COPULAS

Definind variables for copulas

Select cell, click Define Distribution



Equivalent of typing this formula in the cell: =RiskUniform(0.45,0.55,RiskStatic(0.5)) Drag distribution to other cells

Select the 3 cells containing the variables, then click define copulas



Select t copula and type in 0.7 (correlations)



Alternatively, select Clayton Copula



	А	В	С	D	E	F	G	н	Ι
1	0.5	0.5	0.5				@RISK Copu		
2							Туре	GumbelR	
3							Dimension	3	
4							Parameter	2.000	
5									
6									
7									

Then when you click on the cells, they are linked with the copula by their formula A1: =RiskUniform(0.45,0.55,RiskStatic(0.5),RiskCopula(Copula1,1)) =RiskUniform(0.45,0.55,RiskStatic(0.5),RiskCopula(Copula1,2)) =RiskUniform(0.45,0.55,RiskStatic(0.5),RiskCopula(Copula1,3))

Set # iterations to 5000 then start simulation

Reverse engineer correlations if given results

Click Excel reports / Simulation data inputs: Shows you input data 💵 🗄 ち・ ぐ・ 🕫 Book2 - Excel HOME INSERT PAGE LAYOUT FORMULAS ADD-INS DATA REVIEW VIEW Capital IQ M* Direct Q 100 Iterations 5000 ÷ Kale Summa fx ▲ ✓ * V 4 Simulations 1 Ŧ T Define F Define Add Insert Define Distribution Model Data Start Excel Browse Settings 🖉 🖉 🛃 🏝 Simulation Reports Results I Xi 🖅 Distributions Output Function - Correlations Fitting Vindow Viewer Model Simulation Results <u>F</u>it.. Bat X \checkmark **f**x C10 Fit Fit ! RiskExcel12_EN С В н т 1 <u>A</u>rti Tell me more **@RISK Input Data** Performed By: Kingf00 Date: April-05-16 7:40:16 PM 5 Name 6 Description 0.45.0.5! RiskUnifo rm(0.45,0.5! RiskUnifo m(0.45,0.55,RiskStatic(0.5),RiskCopula(Copula1,3)) 7 Iteration / Cell \$A\$1 \$8\$1 \$C\$1 0.54541077 0.546978829 0.523940688 8 0.546746982 0.538176714 0.532025839 q 0.540775351 10 0.508073235 0.521681319 0.521726422 0.488145771 11 0.514806403 0.481488884 0.528207972 12 13 6 0.480172355 0.471915826 0.470473693 0.484488909 0.45664034 0.494334564 14 0.484053165 0.47149556 0.458937383 15 0.471922468 0.47754231 0.50638331 9 16 17 10 0.504068215 0.488949021 0.507445888 11 0.46240074 0.466022802 0.468792669 18 12 0.534967192 0.485014765 0.507062089 19 20 13 0.486298885 0.467562227 0.503195779 Tells you best fit is uniform distribution (which is what was originally inputted into the variable

Fit then write to cell

Select second column/Distribution fitting

Could also fit copula:

<u>~ =</u>	E .	5 ° C	÷ – –								Booká	2 - Excel				
FIL	E	HOME	INSERT	PAGE L	AYOUT	FORMUL	AS D	ATA REV	IEW	VIEW	ADD-INS	Ca	oital IQ	M* [Direct	D
De Distrik	fine butions	Add Output	fx Insert Function +	Define Correlations	Distribut Fitting	tion Mode	I Data w Viewer	Iterations Simulations Settings	5000 1	- - - -	Start Simulation	Excel Reports	Browse Results	Ka Su V De	immary efine Filt	ters %
				Define	Correlatio	n <u>M</u> atrix			Simul	ation			Re	esults		
D49	77	-	: X	Define	<u>C</u> opula											
				<u>F</u> it Cop	oula				-	-						
		В		-			- E		F	G	Н	1		J	K	(
955	4948		0.54	8296691	Fit (Copula			_							
956	4949		0.40	00000007		RiskExcel1	2_EN									
4957	4950		0.51	6454307		Tell me mo	re									
4958	4951		0.40	0951225	0.4997	E4202	0.49614	242								
4959	4052		0.51	027440E	0.4667	27272	0.47555	1727								
4960	4555		0.47	02/1403	0.5005	0/120	0.47330	549								
4961	4954		0.4	0520055	0.54510	04246	0.343320	2005								
4962	4955		0.4	0240796	0.45150	00949	0.467370	1021								
4963	4957		0.40	7920427	0.4515	72721	0.403724	444								
4964	4958		0.50	7405849	0.5035	31673	0.50378	744								
4965	4959		0.49	2426138	0.4830	91629	0.50265	5303								
4966	4960		0.52	6493455	0 4805	31927	0.487071	7414								
4967	4961		0.51	5281103	0.49730	00711	0.545285	5781								
4900	4962		0.49	95022616	0.5351	67368	0.492342	2712								
4909	4963		0.47	3981633	0.4670	16086	0.468965	5211								
4970	4964		0.48	32465019	0.5199	30314	0.493948	3599								
4971	4965		0.48	37341592	0.48590	01812	0.497963	3522								
4972	4966		0.54	5776341	0.53793	32584	0.500142	2918								
4974	4967		0.45	1492721	0.47337	75428	0.464178	3407								
4975	4968		0.4	852447	0.48177	79886	0.46294	1739								
4976	4969		0.5	3342751	0.5215	17275	0.538808	3936								
4977	4970		0.45	6276715	0.4573	32601	0.45540	051					0.5			
4978	4971		0.53	32764113	0.53484	40368	0.535174	4639				0.49	9995			
4979	4972		0.51	7616696	0.5153	57309	0.485059	9518								
4980	4973		0.46	4968975	0.4567	5923	0.469128	3321								
4981	4974		0.49	4881666	0.5115	56347	0.500646	5488								
4982	4975		0.48	35815584	0.45776	65879	0.486539	9635								
4983	4976		0.51	18064826	0.5376	31673	0.539673	3019								
409.4	4977		0.49	5240564	0.4900	69133	0.509412	2049								

			@RJSK - Fit Copulas to Data
5,0.55	RiskUniform(0.45,0.	5! RiskUniform	Data Set
	\$B\$1	\$C\$1	
3	0.54541077	0.54697	Range c8:E5007
4	0.546746982	0.53202	Variable Names in First Row
5	0.540775351	0.52168	Data Already Demarginalized
1	0.521726422	0.48814	
2	0.514806403	0.48148	Fitting
5	0.471915826	0.47047	Method Maximum Likelihood Estimation (High Accuracy)
Э	0.45664034	0.49433	
5	0.47149556	0.45893	V Gaussian Elliptical copula
3	0.47754231	0.50638	Clayton Archimedean copula
5	0.488949021	0.50744	ClaytonR ClaytonR copula with all variables reversed
	0.466022802	0.46879	Gumbel Archimedean copula
2	0.485014765	0.50706	GumbelR GumbelR copula with all variables reversed
5	0.467562227	0.50319	
1	0.472752389	0.45915	
3	0.460190674	0.48114	
2	0.462230463	0.48630	
)	0.471112874	0.47365	
Э	0.489390308	0.49777	Load Fit From File OK Cancel
3	0.456940251	0.47699	
	0.465084298	0.452831	003

Tells you Clayton is the best – retrieved all information that was originally inputted. Write to spreadsheet – will write copula on excel

@RISK Copula: Copula1							
Туре	Clayton						
Dimension	3						
Parameter	1.442						

Application: Stocks, want to know correlation Define Distributions:



1	@RISK Inc	RISK Input Data			l Binomial	Cumul	Discrete	Expon	Gamma	General	Histogrm	
2	Performed By: King Date: April-05-16 7:	1600 140: 16 PM										
4												
5	Name			Lognorm	Normal	Pert	Poisson	Triang	Trigen	Uniform	Vary	
6	Description	RiskUniform(0.45,0.5	RiskU									
7	Iteration / Cell	SAS1	\$8\$1									
8	1	0.523940688	0	Weibul								
9	2	0.538176714	0.									
10	3	0.508073235	0.									
11	4	0.535883581	0.									
12	5	0.528207972	0.	<u></u>				Make Eavorit	s l sala	et Distribution	Cancel	
13	6	0.480172355	oll	•				Makeravona	- <u>Jeic</u>	CC DIStribution		J
14	7	0.484488909	0.4	5664034	0.494334564		Para	meter 1.4	42			
15	8	0.484053165	0.4	7149556	0.458937383				_			
16	9	0.471922468	0.4	7754231	0.50638331							
17	10	0.504068215	0.48	8949021	0.507445888			10				
18	11	0.46240074	0.46	6022802	0.468792669		The second se					
19	12	0.534967192	0.48	35014765	0.507062089							
20	13	0.486298885	0.46	7562227	0.503195779							



Then select a uniform distribution

erformed By: Kingf00 ate: April-05-16 7:40:16 PM		Tell me mo	re		
me					
scription	RiskUniform(0.45,0.	5! RiskUniform(0.45,0	5! RiskUniform(0.45,0.5)	5,RiskStatic(0.5),Risk	Copula(Copula1,3))
ration / Cell	\$A\$1	\$B\$1	\$C\$1		
	0.523940688	0.54541077	0.546978829		
	0.538176714	0.546746982	0.532025839		
	0.508073235	0.540775351	0.521681319		
	0.535883581	0.521726422	0.488145771		@RISK Copula: Copula:
	0.528207972	0.514806403	0.481488884		Type Clayton
	0.480172355	0.471915826	0.470473693		Dimension
	0.484488909	0.45664034	0.494334564		Parameter 1.442
	0.484053165	0.47149556	0.458937383		,
	0.471922468	0.47754231	0.50638331		
	0.504068215	0.488949021	0.507445888		10
	0.46240074	0.466022802	0.468792669		0
	0.534967192	0.485014765	0.507062089		-25
	0.486298885	0.467562227	0.503195779		20
	0.466801101	0.472752389	0.459155227		
	0.505350268	0.460190674	0.481147482		
	0.513634612	0.462230463	0.48630067		
	0.4507355000	0.074440074	0.433650363	i	

Now link them using the copula we just built.

Click in the copula

III @RISK - I	Define Copula		
Name Location Copula Type	Eopula 1 H11:114 Clayton V 0-Parameter	1.44205	
	Missing - 1	Missing - 2	Missing - 3
Missing - 1			E
Missing - 2			
	a)		Palata OK Count

Edit copula, then attachement editor

1 5 C	×				Book2 -	Excel	
🕕 @RISK - Defi	ne Copula		-	-	-		astre
Name	Copula 1						
Location	H11:14						Adv
Copula Type	Clayton 💌	θ-Parameter	1.44205				Anal
	Clayton						
1 H17	- 10 / Parameter					Attach More	e Inputs
2 H19	- 12 / Parameter					Detach	Inputs
• 3						Resiz	.e
4 H18	- 11 / Parameter					Instan	
						Inistan	
0					Delete	ОК	Cancel
	0.513634612	0.462230463	0.48630067	_			
17	0.462735089	0 471112874	0.473652767				

Attach inputs - add cells just created



Select one of the input cells / Start simulation.





Have 3 stocks.

	Stock 1		Stock 2		Sto	ck 3
Mean Growth Rate		12%		18%		25%
Volatility		25%		35%		50%
	\$		\$		\$	
Initial Stock Price	20		30		40	
# Shares Bought		1000		750		500

\$ Initial Portfolio Value 62,500

Set: G1=RiskNormal(0,1) H1= RiskNormal(0,1) I1= RiskNormal(0,1)

Select cells / define copulas



Set final stock price = [START_STOCK_PRICE]*exp(([GROWTH]-.5*[VOLATILITY]^2)*[TIME]+[VOLATILITY]*sqrt(TIME)^0.5*RISK_NORMAL)

Calculate ARR Add output to the cell containing ARR:

x	•	o- ∂	-							@R	ISK Example	e File List [Read-Only] - E
F	ILE	HOME	INSERT	PAGE LAY	OUT I	FORMI	JLAS	DATA	REVIEW	/ VI	ew ad	D-INS	Capital IQ
	Define Add Insert Define Distribut						del Da	Itera Sim ta	ulations	5000 1	v v Sta	rt Ex	cel Browse
Dist	ributions	Output F	unction • (Correlations * Model	Fitting *	Wind	low Viev	ver Sett	ings <u> </u>	🕶 🚾 🛛 Simulatio	Simula ' Simula	ation Rep	orts Results Res
G	1	Add Ou	Itput		3	/B8)/2	2						
		Add the cell (or output.	e current se range of ce	elected spreads ells) as a simula	heet tion	-	D	E	F		G	н	Ι
1	Mean G		kEvcel12	FN		Sto %	ck 3 25%				0	() 0
3	Volatilit	Tel	I me more		9	%	50%			Final Stock Prices			
4	Initial S	tock Pric	e	Ş 20	Ş 30	\$	40				23.885	38.042	51.361
5	# Shares	Bought		1000	75	0	500						
6													
7										Fina	al Portfoli	o Value	
8	Initial P	ortfolio	Value	\$ 62,500						\$	78,097		
9													
10										Ann	ual Rate o	of Return	
11											4.84%		
12													
	1												

Start simulation

What is the probability to make a loss?

Probability of a loss =RiskTarget(G11,0)

Value at Risk for 99% =RiskPercentile(ARR, 0.01)*INNITIAL_PORTFOLIO_VALUE

Change copula to Gaussian Copula. Chances of losing should be lower.

Click in the copula, define copula

x	🗄 🕤 👌 🚦	•		@RISK Example File L	ist [Read-Only] -	Excel		
F	ILE HOME INSERT	PAGE LAYOUT	FORMULAS DATA REVIEW	V VIEW ADD-INS	Capital IQ	M* Direct Da	atastream @R	USK
Dist	Define Add Insert tributions Output Function ~	Define Correlations - Define Correlation J Define <u>Correlation</u>	Matrix	5000 → 1 → Simulation Simulation	Excel Browse Reports Results Re	Summary Define Filters	Advanced Ri Analyses - Optin	ISK nizer + S Tools
	•	Fit Copula.	no Conula	G	I	I K		м
1		Stock 1 St	RiskExcel12_EN	0	0 0	, K		
2	Volatility	25%	Fell me more	Final Stock Prices				
4	Initial Stock Price	\$ 20 \$ 3	0 \$ 40	23.885 38	.042 51.361			
5	# Shares Bought	1000 75	50 500					
6								
7				Final Portfolio Valu	Je			
8	Initial Portfolio Value	\$ 62,500		\$ 78,097				
9								
10				Annual Rate of Ret	urn	Probab	ility of a loss	
11				4.84%		0.255	7401	
12								
13						VAR		
14						-\$9,46	4.38	
15								
16								

Change to Gaussian Copula

T and Gaussian copulas should be fairly similar in terms of probability of default. But looking at the tails (99% VAR), should be more of a difference; Gaussian copula is more conservative (but t coppula is a more accurate description of stock market.