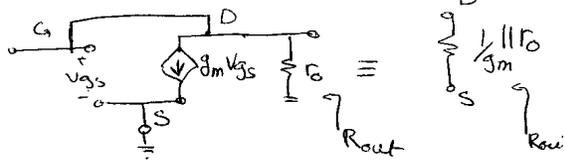
$R_o = \frac{V_A}{I_D} = \frac{1}{0.05} \cdot \frac{1}{0.2 \times 10^{-3}} = \frac{20}{0.2 \times 10^{-3}} = 100 \text{ k}\Omega$

b) $A_v = -0.8 \times 10^{-3} (100 || 110) \times 10^3 = -0.8 \frac{10 \times 100}{110} = -\frac{80}{11} = -7.27$

c)



$I_{ref} = 0.2 \text{ mA}$



$R_{out} = \frac{1}{g_m} || R_o$

$R_o = \frac{V_A}{I_{ref}} = \frac{20}{0.2 \times 10^{-3}} = 100 \text{ k}\Omega$

$g_m = \frac{2 I_{ref}}{V_{GS} - V_{tp}} = \frac{2 \times 0.2 \times 10^{-3}}{3 - 5 - (-1)} = \frac{0.4 \times 10^{-3}}{1} = 0.4 \times 10^{-3}$

$\frac{1}{g_m} = 2.5 \text{ k}\Omega$

$R_{out} = 2.5 \text{ k} || 100 \text{ k} = \frac{2.5 \times 100}{102.5} \text{ k}\Omega = \frac{250}{102.5} \text{ k}\Omega = 2.44 \text{ k}\Omega$