

**SUGGESTED SOLUTIONS**

**Assignment I**

Winter 2008

1. a
2. e
3. a
4. e
5. a
6. e

7. a  $(1+10\%/4)^4 - (1+9\%/365)^{365}$

8. a see below for full solution

9. c see below for full solution

10. A  $-\$100(PVA_{3,10\%}) + \$300(PVA_{4,10\%})(PV_{3,10\%})$   
 $= -\$100(2.4869) + \$300(3.1699)(.7513) = \$466$

11. C c)  $D(CVAF_{8\%,6}) = 10,000 \times 5 (PVAF_{18\%,3}) (1.18)$   
 $D (7.3359) = 50,000 (2.1743) (1.18)$   
 $D = 17,487.11 = \$17,500$

12. B  $\$100,000 = \$9,456(PVIFA_{i,12})$   
 $PVIFA_{i,12} = 10.5753 \quad i = 2\% \text{ per month.}$

Amortization table:

	Beg			End
Month	Balance	Interest	Principal	Balance
1	\$100,000.00	\$2,000.00	\$7,456.00	\$92,544.00
2	92,544.00	1,850.88	7,605.12	84,938.88
3	84,938.88	1,698.78	7,757.22	77,181.66

13. C

$\$20,000 = \$444.89(PVIFA_{i,60})$   
 $PVIFA_{i,60} = 44.9549 \quad i = 1\%. \text{ Annual} = 1\% \times 12 = 12\%$

14. B

15. B  $\$1,297.58 = \$50 (PVA_{20,YTM}) + \$1,000 (PV_{20,YTM})$   
 $YTM \text{ (semiannual rate)} = 3\%. \text{ Annual yield} = 6\%$

16. A Market price =  $\$50 (PVA_{16,6\%}) + \$1,000 (PV_{16,6\%}) = \$898.94$

17. B  $[(45 - x) + .83] / x = .3888 \quad x = 33$

18. B  $\$40 = \$2 / (.14 - g) \quad g = 9\%$

19. A

t	Cash Flow
1	$4(1.15) = 4.60$
2	$4(1.15)^1 = 5.29$
3	$4(1.15)^2 = 6.08$
P3	$6.08(1.10) / (.14 - .10) = 167.29$
Po	$4.60/1.14 + 5.29/(1.14)^2 + (6.08 + 167.29) / (1.14)^3 = 125$

20. D Solution is  $80,000 = 5000 + 5000(1.05) / (.12 - .05)$

21. C  $\$40,000 = \$11,435 (PVAF_{18\%,n})$   
 $3.4980 = (PVAF_{18\%,n}) \text{ where } n = 6 \text{ years}$

22. e)  $(\$40,000 - \$10,000) (CF_{18\%,4}) = 30,000 (1.9388) = \$58,164 = \$58,200$

23. e)  $\$1.08 (1 + g)^5 = \$1.59$ , where  $g = 8.04\%$ ; Dividend '95:  $\$1.59 \times 40\% = \$0.636$   
 $k_s = (0.636) (1.08) / 17 + .08 = 12\%$

24. E =  $(\$30 + \$7) (10\%) = \$3.70$ , which represents an increase of  $85\% = 3.7/2$

25. d) Year 1:  $\$500 (PV_{10\%,1}) = \$500 (0.9091) = \$455$   
 Year 2:  $\$700 (PV_{10\%,2}) = \$700 (0.8264) = 578$   
 Year 3:  $\$1,400 (PV_{10\%,3}) = \$1,400 (0.7513) = 1,052$   
 Year 4:  $\$1,400 (PV_{10\%,4}) = \$1,400 (0.6830) = 956$

PV of the series:  $\$3,041$

$\$3,041 = A (PVAF_{10\%,4}) \quad \$3,041 = A (3.1699) \quad A = \$959 = \$960$

26. b)  $\$23.49 \gg$

$$\text{\$ in account \#1:} = 500FV(5\%,4) = \$607.75$$

$$\text{\$ in account \#2:} = 500FV(6\%,4) = \$631.24$$

$$\text{Difference} = \$23.49$$

27) d) \$90.99

Let X = amount you need to deposit in addition to the \$600 company deposit

The future value of the deposits (an annuity) should equal the present value of the withdrawals

You can think of this problem as being similar to a loan represented by the future value of the deposits and payments in the form of the \$2,000 withdrawals. These should be equal.

$$\text{You get: } (600+X)FVA(.6667\%,180) = 2,000PVA(.6667\%,240), \text{ solve to get } X = \$90.99$$

Where .6667% is the effective monthly interest rate (the 8% APR divided by 12)

28) d.) 9.75-9.95%

By calculator the semi-annual YTM is 4.95% then multiply by 2 to get an annual 9.90%

Using the approximation you would get a semi-annual YTM of 4.90% or an annual 9.79%

Calculator steps to get semi-annual YTM are: -887.76, PV; 35, PMT; 1,000 FV; CPT, I.

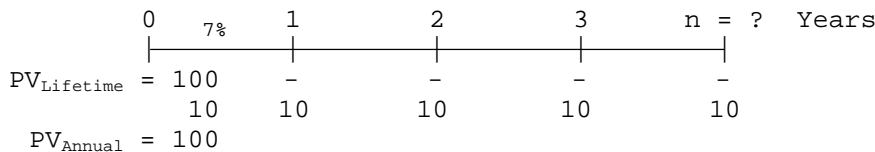
29) e) \$29.40

$$P(0) = [1.40 \cdot 1.05] / [1 - .05] = \$29.40$$

30) a) \$1.21

$$P(0) = [12 / .15] PV(15\%,30) = \$1.21 \text{ The present value of a delayed perpetuity that has no growth (g = 0)}$$

8. Time Line:



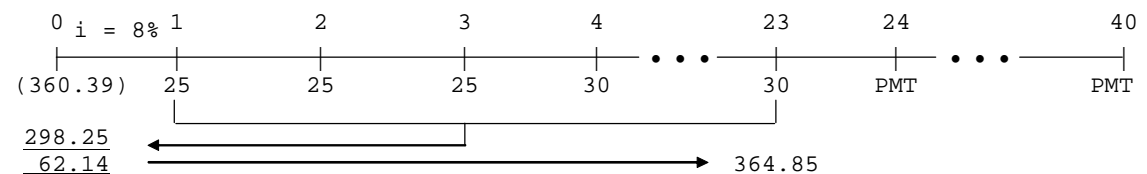
Financial calculator solution:

Inputs: I = 7; PV = -90; PMT = 10; FV = 0. Output: N = 14.695 ≈ 15 years.

9. c

**Required annuity payments**

**Answer: c Diff: T**



Calculate the NPV of payments in Years 1-23:

CF<sub>0</sub> = 0; CF<sub>1-3</sub> = 25; CF<sub>4-23</sub> = 30; I = 8; and then solve for NPV = \$298.25.

Difference between the security's price and PV of payments:

$$\$360.39 - \$298.25 = \$62.14.$$

Calculate the FV of the difference between the purchase price and PV of payments, Years 1-23:

$$N = 23; I = 8; PV = -62.14; PMT = 0; \text{ and then solve for FV} = \$364.85.$$

Calculate the value of the annuity payments in Years 24-40:

$$N = 17; I = 8; PV = -364.85; FV = 0; \text{ and then solve for PMT} = \$40.$$