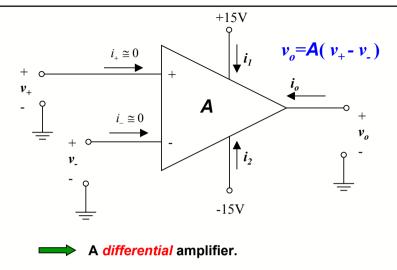
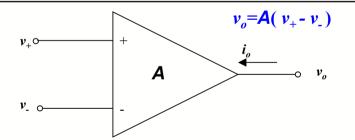
OpAmp Symbol

ECSE 210: Circuit Analysis

Lecture #4: Operational Amplifiers

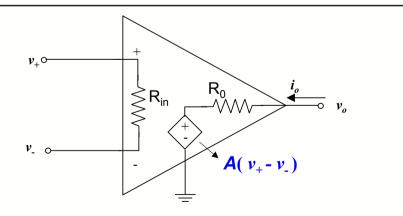


Simplified OpAmp Symbol

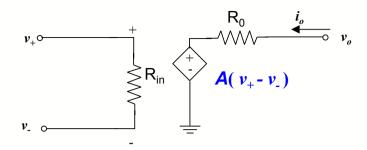


- 1. Supply voltages are not shown.
- 2. Supply currents are not shown. (Be careful with KCL)
- 3. Never do KCL at the reference node (otherwise need to include supply currents).
- 4. KCL at output node v_o is never done unless we want to calculate i_o .

OpAmp Model



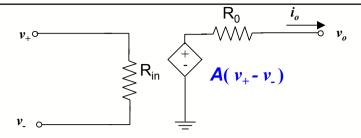
Op-Amp Equivalent Circuit



Based on this circuit, the op-amp is a unilateral device.

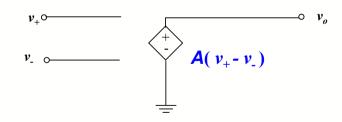
→ The output voltage is determined as a function of the input, *BUT the input voltages are not affected by the output voltage.*

Some Practical Information



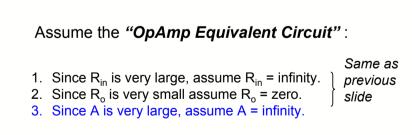
- 1. The input resistance R_{in} is very large, typically in the range of $100k\Omega \rightarrow 1T\Omega$.
- 2. The voltage gain **A** is very high, typically $10^5 \rightarrow 10^7$.
- The output resistance R₀ is very small *compared* to the recommended output load. Typically R₀ is in the range 1Ω→75Ω.
- ➡ These parameters suggest a simpler model!

Simpler Op-Amp Model



- 1. Since R_{in} is very large, assume R_{in} = infinity.
- 2. Since Ro is very small assume $R_0 = zero$
- 3. This model appears on page 84 of the text, Figure 3.7. It depends only on the *open loop* gain *A*.

The Ideal OpAmp Model



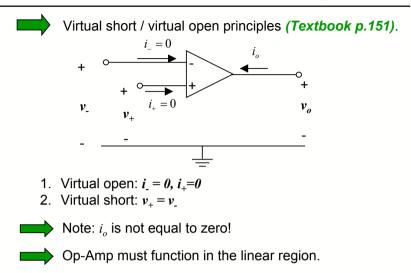
This gives the "Ideal OpAmp Model"

Condition of Linearity

- The *ideal* op-amp is linear.
- For an op-amp to be linear:

$$|v_o| \le v_{sat}$$
 $|i_o| \le i_{sat}$ $\left|\frac{dv_o}{dt}\right| \le SR$

Virtual Short / Virtual Open



Op-Amp Properties

→ <u>Good:</u>

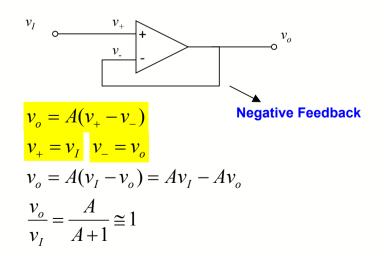
- 1. High input impedance.
- 2. Low output impedance.
- 3. Large gain.

→ <u>Bad:</u>

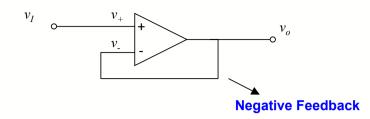
The properties of the op-amp (such as its gain A) are strongly dependent on process variations, temperature variations, etc.

Use closed loop, *negative feedback* configuration.

Voltage Follower



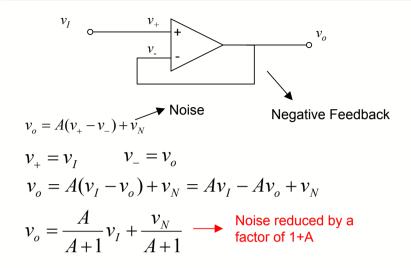
Voltage Follower



Alternatively use virtual short principle for ideal op-amps:



Effect of Feedback on Noise

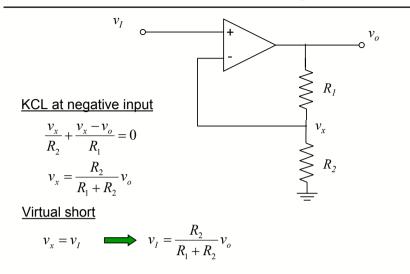


Positive Feedback v_I v_{-} v_o v_o $v_o = A(v_+ - v_-)$ Positive Feedback! $v_+ = v_o$ $v_- = v_I$ $v_o = A(v_o - v_I) = Av_o - Av_I$ $\frac{v_o}{v_I} = \frac{-A}{1-A} \cong 1$ Can be shown to be an unstable configuration.

Nodal Analysis of Op-Amp Circuits

- 1. Make use of the virtual short/virtual open principles.
- 2. Node voltages at the input are equal so one of them can be eliminated.
- 3. The currents at the input are zero and are involved in KCL equations at the *input* nodes.
- 4. The output current is *not* zero.
- Make sure op-amp is in linear region so that virtual open/short principles can be applied (What happens when we have positive feedback?).

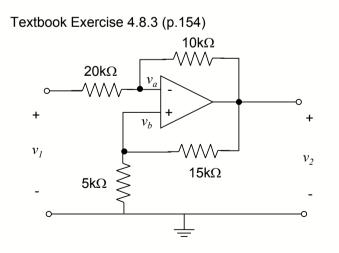
Example: Non-Inverting Amp



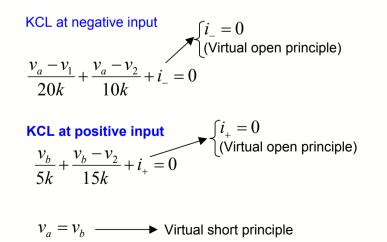
Typical Uses of OpAmps

- 1. Buffer circuit.
- 2. Voltage scaling.
- 3. Analog Computers (solution of differential equations.). OpAmp circuits can be used to perform mathematical operations (addition, subtraction, integration, etc.).
- 4. Negative resistor (active component).
- 5. Active filters.

Example: Inverting Amplifier

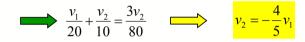


Example: Inverting Amplifier



Example: Inverting Amplifier

First equation: $\xrightarrow{v_a} \frac{v_a}{20} + \frac{v_a}{10} = \frac{v_1}{20} + \frac{v_2}{10} = \frac{3v_a}{20}$ Second equation: $\xrightarrow{v_b} \frac{v_b}{5} + \frac{v_b}{15} = \frac{v_2}{15}$ $4v_b = v_2$ Third equation: $\xrightarrow{v_a} v_a = v_b$



Hints

- 1. Apply KCL at the input of the op-amp and take advantage of the virtual open principle.
- 2. Never apply KCL at the output node of the opamp unless you are asked to calculate its output current.
- 3. Never apply KCL at the reference node. Remember we do not show the currents into the power supplies of the op-amp.
- 4. Make use of the virtual short principle (the input voltages of the op-amp are equal).