

ECSE 210: Circuit Analysis

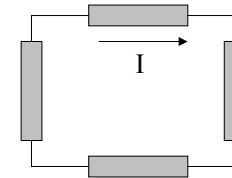
Lecture #1: Introduction

Circuit Analysis

- Design → Creation of a Circuit
- Analysis → Evaluation of a Circuit

Electric Circuit:

An interconnection of electrical elements linked together in a closed path so that electric current may flow.



Analogy: water flow

Linear Electric Circuits

- A linear circuit satisfies the properties of superposition and homogeneity.

Example:

Circuit with input i and output v

$$i \rightarrow v$$

- Superposition:

$$\left. \begin{array}{l} i_1 \rightarrow v_1 \\ i_2 \rightarrow v_2 \end{array} \right\} \rightarrow i_1 + i_2 \rightarrow v_1 + v_2$$

- Homogeneity:

$$i \rightarrow v \rightarrow ki \rightarrow kv$$

Linear Electric Circuits

- Example of a linear element: The resistor

$$\begin{array}{c} + \quad v \quad - \\ \text{---} \text{---} \text{---} \text{---} \text{---} \\ \quad \quad \quad \rightarrow i \end{array} \quad v = iR$$

- Superposition:

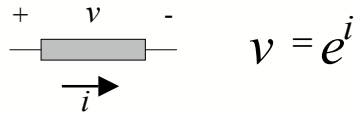
$$\checkmark \quad \left. \begin{array}{l} i_1 \rightarrow v_1 = i_1 R \\ i_2 \rightarrow v_2 = i_2 R \end{array} \right\} \rightarrow i_1 + i_2 \rightarrow v = (i_1 + i_2)R = i_1 R + i_2 R = v_1 + v_2$$

- Homogeneity:

$$\checkmark \quad i \rightarrow v = iR \rightarrow ki \rightarrow kiR = kv$$

Linear Electric Circuits

- Example of a nonlinear element:



- Superposition:

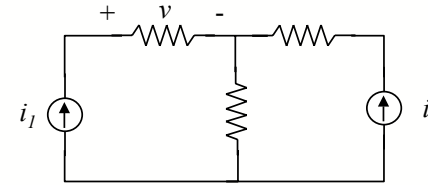
$$\left. \begin{array}{l} \times \quad i_1 \rightarrow v_1 = e^{i_1} \\ \quad \quad i_2 \rightarrow v_2 = e^{i_2} \end{array} \right\} \rightarrow \begin{array}{l} i_1 + i_2 \rightarrow v = e^{i_1 + i_2} \\ \quad \quad \quad \neq e^{i_1} + e^{i_2} \end{array}$$

- Homogeneity:

$$\times \quad i \rightarrow v = e^i \rightarrow ki \rightarrow e^{ki} \neq k e^i$$

Linear Electric Circuits

- Example of superposition



- Remove i_2 and calculate v
- Remove i_1 and calculate v
- Add the two solutions

Circuit Analysis – Basic steps

Given Circuit (Design)



Analysis

1. Identify element models (e.g., $V=IR$ for resistor).
2. Define analysis variables (e.g., currents, voltages).
3. Assemble circuit equations (e.g., KCL, KVL).
4. Solve circuit equations (e.g., matrix methods, computer...).
5. Evaluate circuit performance (e.g., power delivery, dynamic response, frequency response)



Interpretation of results

Circuit Analysis

Note: Circuit analysis yields the “physical” performance of *idealized* electric circuits, without concern for the actual systems represented by the circuits.

- Circuit models are used to approximate real systems;
- Circuit analysis determines the performance of circuit models.
- Electrical engineers use circuits to estimate the performance of real systems and devices.

Question: Do circuit models provide the exact performance of real electric circuits?

Some SI Units

Quantity	Unit	Symbol
length	Meter	m
time	second	s
charge	Coulomb	C
current	Ampere	A
voltage	Volt	V
resistance	Ohm	Ω
capacitance	Farad	F
inductance	Henry	H
energy	Joule	J
power	Watt	W

Standard SI prefixes

Prefix	Symbol	Multiplier
pico	p	10^{-12}
nano	n	10^{-9}
micro	μ	10^{-6}
milli	m	10^{-3}
kilo	k	10^{+3}
mega	M	10^{+6}
giga	G	10^{+9}
tera	T	10^{+12}

Standard SI prefixes

Examples:

0.0015 Amperes should be written 1.5mA
3,500,000 Watts should be written 3.5MW
0.0012 mA should be written as 1.2 μ A

➡ Concept of significant figures vs. decimal places

Standard SI prefixes

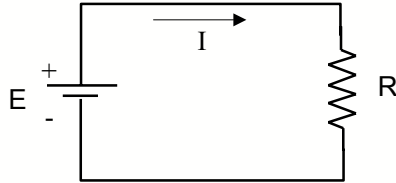
Examples:

0.0015 Amperes should be written 1.5mA
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➡ Concept of significant figures vs. decimal places

More Basics - Current

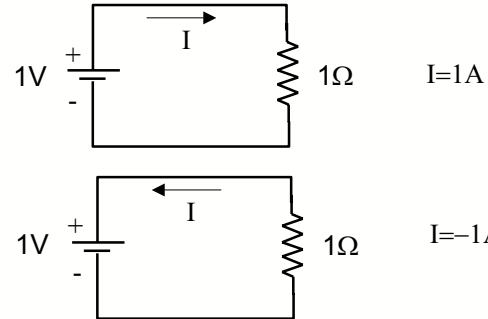
Circuit analysis **current variables** must be defined with prescribed **directions**.



Does it matter which direction we assign to the current?

More Basics - Current

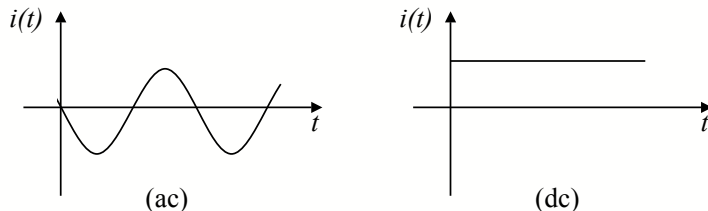
Current variable need not correspond to **physical** current flow.



More Basics - Current

There are two types of current:

- Time-invariant (stationary), commonly known as **direct current** (dc).
- Time-varying, e.g, the sinusoidal **alternating current** (ac)



Voltage or Potential

Charge in motion  Energy Transfer

- The **voltage between two points** in a circuit is defined as the difference in energy level of a positive unit charge located at each of the two points.
- In other words, the voltage between two points is the energy required to move a positive unit charge between the two points.
- Circuit analysis voltage variables must be defined with prescribed orientation – to identify the point at higher potential.
- The “+” and “-” signs are used: “+” marks the point of higher potential and “-” marks the point of lower potential.

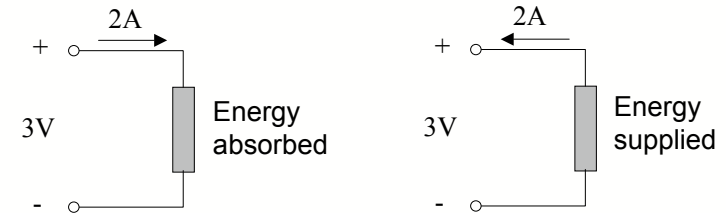
Voltage or Potential

Does it make a difference which orientation we assign to a voltage variable?

Resist mixing variables and values.

Be consistent.

Energy Transfer



By definition (passive sign convention)

- Positive current into positive terminal → energy absorbed.
- Positive current into negative terminal → energy supplied.

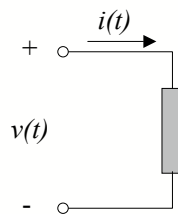
Question: Where does the absorbed (supplied) energy come from (go to)?

Power

Power flow in an electric circuit is defined by the “rate of movement of energy” in the circuit.

$$P = VI \quad \text{or} \quad p(t) = v(t)i(t)$$

with the passive sign convention (psc) assumed.



Under these conditions (psc), if $p(t)$ is **positive** then power is **absorbed** by the element; if $p(t)$ is **negative**, then power is **supplied** by the element.

Circuit Elements

- In circuit analysis, physical circuit elements are represented by abstract mathematical models which describe their behavior.
- When we refer to a circuit element we actually mean the mathematical model that describes its behavior.
- In this course, all the circuit elements are terminal devices, completely characterized by the current through the element and/or the voltage across it.

Passive vs. Active Elements

Two types of elements: active and passive:

- Active elements can generate energy; e.g., batteries and generators are active.
- Passive elements can't generate energy (but some can store energy); resistors, capacitors and inductors are passive.

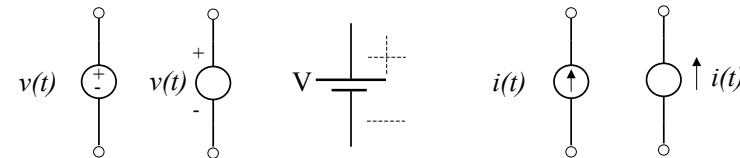
Four Basic Active Elements

Independent Voltage Source:

Two terminal element that maintains a specified voltage between its terminals regardless of the current through it.

Independent Current Source:

Two terminal element that maintains a specified current flow regardless of the voltage across its terminals.



Four Basic Active Elements

Dependent (controlled) Voltage Source:

Two terminal element that maintains a specified voltage between its terminals that is determined by another voltage or current elsewhere in the circuit.

Dependent (controlled) Current Source:

Two terminal element that maintains a specified current flow that is determined by another current or voltage elsewhere in the circuit.

Four Basic Active Elements

